

GOVERNMENT OF PEOPLE'S REPUBLIC OF BANGLADESH
MINISTRY OF LOCAL GOVERNMENT & RURAL DEVELOPMENT
LOCAL GOVERNMENT ENGINEERING DEPARTMENT (LGED)

ROAD STRUCTURES MANUAL FOR DOUBLE LANE BRIDGES

PART-C DESIGN EXAMPLES OF BRIDGES, CULVERTS AND SLOPE PROTECTION WORKS



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Manual on RC Girder & PC Girder Bridges

Part C- Design Examples

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1.1.1.2 Geometrical Data and material properties

Slab	Thickness of deck	= 200 mm = 0.2 m.
	Thickness of WC	= 50 mm = 0.05 m.
	Side walk width	= 875 mm = 0.875 m.
	Overall girder length	= 25650 mm = 25.65 m.
Railing	Cross section of rail post	= 200 mm x 200 mm.
	Height of rail post above deck	= 1105 mm = 1.105 m.
	Cross section of rail bar	= 185 mm x 150 mm.
	Rail post spacing	= 1580 mm = 1.58 m.
	Number of rail posts	= 18
Girder	c/c girder spacing	= 1850 mm = 1.85 m.
	Height of Girder web	= 1800 mm = 1.8 m.
	Girder width	= 460 mm = 0.46 m.
Material properties	Concrete strength, f_c'	= 25 MPa.
	Yield strength of steel, f_y	= 400 MPa.
	Unit wt. of concrete	= 24 kN/m ³ .
	Unit wt. of wearing course	= 23 kN/m ³ .

1.1.3 Structural analysis

1.1.3.1 Interior slab

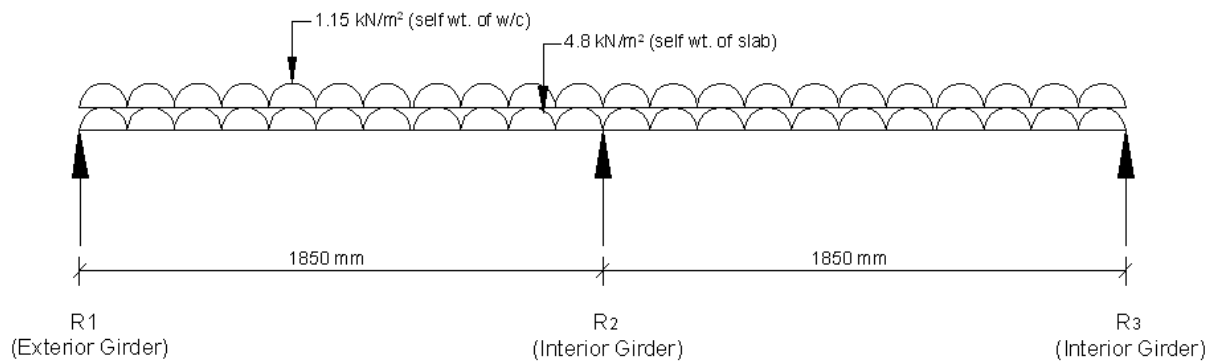


Fig 1.1.2 c/c Girder Spacing Loading Diagram

(Note: Deck overhang and its loading diagram is shown separately in Fig. 1.1.3)

Dead load:

$$\begin{aligned} \text{Self wt. of deck slab} &= 24 \times 0.2 = 4.8 \text{ kN/m}^2. \\ \text{Self wt. of wearing course} &= 23 \times 0.05 = 1.15 \text{ kN/m}^2. \end{aligned}$$

+ve Moment due to dead load

$$+ve \text{ MDLIS1 (due to deck slab)} = 4.8 \times 1.85^2 / 8 = 2.053 \text{ kN-m/m.}$$

$$+ve \text{ MDLIS2 (due to WC)} = 1.15 \times 1.85^2 / 8 = 0.492 \text{ kN-m/m.}$$

Live load:

Vehicular live loading on roadways of bridge deck is designed by vehicle type HL-93, truck loading where, wheel load, $P = 72.5 \text{ kN}$, plus lane loading 9.30 kN/m of lane width. Lane width is considered 3.00 m .

To get the load per unit width of equivalent strip, total load on one design traffic lane is divided by calculated strip width.

$$\text{Distribution width (for +ve moment)} = 660 + 0.55 S \quad (\text{Ref. AASHTO 07, Art.4.6.2.1})$$

$$\text{Strip width (for -ve moment)} = 1220 + 0.25 S \quad (\text{Ref. AASHTO 07, Art.4.6.2.1})$$

Here, $S = \text{c/c spacing of girder} = 1850 \text{ mm} = 1.85 \text{ m}$.

$$\begin{aligned} \text{Distribution width (for +ve moment)} &= 660 + 0.55 \times 1850 &&= 1678 \text{ mm} \\ &&&= 1.678 \text{ m.} \end{aligned}$$

$$\text{Strip width (for -ve moment)} = 1220 + 0.25 \times 1850 = 1683 \text{ mm} = 1.683 \text{ m}$$

$$\begin{aligned} \text{Dynamic load allowance, IM} &= 33\% \\ &= 0.33 \quad (\text{Ref. AASHTO 07, Art.4.6.2.1}) \end{aligned}$$

+ve moment due to live load at interior span:

$$\begin{aligned} \text{MLLIS} &= \{(P_{\text{wheel}} / B_{\text{strip}}) \times S/8\} + \{(9.3/3.0) \times (S^2/8)\} \\ &\quad (\text{Ref. AASHTO 07, Art.4.6.2.1}) \\ &= \{(72.5/1.678) \times (1.85/8)\} + \{(9.3/3.0) \times (1.85^2/8)\} \\ &= 11.32 \text{ kN-m/m.} \end{aligned}$$

Total factored moment for interior span (Strength-i):

$$\begin{aligned} \text{MPOS} &= 1.25 \times \text{MDLIS1} + 1.5 \times \text{MDLIS2} + 1.75 \times \text{MDLIS} (1 + \text{IM}) \\ &= 1.25 \times 2.053 + 1.5 \times 0.492 + 1.75 \times 11.32 (1+0.33) \\ &= 29.65 \text{ kN-m/m.} \end{aligned}$$

Diagram illustrating the structural components and loads for a single rail post and beam assembly:

- Self weight of rail post with rail beam:** 2.74 kN/m
- Height of rail post:** 1105 mm
- Line Load (PLL):** $PLL = 0.89 + 0.73L$
- Loads on the beam:**
 - 3.6 kN/m² (Pedestrian live load)
 - 14.6 kN/m (Line load)
 - 1.15 kN/m² (Self wt. of w/c)
 - 4.8 kN/m² (Self wt. of slab)
- Dimensions:**
 - 875 mm (Total length of beam segment)
 - 300 mm (Offset from post to start of beam segment)
 - 625 mm (Length of beam segment from offset to support R1)
 - 1025 mm (Total length of beam segment from post to support R1)
 - 1125 mm (Total length of beam segment from post to support R2)
 - 1850 mm (Length of beam segment from support R1 to support R2)
- Supports:** R1 and R2

Note: 875 mm = Side walk Width
625 mm = Distributed Overhang Line Load Width
1025 mm = Distance between CL of Rail Post and edge of Girder
1355 mm = Distance between edge of Girder and edge of Sidewalk

Live load:

1. For deck overhang < 1800 mm.
Line load = 14.6 kN/m, located at 300 mm from the face of railing.
(Ref. AASHTO 07, Art.3.6.1.3.4)
2. Concentrated design horizontal live load on each post,
$$P_{LL} = 0.89 + 0.73L$$

(Ref. AASHTO 07, Art.13.8.2)
Here, L = Post spacing = 1580 mm = 1.58 m.

$$P_{LL} = 0.89 + 0.73 \times 1.58 = 2.04 \text{ kN/m.}$$

$$3. \text{ Bridge pedestrian load} = 3.6 \times 10^{-3} \text{ N/m}^2 = 3.6 \text{ kN/m}^2$$

(Ref. AASHTO 07, Art.13.8.2)

-ve moment due to dead load at overhang part:

Here,

Rail post height = 1105 mm.

Slab thickness = 200 mm.

Curb height = 300 mm.

Center of girder to top of rail post height = 1105 + 200 + 300

= 1605 mm.

= 1.605 m.

Distance of distributed line load on overhang = 625 mm = 0.625 m.

Side walk width = 875 mm = 0.875 m.

$$\begin{aligned} \text{-ve MLL overhang} &= (14.6 \times 0.625^2)/2 + 3.6 \times 0.875 \times (1.125 - 0.2)/2 \\ &\quad + 2.04 \times 1.61 \\ &= 7.59 \text{ kN-m/m.} \end{aligned}$$

Total factored moment for deck overhang (Strength-I):

$$\begin{aligned} \text{MNEG} &= 1.25 \times (\text{-ve MDL overhang1}) + 1.5 \times (\text{-ve MDL overhang2}) \\ &\quad + (\text{-ve MLL overhang}) \\ &= 1.25 \times 5.85 + 1.5 \times 0.728 + 1.75 \times 7.59 \\ &= 21.69 \text{ kN-m/m.} \end{aligned}$$

Design moment: +ve MDES = MPOS = 29.65 kN-m/m.
 -ve MDES = MNEG = 21.69 kN-m/m.

1.1.4 Provision of reinforcement:

1.1.4.1 +ve reinforcement:

Here,

Slab thickness = 200 mm.

Clear cover = 50 mm.

Distance of reinforcement = $1.5 \times 12 = 18 \text{ mm}$.

It is proposed to use T12-150 as +ve reinforcement for interior span.

Here,

Area of reinforcement = 113 mm^2 .

$$A_s = 113 \times 1000 / 150 = 753.3 \text{ mm}^2.$$

$$\begin{aligned} \text{Lever arm factor, } a &= (A_s f_y) / (0.85 f_c' b) \\ &= (753.3 \times 400) / (0.85 \times 25 \times 1000) \\ &= 14.18 \text{ mm} = 0.1418 \text{ m} \end{aligned}$$

$$\text{Effective depth, } d = 200 - 50 - 18 = 132 \text{ mm} = 0.132 \text{ m}.$$

$$\begin{aligned} \text{Moment capacity, } \phi M_n &= 0.9 A_s f_y (d - a/2) \\ &= 0.9 \times 753.3 \times 400 \times \{132 - (14.18/2)\} \times 10^{-6} \\ &= 33.88 \text{ kN-m/m.} \end{aligned}$$

$$\text{Ultimate +ve MDES, } 29.65 \text{ kN-m/m.} < \phi M_n, 33.88 \text{ kN-m/m.}$$

OK

1.1.4.2 -ve reinforcement:

Here,

$$\text{-ve MDES} = \text{MNEG} = 21.69 \text{ kN-m/m.}$$

$$\text{Ultimate -ve MDES, } 21.69 \text{ kN-m/m.} < \phi M_n, 33.88 \text{ kN-m/m.}$$

OK

So, to obtain above strength T12-150 is provided as -ve reinforcement.

1.1.4.3 Cracking moment:

For flexural member, AASHTO 07 requires that $\phi M_n > M_F$

$$\text{Modulus of rupture of concrete, } f_r = 0.52 \sqrt{f_c'} = 0.52 \times \sqrt{25} = 2.6 \text{ MPa.}$$

(Ref. AASHTO 07, Art.5.4.2.6)

$$\text{Moment of inertia, } I_g = bh^3/12 = 1 \times 0.2^3/12 = 0.0007 \text{ mm}^4.$$

Here,

$$\text{Distance from neutral axis to extreme tension fiber, } y_t = 100 \text{ mm}$$

$$\begin{aligned} \text{Cracking moment, } M_{cr} &= f_r I_g / y_t \quad (\text{Ref. AASHTO 07, Art.5.7.3.6.2}) \\ &= (2.6 \times 0.0007 \times 10^6) / 100 \\ &= 18.2 \text{ kN-m} \end{aligned}$$

$$\text{Minimum flexural strength, } M_F = 1.2 M_{cr} = 1.2 \times 18.2 = 21.84 \text{ kN-m.}$$

$$\text{So, } \phi M_n > M_F$$

OK

1.1.4.4 Temperature & shrinkage reinforcement:

Here, minimum reinforcement required is

$$\begin{aligned} A_{st} &= 0.003bh \\ &= 0.003 \times 1000 \times 200/2 = 300 \text{ mm}^2. \quad (\text{Ref. AASHTO 07, Art.5.6.3.6}) \end{aligned}$$

Assured Reinf. is T12-200

$$= 0.003 \times 1000 \times 200/2 = 300 \text{ mm}^2.$$

$$A_{s\text{prov}} = 113 \times 1000/200 = 565 \text{ mm}^2 > A_{st} = 300 \text{ mm}^2$$

T12-200 provided as temperature & shrinkage reinforcement on the top layer is OK

1.1.4.5 Distribution reinforcement:

The distribution reinforcement parallel to the traffic is required,

$$A_{sd} = 3840/\sqrt{S} \leq 67\%$$

(Ref. AASHTO 2007, Art.9.7.3.2)

Effective span of deck slab, $S = 1850 - 460 = 1390 \text{ mm} = 1.39 \text{ m}$.

So, required distribution reinf. $A_{sd} = 504.73 \text{ mm}^2$

$$A_{sd} = 3840/\sqrt{1390} = 103 \text{ mm}^2; \text{ or}$$

67% of $A_s = 0.67 \times 753.3 = 504.73 \text{ mm}^2$ whichever is greater .

So,

$$A_{sd} \leq 67\% \text{ of } A_s.$$

Using T12 bar required spacing = $(113 \times 1000)/504.73$

$$= 223.88 \text{ mm}.$$

So, T12-200 is provided as distribution reinforcement on the bottom layer. OK

1.2 STRUCTURAL DESIGN OF RC GIRDER

1.2.1 Introduction

The design example demonstrates the design of a 25.0 m (c/c brg) span reinforced concrete (RC) girder. The deck cross section is the same as shown in Fig. 1.1. This comprises 200mm thick RC deck slab, 50 mm wearing course and cast in situ railing is considered. This example illustrates in detail the design of typical interior and exterior girders. The design is accomplished in accordance with the AASHTO LRFD Bridge Design Specification 07.

Vehicular live loading on the road ways of bridges or incidental structures, designated HL-93, and shall consist of combination of the:

- Design truck similar to HS20-44 of the previous AASHTO Bridge Standards or design tandem of 110000N axles spaced 1200mm apart in addition with
(Ref. AASHTO- 07, Article 3.6.1.2.1)
- Design lane load consist of 9.3 N/mm uniformly distributed in longitudinal direction
(Ref. AASHTO-2007, Article 3.6.1.2.1)

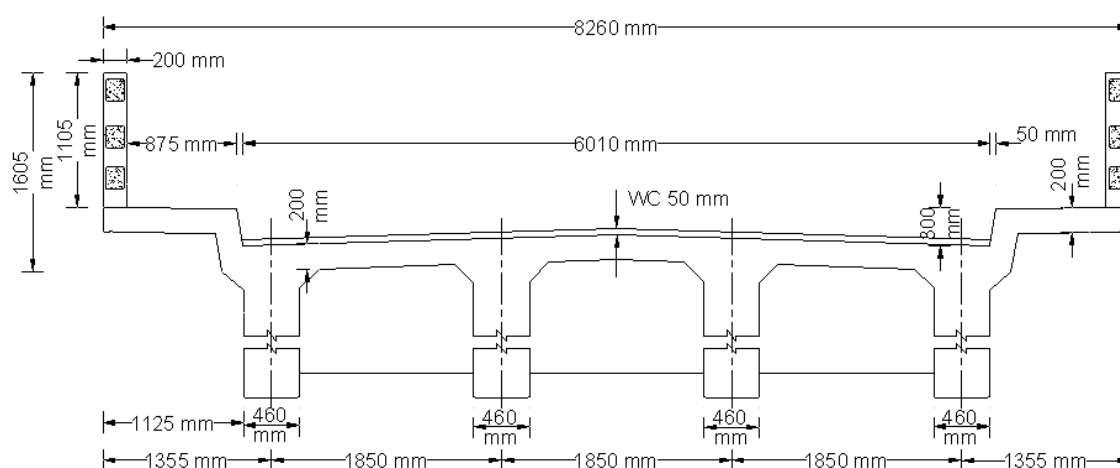


Fig 1.2.1 Cross Section of deck slab (Reproduce of Fig 1.1.1)

1.2.2 Geometrical data

Span length	: 25.0 m
Thickness	: 0.2 m
Wearing course, WC	: .05 m
Rail Post height	: 1.1 m
Rail Post Width	: 0.2 m
C/C Rail	
Rail Post spacing	: 1.58 m
Rail beam x-section	: 0.185 m x 0.15 m
Side walk height	: 0.2 m
Side walk width	: 0.875 m
Curb height	: 0.3 m
Girder height	: 1.8 m

Girder Width	:	0.46 m
C/C Girder Spacing	:	1.85 m
X-girder height	:	1.3 m
X-girder Width	:	0.375 m

1.2.3 Material Specifications:

Concrete strength, f_c	= 25 MPa
Yield Strength of Reinforcing steel, f_y	= 400 MPa
Unit wt of concrete	= 24 kN/m ³
Unit wt of wearing course	= 23 kN/m ³

1.2.4 Calculation of Centroid & Moment of Inertia of Girder about X-X axis

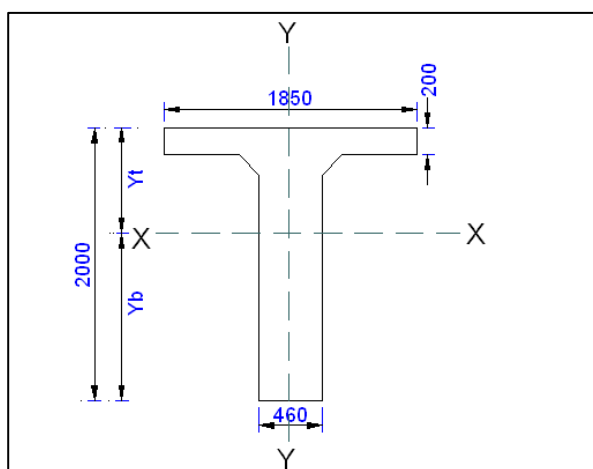


Fig 1.2.2 Centroid about X-X axis

Table: Showing Section Properties of Girder

Component	b	d	A	y	Ay	$y_b NA$	I	ybar	$A(ybar)^2$
	mm	mm	mm ²	mm	mm ³	mm	mm ⁴	mm	mm ⁴
1	1850	200	3.70E+05	1900	7.03E+08	1228.43	1.23E+09	681.18	1.72E+11
2	460	1800	8.28E+05	900	7.45E+08		2.24E+11	318.82	8.42E+10
3	150	150	2.25E+04	1750	3.94E+07		2.81E+07	531.18	6.35E+09
$\Sigma A =$			1.243E+06	$\Sigma Ay =$	1.526E+09	$\Sigma I =$	2.25E+11	$\Sigma A(ybar)^2 =$	2.62E+11

y_b = distance from centroid to the extreme bottom fiber of girder.

$$y_b = \Sigma Ay / \Sigma A = 1228.43 \text{ mm}$$

$$y_t = \text{distance from centroid to extreme top fiber of girder} = 771.57 \text{ mm}$$

$$I = \text{moment of inertia of composite section} = \Sigma I + \Sigma A(ybar)^2 = 4.86 \times 10^{11} \text{ mm}^4$$

$$S_b = \text{section modulus for the extreme bottom fiber} = I / y_b = 3.97 \times 10^8 \text{ mm}^4$$

$$S_t = \text{section modulus for the extreme top fiber} = I / y_t = 6.29 \times 10^8 \text{ mm}^4$$

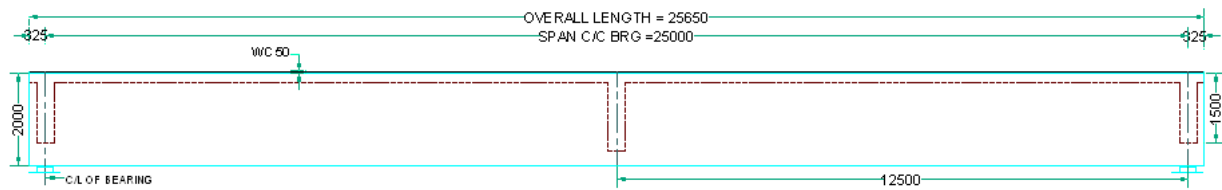


Fig. 1.2.3: Long section of girder

1.2.5 Live load distribution factor for typical interior beam:

Live load bending moment and shear force are determined by using the simplified distribution factor formulas (AASHTO 07, Art-4.6.2.2). To use the simplified live load distribution factor formula the following conditions apply:

- Width of slab is constant **OK**
- Number of girder, $N_b \geq 4$ ($N_b = 4$) **OK**
- Beams are parallel and of same stiffness **OK**
- Road way part of overhang, $d_e \leq 910$ mm ($d_e = 0$) **OK**
- Curvature is less than 4° (Ref. AASHTO 07 table 4.6.1.2.1-1) **OK**
(curvature = 0°)

Number of design lanes = 2

1.2.5.1 Distribution factor for bending moment

For two or more design lane loaded,

For interior beam

$$\text{DFM} = 0.075 + (S/2900)^{0.6} (S/L)^{0.2} (K_g/Lt_s^3)^{0.1}$$

where,

DFM = Distribution factor for interior beam

$$1100 \leq S \leq 4900$$

S = Beam/girder spacing, mm = 1850mm

$$110 \leq t_s \leq 300$$

t_s = Thickness of deck, mm = 200mm

$$6000 \leq L \leq 73000$$

L = Length of girder, mm = 25650mm

$$N_b \geq 4$$

$K_g = n(I + Ae_g^2)$ = longitudinal stiffness parameter

$$4 \times 10^9 \leq K_g \leq 3 \times 10^{12}$$

in which $n = E_b / E_d = 1/1 = 1$, So, $n = 1$

e_g = Distance between the cg of beam and cg of deck
= 1000mm

Here, concrete strength for both beams and deck are $f'_c = 25$ MPa

Here, cylinder strength of beam = cylinder strength of deck = 25 MPa

A = Cross-sectional area of girder, $\text{mm}^2 = 460 \times 1800 = 828000 \text{ mm}^2$

I = Moment of inertia of beam, $\text{mm}^4 = 2.24 \times 10^{11} = \text{mm}^4 = 2.24 \times 10^{11} = \text{mm}^4$

Thus,

$$\begin{aligned} K_g &= n(1 + ae_g^2) &= & 1 (2.24 \times 10^{11} + 828000 \times 1000^2) \\ & &= & 1.05 \times 10^{12} \text{ mm}^4 \end{aligned}$$

Therefore,

$$\begin{aligned} \text{DFM} &= 0.075 + (1850/2900)^{0.6} (1850/25650)^{0.2} (1.05 \times 10^{12} / 25650 \times 200^3)^{0.1} \\ &= 0.60 \text{ per/girder} \end{aligned}$$

1.2.5.2 Distribution factor for shear force

For two or more lane loaded,

$$\text{DFV} = 0.2 + s/3600 - (s/10700)^{2.0}$$

Provided that, $1100 \leq S \leq 4900$ where $S = 1850 \text{ mm}$

$6000 \leq L \leq 73000$ where $L = 25650 \text{ mm}$

$110 \leq t_s \leq 300$ where $t_s = 200 \text{ mm}$

$N_b \geq 4$ where $N_b = 4$

OK.

In which,

DFV = Distribution factor for shear for interior beam

This gives,

$$\begin{aligned} \text{DFV} &= 0.2 + (1850/3600) - (1850/10700)^{2.0} \\ &= 0.2 + 0.5138 - 0.029 \\ &= 0.68 \text{ per / girder (AASHTO 07 Table 4.6.2.2.3a-1)} \end{aligned}$$

1.2.5.3 Dynamic Allowance

IM = 33% (Ref. AASHTO 07 Table 3.6.2.1-1)

Where, IM = dynamic load allowance applied to truck load only.

1.2.6 Live load distribution factor for typical exterior beam

1.2.6.1 Distribution factor for bending moment

For exterior girder,

$$\text{DFM} = e \times g_{\text{girder}}$$

Where, $-300 \leq d_e \leq 1700$

$$e = 0.77 + d_e/2800$$

in which,

e = correction factor (AASHTO 07 Table 4.6.2.2.2d)

g = distribution factor

d_e = distance from the exterior web of exterior girder to the interior edge of curb as traffic barrier(mm)

= 50 mm

This gives,

$$e = 0.77 + 50/2800 = 0.77$$

& $\text{DFM} = e \times g_{\text{interior}}$

$$= 0.787 \times 0.6$$

$$= 0.473 \text{ per/girder}$$

1.2.6.2 Distribution factor for shear force

For exterior girder

DFV,

$$\text{DFV} = e \times g_{\text{interior}} \quad (\text{Ref. AASHTO 07 Table 4.6.2.2.3b-1})$$

$$e = 0.60 + de/3000$$

$$\text{Here, } e = 0.60 + 50/3000 = 0.62$$

This gives

$$\text{DFV}_{\text{interior}} = 0.68 \text{ per/girder (previous calculation)}$$

$$\text{DFV}_{\text{exterior}} = 0.62 \times 0.68 = 0.42 \text{ girder}$$

1.2.7 Simplified conventional method for live load distribution factor

1.2.7.1 For Interior Girder

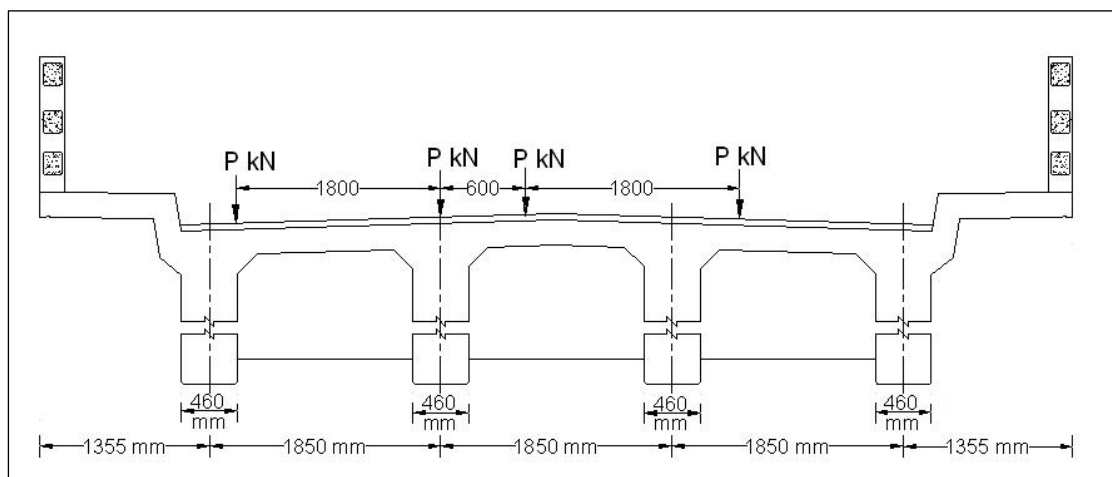


Fig 1.2.3 Truck Load Distribution (interior girder)

$$\text{Load per girder} = P + (1850 - 1800)/1850 \times P + (1850 - 600)/1850 \times P$$

$$= 1.7 \times P \quad \text{here, } P = \text{wheel load}$$

1.2.7.2 For Exterior Girder

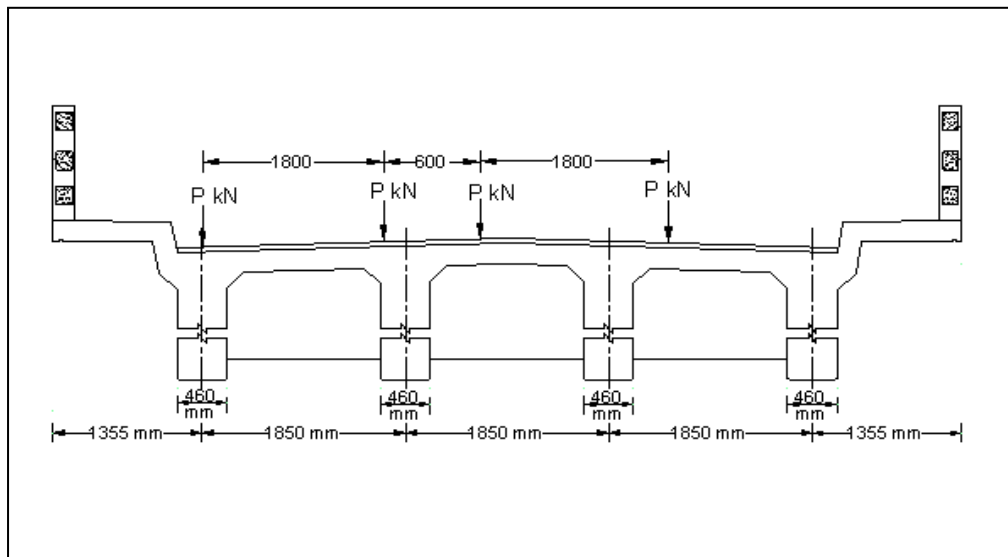


Fig 1.2.4 Truck Load Distribution (exterior girder)

$$\begin{aligned}\text{Load per girder} &= P + (1850-1800)/1850 \times P \\ &= 1.03 \times P \quad \text{here, } P = \text{wheel load, kN}\end{aligned}$$

1.2.8 Service shear force and bending moment:

The self weight of girder, X- girder, deck slab, wearing course and live loads with wheel loads, lane load and impact load are considered. For exterior girder design calculation, self weight of rail post, rail bar, sidewalk are considered, in addition to previously considered dead loads. For live load calculation, pedestrian live load is considered along with wheel load and lane load.

1.2.8.1 Interior girder

1.2.8.1.1 Calculation of Weight

$$\begin{aligned}\text{Self wt of girder} &= 0.46 \times 1.8 \times 24 = 19.87 \text{ kN/m} \\ \text{X- girder} &= 0.375 \times 1.3 \times 1.85 \times 24 = 21.65 \text{ kN} \\ \text{Deck slab} &= 0.20 \times 1.85 \times 24 = 8.88 \text{ kN/lm} \\ \text{Wearing course} &= 0.05 \times 1.85 \times 23 = 2.13 \text{ kN/lm}\end{aligned}$$

1.2.8.1.2 Bending Moment due to Dead Load

$$\begin{aligned}\text{Moment due to dead load at mid point,} \\ \text{Girder} &= 19.87 \times 25^2 / 8 = 1552.5 \text{ kN-m} \\ \text{Deck slab} &= 8.80 \times 25^2 / 8 = 687.5 \text{ kN-m} \\ \text{Wearing course} &= 2.13 \times 25^2 / 8 = 166.5 \text{ kN-m} \\ \text{Support reaction of X- girder}\end{aligned}$$

$$\sum F_y = 0$$

$$\begin{aligned} \blacktriangleright 21.65 \times 12.5 + 21.65 \times 25 - R \times 25 &= 0 \\ \blacktriangleright R &= 32.5 \text{ kN} \end{aligned}$$

$$\text{X- girder moment} = 32.5 \times 12.5 - 21.6 \times 12.5 = 135.5 \text{ kN-m}$$

Dead load moment due to self weight, x-girder and deck slab

$$\begin{aligned} M_1 &= (1552.5 + 135.5 + 687.5) \\ &= 2375.5 \text{ kN-m} \end{aligned}$$

Dead load moment due to wearing course

$$M_2 = 166.5 \text{ kN-m}$$

1.2.8.1.3 Shear Force due to Dead Load

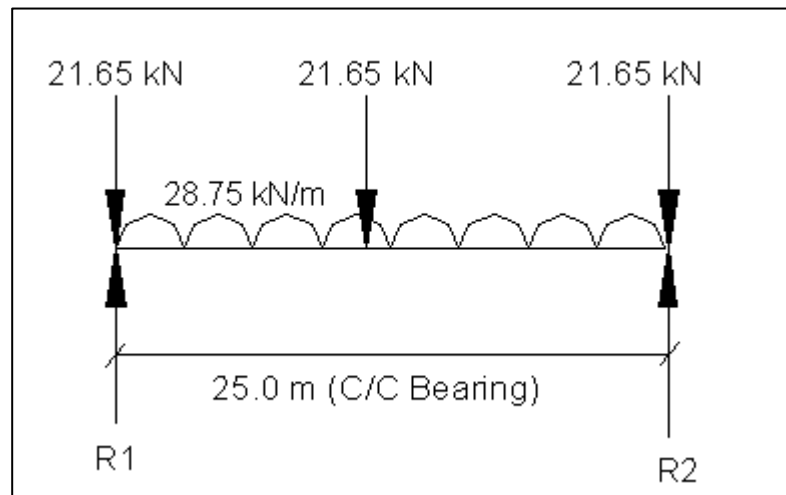


Fig 1.2.5 Load Diagram of Interior Girder (Dead load)

$$R_1 = \{ (21.65 \times 25) + (21.65 \times 12.5) + (28.75 \times 25 \times 12.5) \} / 25 = 391.85 \text{ kN}$$

NOTE: For this calculation self wt of deck slab, self wt of girder has been considered as uniform load = 28.75 kN/m and self wt of cross girder have been considered as concentrated Load of 21.65kN. (Previous Calculation)

Maximum shear at support

$$\begin{aligned} &= (391.85 - 21.65) \\ &= 370.20 \text{ kN} \end{aligned}$$

$$\text{Shear force due to wearing course} = (2.13 \times 25) / 2 = 26.63 \text{ kN}$$

1.2.8.1.4 Bending Moment Due to Truck Load

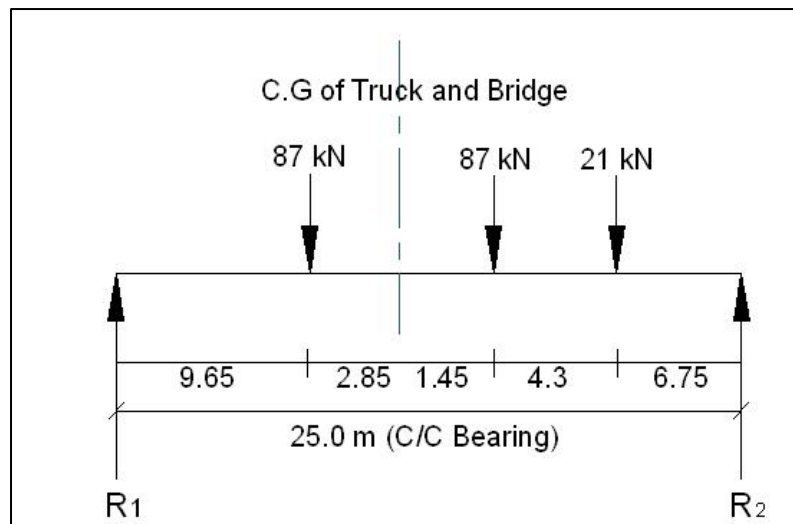


Fig 1.2.6 Loading Diagram of Interior Girder with truck load only

For obtaining maximum moment as single span bridge the C.G of truck is placed at the centre of the bridge.

(AASHTO 2007, Table 3.6.2.1-1)

$$P_1 = \text{Rear end wheel load of truck} = (72.5 \times 2 \times \text{DFM}) = 87 \text{ kN}$$

$$P_2 = \text{Middle wheel load of truck} = (72.5 \times 2 \times \text{DFM}) = 87 \text{ kN}$$

$$P_3 = \text{Front wheel load of truck} = 17.2 \times 2 \times \text{DFM} = 21 \text{ kN}$$

$$W = \text{lane load} = 9.3 \times \text{DFM} \quad (\text{Ref. AASHTO 07 Article No 3.6.1.2.4}) \\ = 5.58 \text{ kN/m}$$

$$R_1 = 21 \times 6750 + 87 \times (4300 + 67500) + 87 \times (4300 + 4300 + 6750) / 25000 = 97.55 \text{ kN}$$

Maximum moment at mid span due to truck load,

$$(97.55 \times 125000) - (87 \times 2850) = 971425 \text{ kN-mm} = 972 \text{ kN-m}$$

$$\begin{aligned} \text{Total truck load moment with impact moment} &= 972(1 + \text{IM}) \\ &= 972(1 + 0.33) \\ &= 1292.76 \text{ kN-m} \end{aligned}$$

1.2.8.1.5 Bending Moment Due to Lane Load

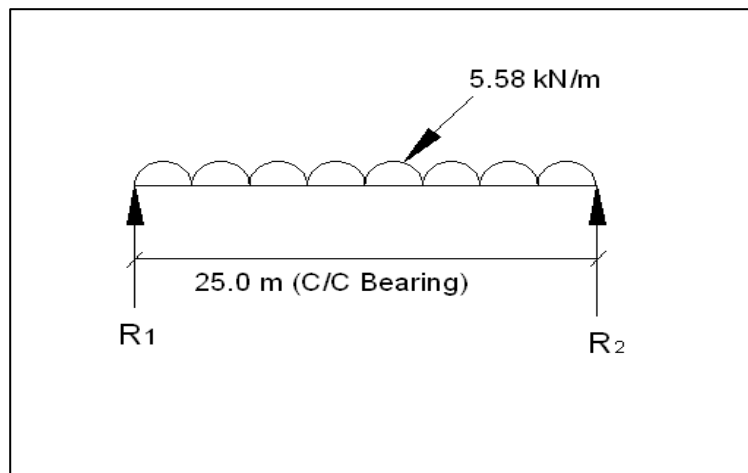


Fig 1.2.7 Loading Diagram of Interior Girder with Lane Load

Maximum moment due to lane load at mid span,

$$= 5.58 \times (25)^2 / 8 = 435.93 \text{ kN-m}$$

1.2.8.1.6 Shear Force due to Truck Load

$$P_1 = DFV \times 2P = 0.68 \times 2 \times 72.5 = 98.6 \text{ kN}, P = 72.5 \text{ kN}$$

$$P_2 = DFV \times 2P = 0.68 \times 2 \times 72.5 = 98.6 \text{ kN}, P = 72.5 \text{ kN}$$

$$P_3 = DFV \times 2P = 0.68 \times 2 \times 17.5 = 23.8 \text{ kN}, P = 17.5 \text{ kN}$$

(NOTE: For maximum shear, rear wheel have been placed at support)

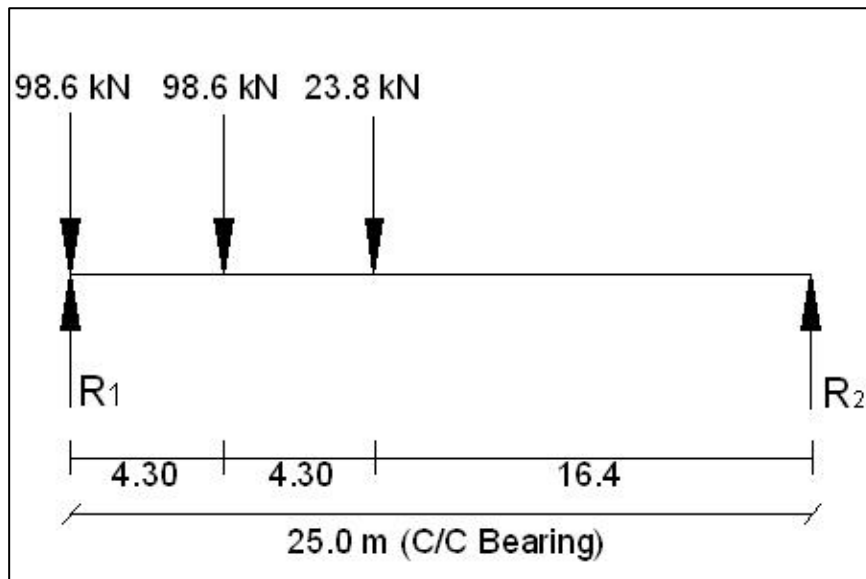


Fig 1.2.8 Loading Diagram of Truck Load for Shear Force Calculation

$$R_1 = \{23.8 \times 16.4 + 98.6 \times (4.3 + 16.4) + 98.6 \times (4.3 + 4.3 + 16.4)\} / 25$$

$$= 195.85 \text{ kN}$$

Maximum shear at support,

$$= 195.85 - 98.6 \text{ kN} = 97.3 \text{ kN}$$

Maximum shear with impact load,

$$\begin{aligned} &= 97.3(1 + \text{IM}) \\ &= 97.3(1 + .33) \\ &= 130 \text{ kN} \end{aligned}$$

1.2.8.1.7 Shear Force due to Lane Load

$$\text{Lane load} = \text{DFV} \times 9.3 = 6.32 \text{ kN/m}$$

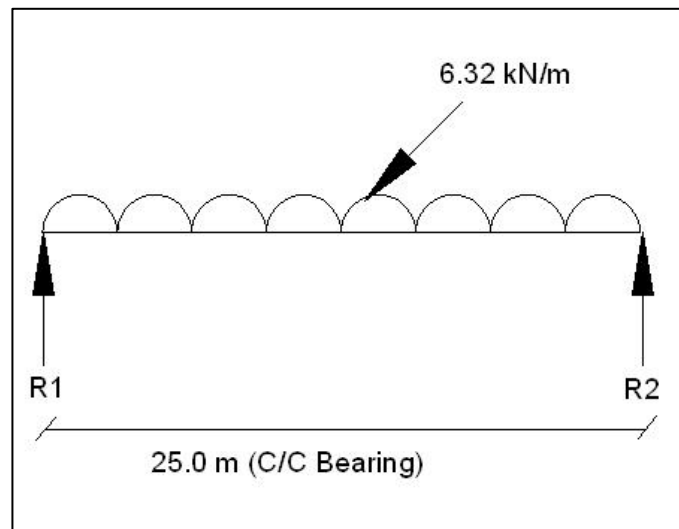


Fig 1.2.9 Loading Diagram of Lane Load for Shear Force Calculation

$$R_1 = (96.32 \times 25 \times 25/2)/25 = 79 \text{ kN}$$

Maximum shear at support = 79 kN

1.2.8.1.8 Bending Moment from Simplified Conventional Method for Truck Load

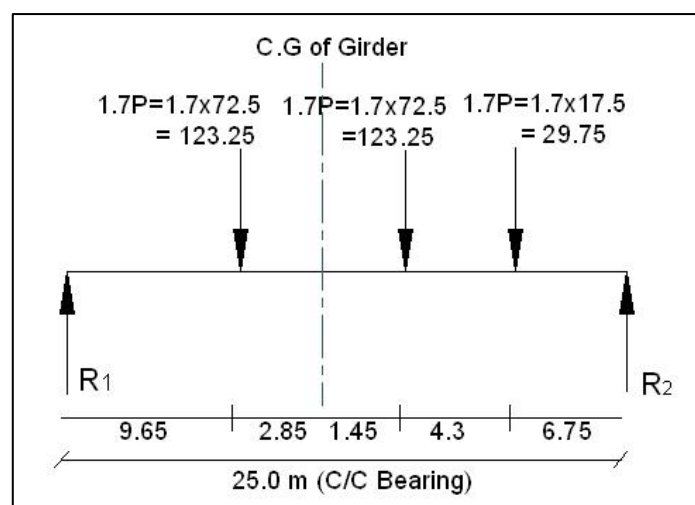


Fig 1.2.10 Truck Load Diagram for Bending Moment

$$R_1 = (29.75 \times 6.75) + 123.25 \times (4.3 + 6.75) + 123.25(2.85 + 1.45 + 4.3 + 6.75) \\ = 138.18 \text{ kN}$$

$$\text{Moment at mid span} = 1376.04 \text{ kN-m}$$

$$\text{Moment with impact factor} = 1376.04(1 + 0.33) = 1830.13 \text{ kN-m}$$

1.2.8.1.9 Bending Moment from Simplified Conventional Method for Lane Load

In this method lane load considered as

$$= 9.3 \times 1.85 / 3 = 5.73 \text{ kN/m}$$

here, c/c girder distance = 1.85 m

Total lane load moment at mid span

$$M = 5.73 \times 25^2 / 8 = 447.65 \text{ kN-m}$$

1.2.8.1.10 Summary of design moment and shear factored

For interior girder,

Total factored moment (AASHTO 07)

$$= (1.25 \times 2375.5) + (1.5 \times 166.5) + (1.75 \times 1292.76) + (1.75 \times 435.93) \\ = 6244.33 \text{ kN-m}$$

Total factored moment (Simplified Conventional Method)

$$= 1.25 \times 2375.55 + 1.5 \times 166.5 + 1.75 \times 830.13 + 1.75 \times 447.65 \\ = 7205.24 \text{ kN-m}$$

Total factored shear

$$= (1.25 \times \text{DL shear due to self weight of girder, x-girder \& deck}) + (1.5 \times \text{DL shear due to self weight of wearing course}) + (1.75 \times \text{LL shear from Truck Load and impact}) + (1.75 \times \text{LL shear from lane load}) \\ = (1.25 \times 370.2) + (1.5 \times 26.63) + (1.75 \times 130) + (1.75 \times 79) \\ = 868.45 \text{ kN}$$

Since total moment calculated for simplified distribution method from AASHTO 07 is less than that of simplified conventional method, design moment is chosen for reinforcement calculation from simplified conventional method, given below:

$$\text{Design Flexural Moment} = 7205.24 \text{ kN-m}$$

For calculation of reinforcement, refer to 1.2.8.1.11 below.

1.2.8.1.11 Crack Width Calculation

Bar stacing for maximum crack width of 0.22mm as per AASHTO '07, Art. 5.7.3.4-1

In which,

$$S \leq (123000 \gamma_e / \beta_s f_{ss}) - 2d_c$$

$$\gamma_e = 0.5$$

$$d_c = \text{clear cover} + \text{bar dia}$$

(we use T10 for shear reinforcement)

$$= 50 + 5 = 55$$

$$\beta_s = [\{ 1 + d_c \{ 0.7(h - d_c) \}] = [\{ 1 + 55 / \{ 0.7(2000 - 55) \}]$$

$$= 1.040$$

Service bending moment = 4270 kN-m

$$= 4270 \times 10^6 \text{ N-mm}$$

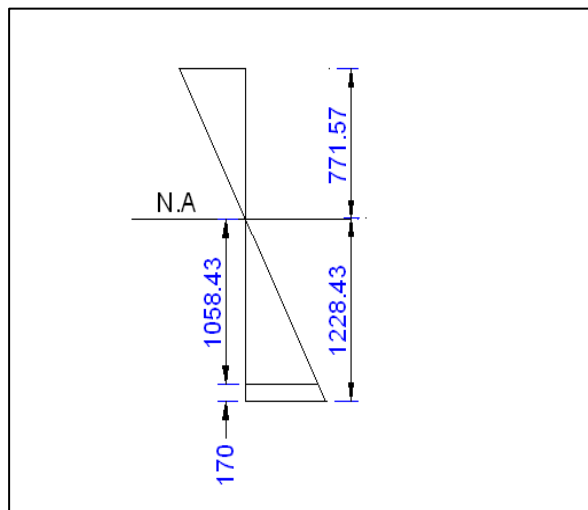


Fig 1.2.11 Stress Diagram of Interior Girder

$$f_b = M C_b / I = (4270 \times 10^6 \times 1228.43) / 4.86 \times 10^{11}$$

$$= 10.79 \text{ N/mm}^2$$

$$f_{sc} = 9.29 \text{ N/mm}^2 \quad [10.79 / 1228.43 = f_{sc} / 1058.43, f_{sc} = 10.79 / 1228.43 \times 1058.43]$$

$$f_{ss} = 9.2 \times 8.33$$

$$= 77.38 \text{ MPa}$$

$$f_{ss} = (E_s / E_c) \times f_{sc}$$

$$E_c = 24 \times 10^3 \text{ MPa}$$

$$E_s = 200 \times 10^3 \text{ MPa}$$

$$E_s / E_c = 8.33$$

$$S \leq (123 \times 10^3 \times 0.5 / 77.38 \times 1.040) - 2 \times 55$$

$$\leq 654.15 \text{ mm}$$

BS Method:

$$f_t = (4270 \times 10^6 \times 771.57) / 4.86 \times 10^{11}$$

$$= 6.77 \text{ N/mm}^2$$

$$\text{Concrete strain} = 6.77 / 24 \times 10^3 = .0003$$

$$\begin{aligned}\text{Crack width} &= 3 \epsilon_{\min} \times a_{cr} = 3 \times 0.0003 \times 107.35 \quad [a_{cr} = \sqrt{(100^2 + 55^2)} = 107.35] \\ &= 0.090 < 0.2\end{aligned}$$

Maximum crack width 0.22 mm.

1.2.8.1.12 Deflection for 25.0m Girder (due to live load):

Deflection due to beam self wt,

$$\begin{aligned}\Delta_g &= 5wL^4 / (384EI) \\ w &= \text{beam self wt.} = 19.87 \text{ kN/m} \\ \Delta_g &= (5 \times 19.87 \times (25.65)^4) / (384 \times 24 \times 10^6 \times 0.486) \\ &= 0.0096 \text{ m} = 9.6 \text{ mm } (\downarrow)\end{aligned}$$

Deflection due to slab wt,

$$\begin{aligned}\Delta_s &= 5wL^4 / (384EI) \\ w &= \text{slab wt.} = 8.88 \text{ kN/m} \\ \Delta_s &= (5 \times 8.88 \times (25.65)^4) / (384 \times 24 \times 10^6 \times 0.486) \\ &= 0.0043 \text{ m} = 4.3 \text{ mm } (\downarrow)\end{aligned}$$

Deflection due to X-girder load,

$$\begin{aligned}\Delta_{X\text{-girder}} &= PL^3 / (48EI) \\ P &= \text{X-girder load} = 21.65 \times 3 = 37.95 \text{ kN} \\ \Delta_{X\text{-girder}} &= (37.95 \times (25.65)^3 \times 1000) / (48 \times 24 \times 10^6 \times 0.486) \\ &= 1.15 \text{ mm } (\downarrow)\end{aligned}$$

Deflection due to wearing course,

$$\begin{aligned}\Delta_{wc} &= 5wL^4 / (384EI) \\ w &= \text{wearing course wt.} = 2.13 \text{ kN/m} \\ \Delta_{wc} &= (5 \times 2.13 \times (25.65)^4) / (384 \times 24 \times 10^6 \times 0.486) = 1 \text{ mm } (\downarrow)\end{aligned}$$

Deflection due to lane load,

$$\begin{aligned}\Delta_{LL} &= 5wL^4 / (384EI) \\ w &= \text{lane load} = 5.58 \text{ kN/m} \\ \Delta_{LL} &= (5 \times 5.58 \times (25.65)^4) / (384 \times 24 \times 10^6 \times 0.486) \\ &= 2.69 \text{ mm } (\downarrow)\end{aligned}$$

Deflection due to truck & impact load,

$$\begin{aligned}\Delta_{WL} &= PL^3 / (48EI) \\ P &= \text{wheel load} = (145 \times 2 + 35) \times \text{DFM} \times \text{Dynamic allowance} \\ &= 325 \times 0.6 \times 1.33 \\ &= 259.3 \text{ kN} \\ \Delta_{WL} &= (259.3 \times (25.65)^3 \times 1000) / (48 \times 24 \times 10^6 \times 0.486) \\ &= 7.8 \text{ mm } (\downarrow)\end{aligned}$$

Allowable deflection for live load = $L/800$ (Ref. AASHTO 07 Art. 2.5.2.6.2)
 = $(25.65) \times 100/800 = 32.06 \text{ mm}$
 Total live load deflection = $7.8+2.69 = 10.49 \text{ mm} < 32.06 \text{ mm}$

OK

1.2.8.1.13 Reinforcement calculation

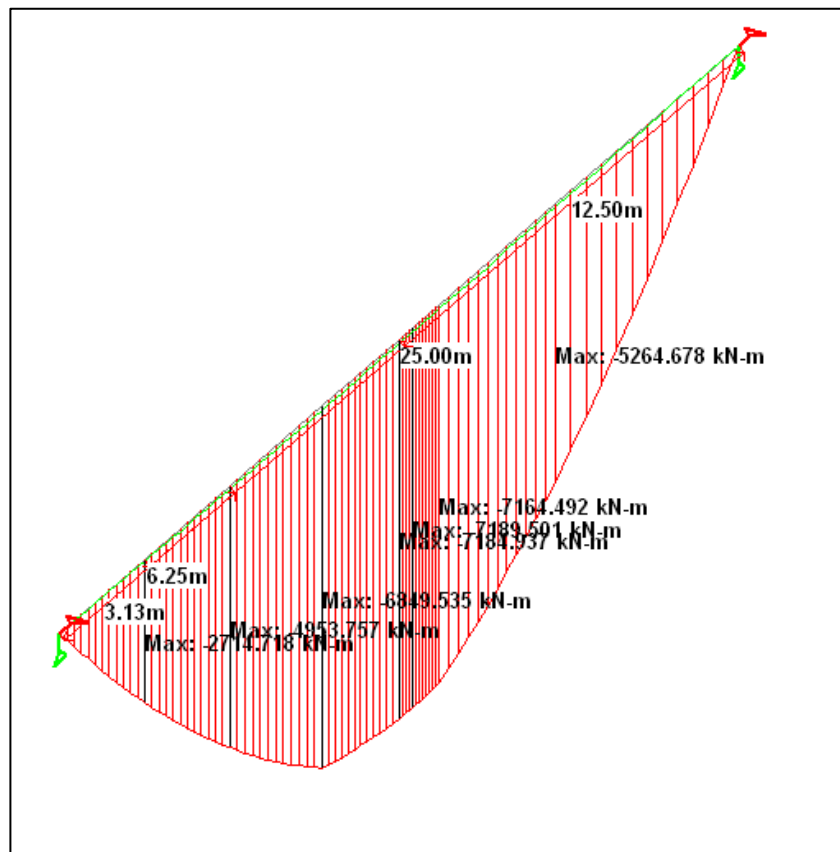


Fig 1.2.12 Moment Diagram of Interior Girder of 25.0m span
 (From STAAD.PRO analysis)

a) Flexural Moment

Total moment, $M_u = 7205.24 \text{ kN-m}$ (Simplified Conventional Method).

Using STAAD.Pro 2006, this analysis is again confirmed using live load distribution factor from simplified conventional method and thus design moment is chosen as 7200 kN-m.

Using, $20\text{-T}28 = 12300 \text{ mm}^2$

Effective depth of girder, $d = 1800 \text{ mm}$

Lever arm factor, $a = A_s f_y / 0.85 \times f'_c \times b$
 = $(12300 \times 400) / (0.85 \times 25 \times 1850)$
 = 128.27 mm

$$\begin{aligned}
 \text{Nominal moment, } \Phi M_n &= 0.9 \times A_s \times f_y (d - a/2) \\
 &= 0.9 \times 12300 \times 400 (1800 - 128.27/2) \\
 &= 7690 \text{ kN-m}
 \end{aligned}$$

As, $\Phi M_n > M_u$
Flexure design is OK

b) Cracking Moment

$$\text{Cracking moment, } M_{cr} = S_c (f_r + f_{cpe}) - M_{dnc} (S_c / S_{nc} - 1) \quad (\text{AASHTO 07 Art 5.7.3.3.2-1})$$

f_{cpe} = compressive stress in concrete due to effective prestress force only (after allowance for all prestress losses) at extreme fiber of section where tensile stress is caused by externally applied loads.

$$= 0 \text{ (for RC girder)}$$

$$S_c = S_{nc} = \text{section modulus of composite girder} = I_g / y_t \text{ (for RC girder)}$$

M_{dnc} = total service dead load moment acting on the monolithic or non-composite section (N-mm)

$$\text{So, } M_{cr} = S_c (f_r + f_{cpe}) - M_{dnc} (S_c / S_{nc} - 1)$$

$$= (f_r \times I_g) / y_t$$

Modules of rupture, f_r (for normal density concrete) = $0.52 \sqrt{f_c'}$

(Ref. AASHTO 07 Art 5.4.2.6)

$$\begin{aligned}
 &= 0.52 \sqrt{25} \\
 &= 2.6 \text{ MPa}
 \end{aligned}$$

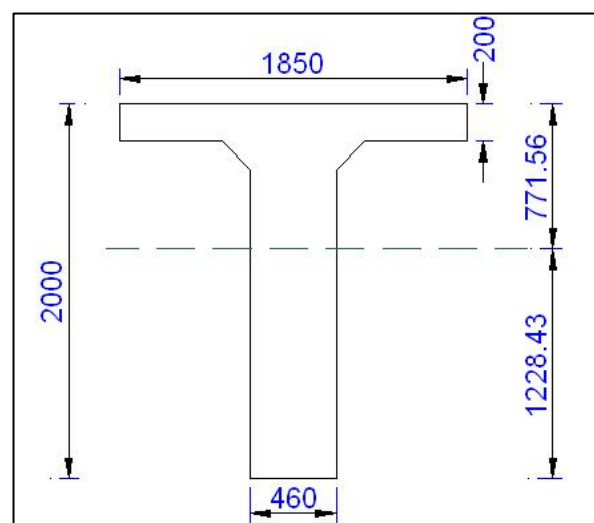


Fig 1.2.13 X-section of Girder

Distance from N.A to the top fiber of the section, $y_t = 771.56$

Moment of inertia, $I = 4.86 \times 10^{11} \text{ mm}^4$

Cracking moment, $M_{cr} = (2.6 \times 4.86 \times 10^{11}) / 771.2 = 1638.48 \text{ kN-m}$

$1.2 \times M_{cr} = 1.2 \times 1638.48 = 2383 \text{ kN-m}$

As $\Phi M_n > M_{cr}$ flexure design is OK

c) Surface Reinforcement

$$\begin{aligned} \text{Minimum reinforcement} &= 0.003bt \\ &= 0.003 \times 1000 \times 460 / 2 \\ &= 690 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Providing T-10,} \\ \text{Spacing} &= (1000 \times 78.5) / 690 \\ &= 113.76 \text{ mm} \\ &= 100 \text{ mm} \end{aligned}$$

Effective depth = 1800 mm

$$\begin{aligned} \text{Total no of surface reinforcement} &= 1800 / 100 \times 2 \\ &= 9 \end{aligned}$$

d) Shear Reinforcement

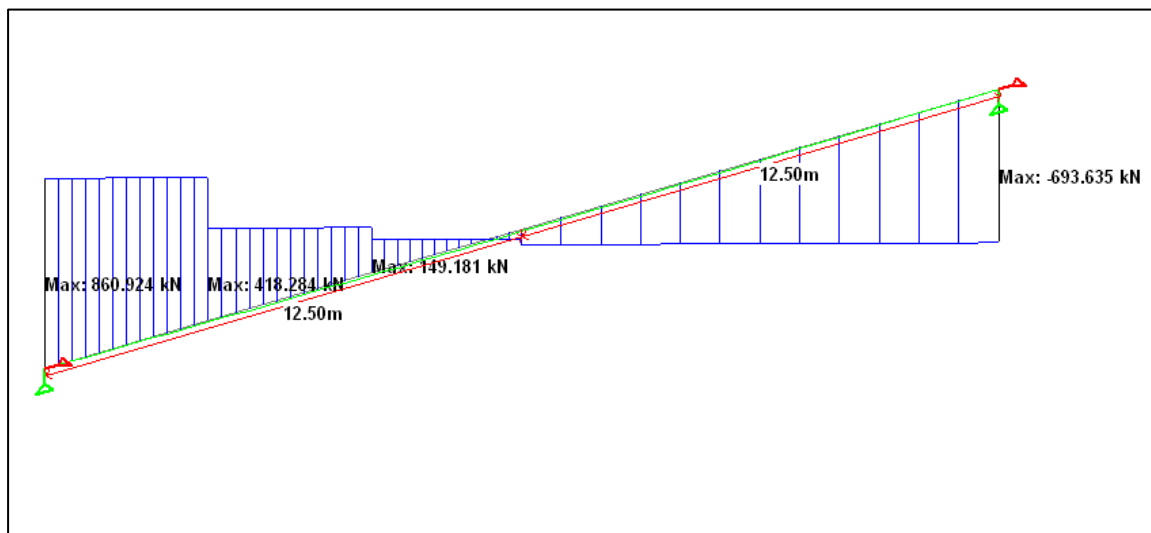


Fig 1.2.14 Shear Force Diagram for 25.0m Span (From STAAD.Pr0 Analysis)

i) Nominal shear resistance calculation

Nominal shear resistance, V_n shall be determined as lesser of

$$V_n = V_c + V_s + V_p \quad (\text{Ref. AASHTO 07 Art. 5.8.3.3-1})$$

$$V_n = 0.25 f'_c b_v d_v + V_p \quad (\text{Ref. AASHTO 07 Art. 5.8.3.3-2})$$

Here, $V_c = 0.083\beta\sqrt{f'_c} b_v d_v$ (Ref. AASHTO 07 Art. 5.8.3.3-3)

$$V_s = (A_v f_y d_v \cot \theta) / s$$

b_v = effective web width taken as the minimum web width within the depth d_v .

d_v = effective shear depth.

s = spacing of stirrups.

θ = angle of inclination of diagonal compressive stresses.

β = factor indicating ability of diagonally cracked concrete to transmit tension.

A_v = area of shear reinforcement within a distance "s"

V_p = component in the direction of the applied shear of the effective prestressing force.

For flexural members, the distance between the resultants of the tensile and compressive forces due to flexure can be determined as

$$\begin{aligned} d_v &= M_n / A_s f_y \quad (\text{AASHTO Art 5.8.2.9}) \\ &= A_s f_y (d - a/2) / A_s f_y \\ &= 1736 \text{ mm} \end{aligned}$$

d_v need not to be taken to be less than the greater of $0.9d_e$ or $0.72h$ (mm)

Here, $d = 1800 \text{ mm}$

$$\begin{aligned} a &= (A_s f_y) / (0.85 f'_c b) \\ &= 128.27 \text{ mm} \end{aligned}$$

Now, $0.72h = 0.72 \times 2000 = 1440 \text{ mm}$

$$0.9d_e = 1794 \times .9 = 1614.6 \text{ mm}$$

$d_v > \text{greater of } 0.72h \text{ and } 0.9 d_e$.

So, OK.

ii) Calculation of β & θ

θ = angle of inclination of diagonal compressive stresses.

β = factor indicating ability of diagonally cracked concrete to transmit tension.

$$\begin{aligned} v_u / f'_c &= 0.69/25 & \text{here, } v_u &= \text{total factored shear/area} \\ &= .028 & &= 868.45/1243 \times 10^3 \\ & & &= 6.9 \times 10^{-4} \text{ kN/mm}^2 \\ & & &= 0.69 \text{ N/mm}^2 \end{aligned}$$

from AASHTO Table-5.8.3.4.2-1

let $\epsilon_x = .001$

$\theta = 36.4$

$\beta = 2.23$

Hence,

$$\begin{aligned} V_c &= 0.083\beta\sqrt{f'_c} b_v d_v \\ &= 0.83 \times 2.23 \times \sqrt{25} \times 460 \times 1730 \\ &= 736.47 \text{ kN} \end{aligned}$$

Using, T12-150

V_s shall be determined by,

$$\begin{aligned} V_s &= A_v f_y d_v \cot \theta / s & (\text{Ref. AASHTO 07 Art 5.8.3.3-1}) \\ &= (2 \times 113 \times 400 \times 1736 \times 1.37) / 150 \\ &= 1428.38 \text{ kN} \end{aligned}$$

$$\begin{aligned} V_n &= V_c + V_s + V_p \\ &= 736.47 + 1428.38 + 0 = 2164.85 \text{ kN} \end{aligned}$$

$$\begin{aligned} V_n &= 0.25 f'_c b_v d_v + V_p \\ &= 0.25 \times 25 \times 460 \times 1736 + 0 \\ &= 4973.75 \text{ kN} \end{aligned}$$

Nominal Shear resistance, V_n shall be lesser than these two values.

$$\text{So, } V_n = 2164.85 \text{ kN}$$

Again, Using T10-150

$$\begin{aligned} V_s &= (A_v \times f_y \times d_v \cot \theta) / s = (2 \times 78.5 \times 400 \times 1736 \times 1.37) / 150 = 992.28 \text{ kN} \\ V_n &= V_c + V_s + V_p = 736.47 + 992.28 + 0 = 1728.75 \text{ kN} \\ V_n &= 0.25 \times f'_c \times b_v \times d_v + V_p = 4973.75 \text{ kN} \end{aligned}$$

Therefore,

$$V_n = 1728.75 \text{ kN}$$

$$V_u = 868.45 \text{ kN}$$

For the conservative design critical shear have been taken at support.

$$V_u < V_n \text{ so OK.}$$

So we provide T10-150 at a distance “d” from support and then provide T10-200 after distance “d”.

iii) Regions for requiring Transverse Reinforcement

$$\text{For beam, } V_u > 0.5\phi (V_c + V_p) \quad (\text{Ref. AASHTO 07, Art. 5.8.2.4-1})$$

$$V_u = 868.45 \text{ kN}$$

$$0.5 \times \phi \times V_c = 0.5 \times 0.9 \times 637 = 286.65 \text{ kN}$$

as $V_u > V_c$ so shear reinforcement is needed.

iv) Minimum Transverse Reinforcement

$$A_v \geq 0.083 \sqrt{f'_c} b_v s / f_y = 0.083 \sqrt{25} \times 460 \times 150 / 400 = 71.58 \text{ mm}^2 \quad (\text{Ref. AASHTO 07 Art. 5.8.2.5})$$

v) Maximum Spacing of Transverse Reinforcement:

The spacing of the transverse reinforcement shall not exceed the maximum permitted spacing s_{\max} determined as:

If $V_u < 0.125 \times f'_c$ then:

$$s_{\max} = 0.8d_v \leq 600 \text{ mm}$$

(Ref. AASHTO 07 Art. 5.8.2.7-1)

If $v_u \geq 0.125x f_c'$

then:

$$s_{\max} = 0.4 d_v \leq 300 \text{ mm} \quad (\text{AASHTO Art. 5.8.2.7-2})$$

$$v_u = V_u/A = 868 \times 10^3 / 1243 \times 10^3 = 0.69 \text{ N/mm}^2$$

$$v_u / f_c' = 0.69 / 25 = 0.027$$

Therefore,

$$s_{\max} = 0.8d_v \leq 600 \text{ mm}$$

$$= 0.8 \times 1736 \leq 600$$

$$= 1388 \leq 600$$

provided maximum spacing = 200 mm < 600 mm, so ok.

1.2.8.2 Exterior Girder

Bending moment and shear fore due to dead load

$$\text{Self wt of girder} = 0.46 \times 1.8 \times 24 = 19.87 \text{ kN/m}$$

$$\text{X – girder} = 0.375 \times 1.3 \times 24 \times 1.85 / 2 = 10.82 \text{ kN}$$

$$\text{Deck slab} = 0.2 \times 1.85 / 2 \times 24 = 4.44 \text{ kN/m}$$

$$\text{W/c} = 0.05 \times 1.85 / 2 \times 24 = 1.11 \text{ kN/m}$$

$$\text{Rail post} = (0.2 \times 0.2 \times 1.1 \times 24) / 1.58 = 0.67 \text{ kN/m}$$

$$\text{Rail beam} = 0.185 \times 0.15 \times 24 \times 3 = 2 \text{ kN/m}$$

$$\text{Side walk slab} = 1.125 \times 2 \times 24 = 5.4 \text{ kN/m}$$

1.2.8.2.1 Bending Moment due to Dead Load

$$\text{Moment due to girder} = 19.87 \times 25^2 / 8 = 1552.34 \text{ kN-m}$$

$$\text{Moment due to deck slab} = 4.4 \times 25^2 / 8 = 344 \text{ kN-m}$$

$$\text{Moment due to w/c} = 1.11 \times 25^2 / 8 = 86.72 \text{ kN-m}$$

$$\text{Moment due to rail post} = 0.67 \times 25^2 / 8 = 52.34 \text{ kN-m}$$

$$\text{Moment due to rail beam} = 2 \times 25^2 / 8 = 156.2 \text{ kN-m}$$

$$\text{Moment due to side walk} = 5.4 \times 25^2 / 8 = 421.87 \text{ kN-m}$$

$$\begin{aligned} \text{Moment due to cross girder,} \\ &= [\{(10.82 \times 12.5) + (10.82 \times 25)\} / 25] \times 12.5 \\ &\quad - (10.82 \times 12.5) \\ &= 67.62 \text{ kN-m} \end{aligned}$$

Dead load moment due to girder, deck, rail post, rail beam, side walk and wearing course

$$M_1 = 2594.17 \text{ kN-m}$$

Dead load moment due to wearing course

$$M_2 = 86.72 \text{ kN-m}$$

1.2.8.2.2 Shear Force due to Dead Load

For this calculation self wt of deck slab, girder, rail post and rail beam, side walk have been considered as uniform load = 32.38 kN/m and self wt of cross girder have been considered as concentrated load value of 10.82 kN

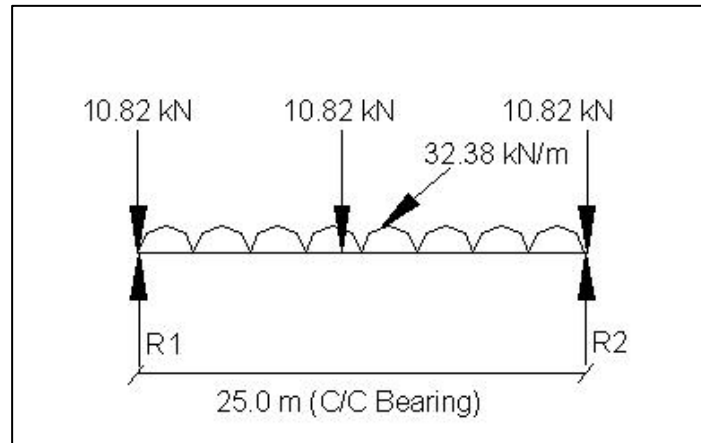


Fig 1.2.15 Loading Diagram for Shear (Exterior Girder)

$$R_1 = \{(32.38 \times 25 \times 25/2) + (10.82 \times 12.5) + (10.82 \times 25)\} / 25 = 420.98 \text{ kN}$$

Maximum shear at support,

$$\begin{aligned} &= 420.98 - 10.82 \\ &= 410.16 \text{ kN} \end{aligned}$$

$$\text{Wearing course shear force} = (1.11 \times 25) / 2 = 13.87 \text{ kN}$$

For live load moment calculation,

Pedestrian live load of 3.6×10^{-3} MPa shall be applied to all side walks wider than 600 mm and considered simultaneously with the vehicular design live load.

$$\text{Total side walk} = 0.875 \text{ m}$$

$$\text{Distribution load over side walk} = 0.875 \times 3.6 \times 10^{-3} = 3.15 \text{ kN/m}$$

$$\text{Moment due to pedestrian load} = 3.15 \times 25^2 / 8 = 246.09 \text{ kN-m}$$

Rest of the calculation are similar to that of as provided for interior girder.

1.3 STRUCTURAL DESIGN OF PC GIRDER

1.3.1 Introduction

The design example demonstrates the design of a 40.0 m span prestressed concrete girder. For this example, 200mm thick RC deck slab, 50 mm wearing course and pre-cast railing are considered. This example illustrates in detail the design of typical interior girders. The design is accomplished in accordance with the AASHTO LRFD Bridge Design Specification 2007.

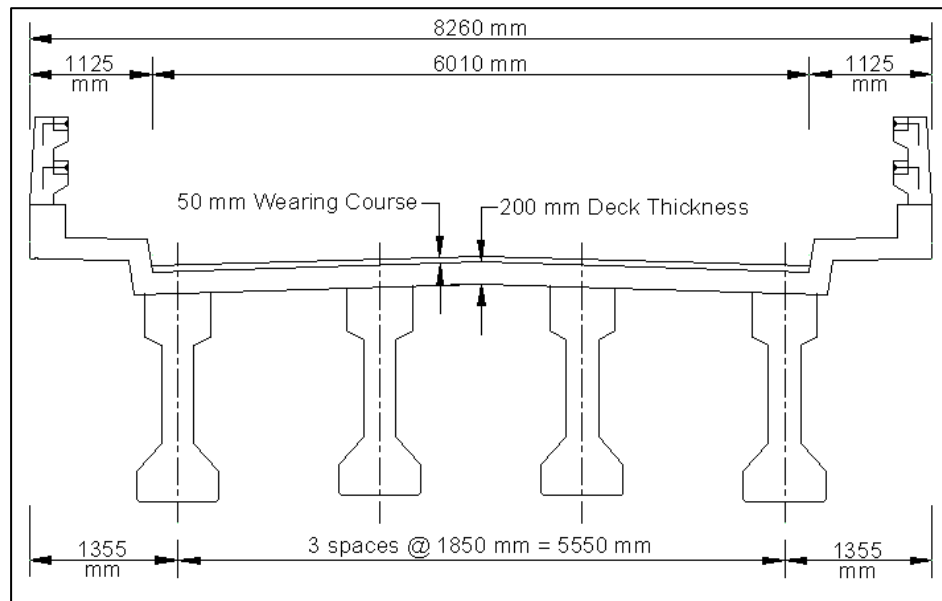


Fig 1.3.1 Bridge Cross Section

1.3.2 Data

Cast in place deck slab:

Actual thickness, $t_s = 200$ mm

Concrete strength at 28 days, $f'_c = 25$ MPa

Pre-cast girder:

Concrete strength at transfer, $f'_{ci} = 0.75 \times 35 = 26.25$ MPa

Concrete strength at 28 days, $f'_c = 35$ MPa

Concrete unit weight = 24 kN/m^3

Overall beam length = 40.65 m

Design span = 40 m

Pre-stressing strands:

12.7 mm dia , seven wire, low relaxation strands

Area of one strand = 98.71 mm^2

No of strands in one cable = 12

No of cable = 6

$$\begin{aligned}\text{Ultimate strength, } f_{pu} &= 1860 \text{ MPa} \\ \text{Yield strength} &= 0.9 f_{pu} = 1674 \text{ MPa}\end{aligned}$$

Stress limit for pre-stressing strands:

[Ref. AASHTO 07, Table 5.9.3-1]

$$\text{Before transfer, } f_{pbt} \leq 0.75 f_{pu} = 0.75 \times 1860 = 1395 \text{ MPa}$$

At service limit state after all Losses,

$$f_{pe} \leq 0.80 f_{py} = 0.80 \times 1674 = 1339.2 \text{ MPa}$$

$$\text{Modulus of elasticity, } E_p = 197000 \text{ MPa}$$

[Ref. AASHTO 07, Art. 5.4.4.2]

Non pre-stressing reinforcement:

$$\text{Yield strength of steel, } f_y = 415 \text{ MPa}$$

$$\text{Modulus of elasticity, } E_s = 200,000 \text{ MPa}$$

1.3.3 Section Property:

1.3.3.1 Non Composite Section at Mid Span:

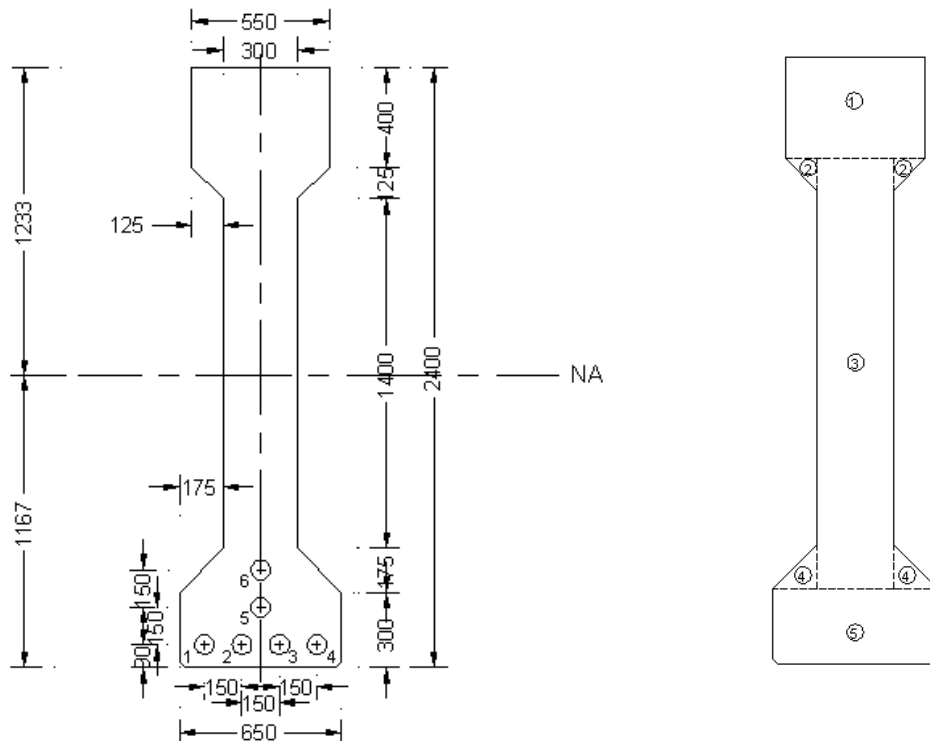


Fig 1.3.2 Non Composite Mid-Section

Table: Showing $\sum A$, $\sum Ay$, $\sum I$, $\sum A(\bar{y})^2$ for non-composite mid-section of girder

Component	b	h	A	y	Ay	y NA	I	Y bar	A(y bar) ²
	mm	mm	mm ²	mm	mm ³	mm	mm ⁴	mm	mm ⁴
1	550	400	2.20E+05	2200	4.84E+08	1167.31	2.93E+09	1032.69	2.35E+11
2	125	125	1.56E+04	2083.3	3.26E+07		6.78E+06	916.02	1.31E+10
3	300	1700	5.10E+05	1150.0	5.87E+08		1.23E+11	-17.31	1.53E+08
4	175	250	4.38E+04	383.3	1.68E+07		7.60E+07	783.98	2.69E+10
5	650	300	1.95E+05	150.0	2.93E+07		1.46E+09	1017.31	2.02E+11
Non-Composite $\sum A =$			9.84E+05	$\sum Ay =$	1.15E+09	$\sum I =$	1.27E+11	$\sum A(\bar{y})^2 =$	4.77E+11

y_b = Distance from centroid to the extreme bottom fiber of non-composite girder
= 1167.31 mm

y_t = Distance from centroid to extreme top fiber of non-composite girder
= 1232.69 mm

$\sum I = 1.32E+11 + 4.63E+11$
= 6.04E+11 mm⁴

S_b = Section modulus for the extreme bottom fiber = $I / y_b = \frac{6.04 \times 10^{11}}{1167.31} = 5.17 \times 10^8 \text{ mm}^3$

$S_t = I / y_t = \frac{6.04 \times 10^{11}}{1232.69} = 4.90 \times 10^8 \text{ mm}^3$

For normal density concrete with, $\gamma_c = 2320 \text{ kg/m}^3$

Modulus of elasticity = $4800 \sqrt{f'_c}$

Therefore, Modulus of elasticity for cast in place slab = $E_c = 4800 \sqrt{2500}$
= 24000 MPa

Pre cast girder at transfer, $E_{ci} = 4800 \sqrt{26.25} = 24592 \text{ MPa}$

Pre cast girder at service load, $E_c = 4800 \sqrt{35} = 28397 \text{ MPa}$

Calculation for effective flange width of Non- composite section:

(Ref. AASHTO 07, Art. 4.6.2.6.1)

Effective flange width shall be the lesser of:

1. $1/4 \text{ span} = 1/4 \times 40 = 10\text{m} = 10000 \text{ mm}$
2. $12 t_s + \text{greater of web thickness or } 1/2 \times \text{beam top flange width}$
= $12 \times 200 + 1/2 \times 550 = 2675 \text{ mm}$
3. Average spacing between girder = 1850 mm
Effective flange width = 1850 mm

1.3.3.2 Composite Section at Mid Span

$$\begin{aligned} \text{Modular ratio between slab and girder materials, } n &= \frac{E_c(\text{slab})}{E_c(\text{girder})} \\ &= \frac{24000}{28397} \\ &= 0.8452 \end{aligned}$$

$$\begin{aligned} \text{Transformed flange width} &= n \times (\text{effective flange width}) = 0.8452 \times 1850 \\ &= 1563.62 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{Transformed flange area} &= n \times (\text{effective flange width}) t_s = 0.8452 \times 1850 \times 200 \\ &= 312724 \text{ mm}^2 \end{aligned}$$

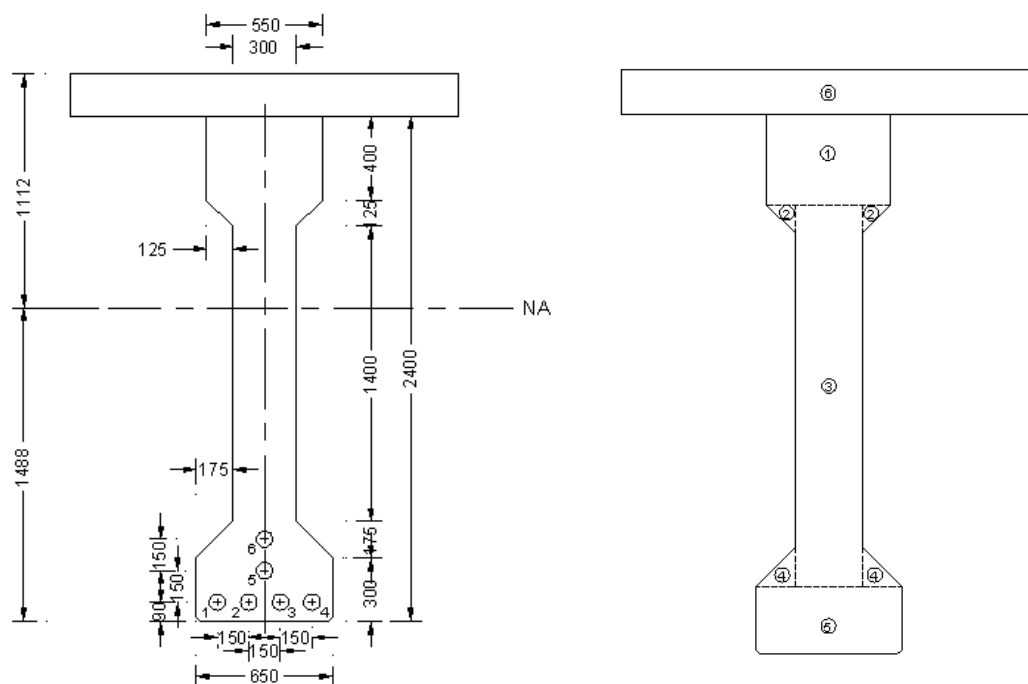


Fig 1.3.4 Composite Mid-Section

Table: Showing $\sum A$, $\sum Ay$, $\sum I$, $\sum A(\bar{y})^2$ for composite mid-section of girder

Component	b	h	A	y	Ay	y _{NA}	I	y _{bar}	A(y _{bar}) ²
	mm	mm	mm ²	mm	mm ³	mm	mm ⁴	mm	mm ⁴
1	550	400	2.20E+05	2200	4.84E+08	1488.60	2.93E+09	711.40	1.11E+11
2	125	125	1.56E+04	2083.3	3.26E+07		2.03E+07	594.73	5.53E+09
3	300	1700	5.10E+05	1150	5.87E+08		1.23E+11	-338.60	5.85E+10
4	175	250	4.38E+04	383.3	1.68E+07		2.28E+08	1105.27	5.34E+10
5	650	300	1.95E+05	150	2.93E+07		1.46E+09	1338.60	3.49E+11
6	1564	200	3.13E+05	2500	7.82E+08		1.04E+09	1011.40	3.20E+11
composite $\sum A =$			1.28E+06	$\sum Ay =$	1.93E+09	$\sum I$	1.29E+11	$\sum A(\bar{y})^2$	8.98E+11

$$\begin{aligned}
 A_c &= \text{Total area of composite girder} \\
 &= 1.30 \text{ E}+06 \text{ mm}^2 \\
 h_c &= \text{overall depth of the composite section} = 2400 + 200 = 2600 \text{ mm} \\
 I_c &= \text{moment of inertia of the composite section} \\
 &= 1.34\text{E}+11 + 8.82\text{E}+11 = 1.03\text{E}+12 \\
 y_{bc} &= \text{distance from the centroid of the composite section to the extreme bottom fiber of the pre-cast girder} = 1488.60 \text{ mm} \\
 y_{tc} &= \text{distance from the centroid of the composite section to the extreme top fiber of the deck} \\
 &= 1111.40 \text{ mm} \\
 y_{tg} &= \text{distance from the centroid of the composite section to the extreme top fiber of the pre-cast girder} = (2400 - 1488.60) = 911.4 \text{ mm} \\
 S_{bc} &= \text{Composite section modulus for the extreme bottom fiber of the pre cast girder} \\
 &= I_c / y_{bc} = 1.03 \times 10^{12} / 1488.60 = 6.9 \times 10^8 \text{ mm}^3 \\
 S_{tg} &= \text{Composite section modulus for the top fiber of the pre-cast girder} = I_c / y_{tg} \\
 &= 1.03 \times 10^{12} / 911.40 = 1.13 \times 10^9 \text{ mm}^3 \\
 S_{td} &= \text{Composite section modulus for the extreme top fiber of the deck} \\
 &= 1/n \times (I_c / y_{tc}) = 1.03 \times 10^{12} / 1111.40 \times (1/0.8452) \\
 &= 1.09 \times 10^9 \text{ mm}^3
 \end{aligned}$$

1.3.3.3 End section of PC Girder:

$$\begin{aligned}
 X - \text{sectional area} &= (300 \times 650) + (50 \times 50) + (2100 \times 550) \\
 &= 1.35 \times 10^6 \text{ mm}^2 \\
 &= 1.35 \text{ m}^2
 \end{aligned}$$

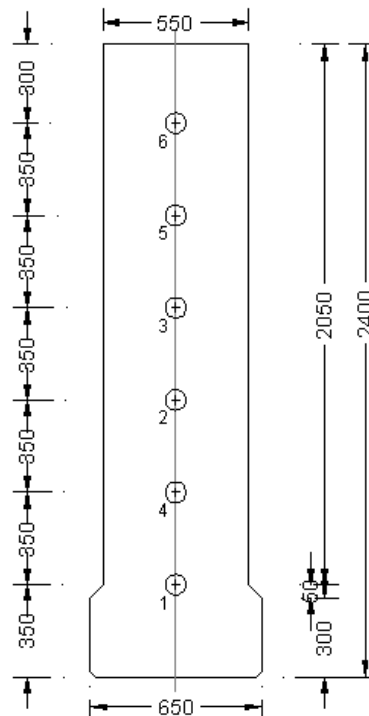


Fig 1.3.5 Non Composite End Section

1.3.4 Calculations for Interior Girder:

1.3.4.1 Dead Load Moment due to Self Weight:

Self wt. of end block = $1.35 \times 24 = 32.4 \text{ kN/m}$

Self wt of mid block = $0.984 \times 24 = 23.62 \text{ kN/m}$

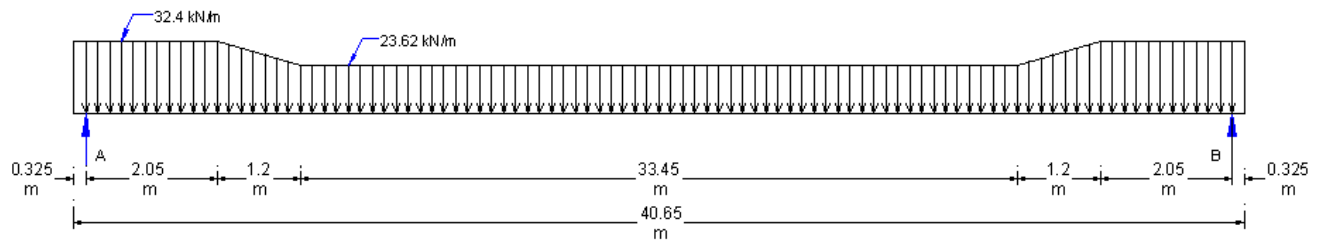


Fig 1.3.6 Load Diagram for girder self weight

$$R_A = (32.4 \times 2.4) + (32.4 + 23.62)/2 \times 1.2 + 23.62 \times 16.725$$

$$= 506.42 \text{ kN}$$

$$M_{cg} = 506.42 \times 20 - 77.76 \times 19.125 - 8.78 \times (20.325 - 2.4 - 1/3 \times 1.2) - 23.62 \times 1.2 \times 17.325$$

$$- 395.04 \times 8.36$$

$$= 4693.79 \text{ kN-m}$$

1.3.4.2 Dead Load Moment due to Cross Girder:

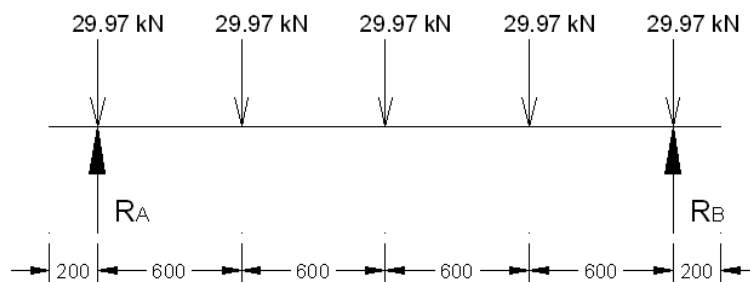


Fig 1.3.7 Load Diagram for Cross Girder

For interior girder, distance between girder = 1.85m c/c

$$\text{Load from cross girder} = (2400 \times 3/4)/1000 \times 375/1000 \times 1.85 \times 24$$

$$= 29.97 \text{ kN}$$

$$M_{c.xg} = 5 \times 29.97/2 \times 20 - 29.97 \times (10+20) = 599.4 \text{ kN-m}$$

1.3.4.3 Dead Load Moment due to Deck Slab

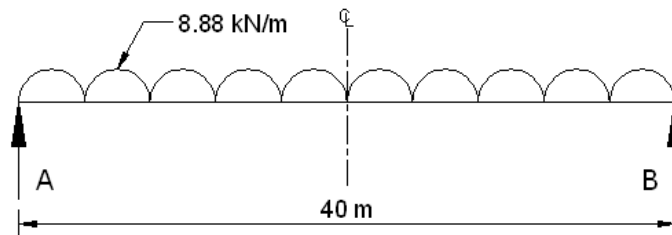


Fig 1.3.8 Load Diagram for Deck slab

$$W_d = 1.85 \times 0.2 \times 24 = 8.88 \text{ kN/m}$$

$$M_c (\text{deck}) = 8.88 \times 40^2 / 8 = 1776 \text{ kN-m}$$

1.3.4.4 Dead Load Moment due to Wearing Course:

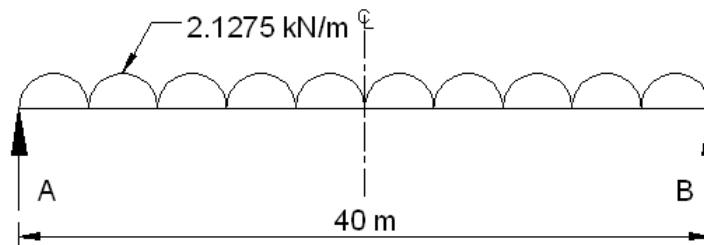


Fig 1.3.9 Load Diagram for wearing course

$$\text{Considering 50 mm thickness of wearing course} = 50/1000 \times 23 \times 1.85 = 2.1275 \text{ kN/m}$$

$$M = \frac{wL^2}{8} = 2.1275 \times 40^2 / 8 = 425.5 \text{ kN-m}$$

1.3.4.5 Total Dead Load Moment:

Total service dead load moment:

$$\begin{aligned} &= 4693.79 + 599.4 + 1776 + 425.5 \\ &= 7494.69 \text{ kN-m} \end{aligned}$$

Total factored dead load moment:

$$\begin{aligned} &= (4693.79 + 599.4 + 1776) \times 1.25 + 425.5 \times 1.5 \\ &= 9474.74 \text{ kN-m} \end{aligned}$$

1.3.5 Live load distribution factor for typical interior beams:

Live load bending moment and shear force are determined by using the simplified distribution factor formulas (Ref. AASHTO 07, Art-4.6.2.2). To use the simplified live load distribution factor formula the following conditions must be made

- Width of slab is constant **OK**
- Number of girder, $N_b \geq 4$ ($N_b = 4$) **OK**
- Beam are parallel and of same stiffness **OK**
- Road way part of overhang, $d_e \leq 910$ mm ($d_e = 0$) **OK**
- Curvature is less than 4^0 (curvature = 0^0) **OK**
(Ref. AASHTO 07 table 4.6.1.2.1-1)

Number of design lanes = 2

1.3.5.1 Distribution factor for Bending Moment:

For two or more design lane loaded,

$$DFM = 0.075 + (S/2900)^{0.6} (S/L)^{0.2} (K_g/Lt_s^3)^{0.1} \quad (\text{Ref. AASHTO 07, Table.4.6.2.2.2b-1})$$

Provided that,

DFM = Distribution factor for interior beam

S = Beam/girder spacing, mm = 1850mm

t_s = Thickness of deck, mm = 200mm

L = Length of girder, mm = 25650mm

$K_g = n(I + Ae_g^2)$ = longitudinal stiffness parameter

Here,

$$n = E_g / E_d = \sqrt{35} / \sqrt{25} = 1.18$$

E_g = Modulus of elasticity of girder

E_d = Modulus of elasticity of deck

e_g = Distance between the C.G of beam and deck = $2600 - 1488.60 - 100 = 1011.4$

mm

A = Cross-sectional area of girder, $\text{mm}^2 = 1.30 \times 10^6 \text{ mm}^2$

I = Moment of inertia of beam, $\text{mm}^4 = 1.03 \times 10^{12} \text{ mm}^4$

Thus,

$$\begin{aligned} K_g &= n(I + Ae_g^2) \\ &= 1.18 \times (1.03 \times 10^{12} + 1.30 \times 10^6 \times (1011.4)^2) \\ &= 2.785 \times 10^{12} \end{aligned}$$

Therefore,

$$\begin{aligned} DFM &= 0.075 + (1850/2900)^{0.6} (1850/40650)^{0.2} \{2.785 \times 10^{12} / (40650 \times 200^3)\}^{0.1} \\ &= 0.586 \text{ lane/girder} \end{aligned}$$

1.3.5.2 Distribution factor for Shear Force:

For two or more lane loaded,

$$DFV = 0.2 + s/3600 - (s/10700)^{2.0} \quad (\text{Ref. AASHTO 07, Table 4.6.2.2.3a-1})$$

Provided that, $1100 \leq S \leq 4900$ where $S = 1850$ mm

$6000 \leq L \leq 73000$ where $L = 40650$ mm

$110 \leq t_s \leq 300$ where $t_s = 200$ mm

$N_g \geq 4$ where $N_g = 4$

OK.

DFV = Distribution factor for shear for interior beam

Therefore,

$$DFV = 0.2 + (1850/3600) - (1850/10700)^{2.0}$$

$$= 0.2 + 0.5138 - 0.029$$

$$= 0.68 \text{ lane / girder}$$

(Ref. AASHTO 07, Table 4.6.2.2.3a-1)

1.3.5.3 Dynamic Allowance

$$IM = 33\%$$

Where, IM = dynamic load allowance applied to truck load only.

(Ref. AASHTO 07, Table 3.6.2.1-1)

1.3.6 Calculation of Live load moment for interior girder:

1.3.6.1 Moment due to truck load:

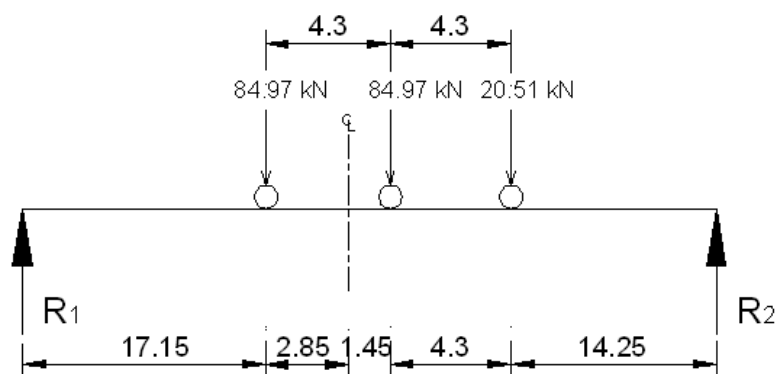


Fig 1.3.10 Load Diagram for Live Load

$$\text{Rear wheel load} = 145 \times 0.586 = 84.97 \text{ kN}$$

$$\text{Front wheel load} = 35 \times 0.586 = 20.51 \text{ kN}$$

$$R_1 = \{20.51 \times 14250 + 84.97 \times (14250 + 4300) + 84.97 \times (14250 + 4300 + 4300)\} / 40000$$

$$= 95.25 \text{ kN}$$

Maximum service moment at mid span due to truck load with dynamic load allowance:

$$= 95.25 \times 20.000 - 84.97 \times 2.850$$

$$= 1662.84 \text{ kN-m}$$

For Impact Moment, $1662.84 \times 1.33 = 2211.58 \text{ kN-m}$

1.3.6.2 Moment due to lane load:

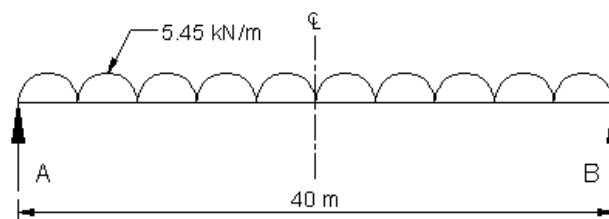


Fig 1.3.11 Load Diagram for Lane Load

Lane load, $w = 9.3 \times \text{DFM}$ (Ref. AASHTO 07, Art. 3.6.1.2.4)

$$= 9.3 \times 0.586$$

$$= 5.45 \text{ kN/m}$$

$$M = w l^2 / 8$$

$$= 5.45 \times 40^2 / 8$$

$$= 1090 \text{ kN-m}$$

Factored live load moment = $(2211.58 + 1090) \times 1.75 = 5777.77 \text{ kN-m}$

1.3.7 Calculation of Shear Force for Interior Girder:

1.3.7.1 Shear force due to truck load

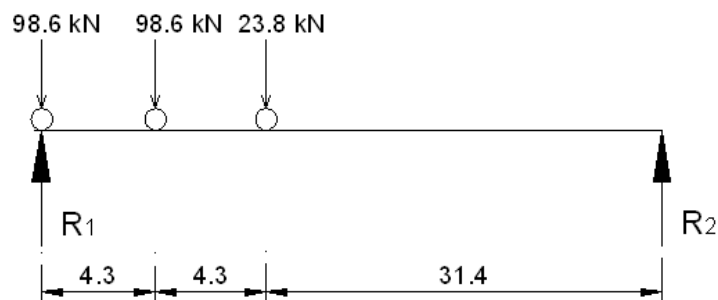


Fig 1.3.12 Load Diagram for Truck Load

$$\text{Rear wheel load} = 145 \times 0.68 = 98.6 \text{ kN}$$

$$\text{Front wheel load} = 35 \times 0.68 = 23.8 \text{ kN}$$

$$R_A = \{23.8 \times 31400 + 98.6(31400 + 4300) + 98.6(31400+4300+4300)\}/40000$$

$$= 205.28 \text{ kN}$$

$$V_A = 205.28 - 98.6 = 106.68 \text{ kN}$$

$$\text{Live load shear with impact} = 106.68 \times 1.33$$

$$= 141.89 \text{ kN}$$

1.3.7.2 Shear force due to lane load

$$W = 9.3 \times 0.68 = 6.32 \text{ kN/m}$$

$$\text{Max shear} = wl/2 = 6.32 \times 40/2 = 126.4 \text{ kN}$$

Total service dead load shear

$$\text{Shear due to self wt of girder} = 506.42 \text{ kN}$$

Shear due to X girder:

$$R_A = 29.97 \times (10+20+30+40)/40$$

$$= 74.925 \text{ kN}$$

$$\text{Shear due to X girder} = 74.925 - 29.97 = 44.96 \text{ kN}$$

$$\text{Shear due to deck slab} = 8.88 \times 20 = 178 \text{ kN}$$

$$\text{Shear due to WC} = 2.1275 \times 20 = 43 \text{ kN}$$

$$\text{Total service dead load shear} = 506.42 + 44.96 + 178 + 43$$

$$= 772.38 \text{ kN}$$

$$\text{Total service live load shear} = 141.89 + 126.4 = 268.29 \text{ kN}$$

$$\text{Total factored dead load shear} = (506.42 + 44.96 + 178) \times 1.25 + 43 \times 1.5 = 976.23 \text{ kN}$$

$$\text{Total factored live load shear} = 268.29 \times 1.75 = 469.51 \text{ kN}$$

$$\text{Total factored shear} = 976.23 + 469.51 \text{ kN}$$

$$= 1445.74 \text{ kN}$$

1.3.8 Calculation of Losses:

(Ref. AASHTO' 07 Art. 5.9.5.1)

1.3.8.1 Immediate Loss:**a) Loss due to wedge pull-in and friction:**

Loss due to friction between the internal pre-stressing tendons and the duct wall may be taken as:

$$\Delta f_{PF} = f_{pj} [1 - e^{-(Kx + \mu\alpha)}]$$

Where,

f_{pj} = Stress in the pre-stressing steel at jacking (MPa)

x = Length of a pre-stressing tendon from the jacking end to any point under consideration (mm).

K = Wobble friction co-efficient (per mm of tendon).

μ = Co-efficient of friction.

α = Sum of the absolute values of angular change of pre-stressing steel path from jacking end

if tensioning is done equally at both ends to the point under investigation (rad).

e = Base of Napierian logarithms.

Here the sample calculation for cable no. 5 is provided

$$\text{Radius of curvature, } R = L^2/8d_r = 40.65^2/(8 \times 1.51) = 136.78 \text{ m}$$

Here,

$$d_r = \text{Vertical sag} = 1510 \text{ mm}$$

When, $X = 1 \text{ m}$

$$\alpha = \sqrt{(\alpha_v^2 + \alpha_h^2)}$$

$$= \sqrt{(\alpha_v^2 + 0)}$$

$$= \alpha_v$$

$$= X/R$$

$$= 1/136.78$$

$$= 0.0073 \text{ rad}$$

Loss of pre-stress force due to friction per unit length,

$$\Delta P = P_i [1 - e^{-(Kx + \mu\alpha)}]$$

Here,

$$P_i = (0.75 \times 1860 \times 98.7 \times 12)/1000$$

$$= 1652 \text{ kN}$$

$$\mu = 0.25$$

$$\alpha = 0.0073 \text{ rad}$$

$$K = 0.007$$

$$X = 1 \text{ m}$$

So,

$$\Delta P = 1652 \times [1 - e^{-(0.007 \times 1 + 0.25 \times 0.0073)}]$$

$$= 14.52 \text{ kN/m}$$

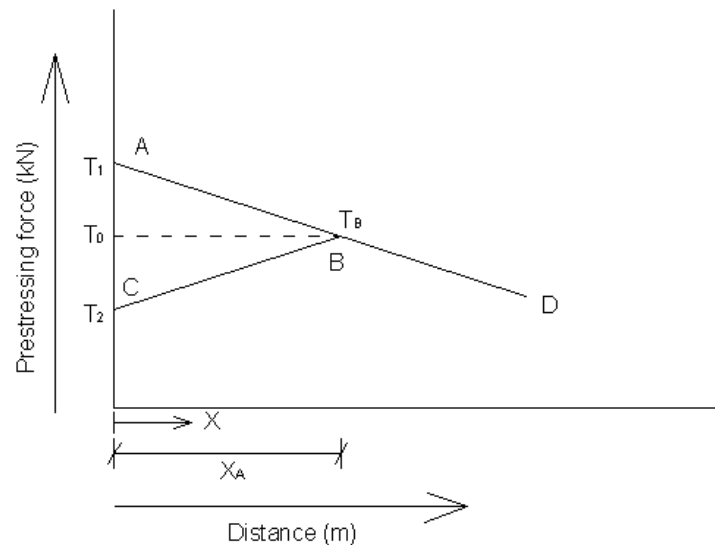


Fig 1.3.13 Loss of prestress Due to Friction and Wedge Pull-in

Note : When distance X is less than X_A the magnitude of prestress force after friction and wedge pull in losses will be the ordinate of line CB and when k is greater than X_A prestress force in the cable will be the ordinate of line BO .

Length of cable subjected to pre-stress loss due to wedge pull-in,

$$X_A = \sqrt{\{(\Delta w_p \text{ Eps } A_p s) / \Delta P\}}$$

Here,

$$\Delta w_p = 8 \text{ mm}$$

$$\text{Eps} = 197 \times 10^6 \text{ kN/m}^2$$

$$A_p s = 98.71 \times 10^{-6} \times 12 = 1184.8 \times 10^{-6} \text{ m}^2$$

So,

$$X_A = \sqrt{\{(0.008 \times 197 \times 10^6 \times 1184.4 \times 10^{-6}) / 14.52\}} = 11.34 \text{ m}$$

Now,

$$\begin{aligned} P_{XA} &= P_i e^{-(Kx + \mu\alpha)} \\ &= 1652 \times e^{-(0.007 \times 11.34 + 0.25 \times 0.0829)} \\ &= 1494.63 \text{ kN} \end{aligned}$$

Cable force at mid,

When, $X_A = 20.325 \text{ m}$

$$\alpha_v = X_A / R = 20.325 / 136.78 = 0.1485 \text{ rad}$$

Now,

$$\begin{aligned} P_{XA} &= P_i e^{-(Kx + \mu\alpha)} \\ &= 1652 \times e^{-(0.007 \times 20.325 + 0.25 \times 0.1485)} \\ &= 1380.70 \text{ kN} \end{aligned}$$

Table: Calculation of sag & radius of curvature

Cable no	Vertical sag, d_r (m)	Radius of curvature, R , (m)
1	0.26	794.43
2	0.96	215.16
3	1.31	157.67
4	0.610	338.61
5	1.51	136.79
6	1.71	12079

Table: Calculation of wedge pull in and friction loss

Cable no	Initial pre-stress force, P_i , (kN)	$\alpha = X/R$ for $X=1$, (rad)	Loss of pre-stress force per unit length, ΔP , (kN/m)	Distance of wedge pull-in X_A , (m)	$\alpha = X_A/R$ for X_A distance, (rad)	Cable force at X_A , P_{XA} , (kN)	$\alpha = X/R$ for $X=20.325$ m distance, (rad)	Cable force at $X=20.325$ m P_x (kN)	Loss of pre-stress %
1	1652	0.0013	12.05	12.45	0.0157	1508.2	0.026	1424	13.80
2	1652	0.0048	13.41	11.80	0.0548	1500.3	0.094	1400	15.25
3	1652	0.0031	14.11	11.50	0.0729	1496.7	0.128	1388	15.98
4	1652	0.0058	12.71	12.12	0.0358	1504.1	0.060	1412	14.52
5	1652	0.0068	14.51	11.34	0.0829	1494.7	0.149	1381	16.40
6	1652	0.0078	14.92	11.19	0.0926	1492.6	0.168	1374	16.80

 $\Sigma P_X = 8998.2 \text{ kN}$ $\Sigma \text{Loss} = 92.75$

Average loss of pre-stress = $92.75/6 = 15.5 \%$

b) Calculation of loss of prestress due to elastic shortening:

$$\text{Elastic shortening, } \Delta f_{\text{PES}} = \left\{ \frac{(N-1)}{2N} \right\} \times \left(\frac{E_P}{E_{ci}} \right) \times f_{cgp}$$

Here,

N = number of identical pre stressing tendon

f_{cgp} = Sum of concrete stresses at the centre of gravity of pre-stressing tendon due the pre-stressing force after jacking and self weight of the member at the section of maximum moment.

f_{cgp} value may be calculated using a steel stress reduced below the initial value by a margin depends on elastic shortening relaxation and friction effect.

$$f_{cgp} = P/A + Pe^2/I - M_{Ge}/I$$

$$\begin{aligned} P &= \text{Effective prestress force} \\ &= P_i - (\% \text{ of elastic shortening} + \text{relaxation} + \text{friction effects}) \times P_i \\ &= 1652 - \{(3+0+16) \times 1652\}/100 \\ &= 1338.12 \text{ kN} \end{aligned}$$

Assume,

Elastic shortening loss = 3%

Relaxation loss = 0%

M_G = Moment for self wt of girder = 4693.79 kN-m

$e = 1167.31 - 165 = 1002.31 \text{ mm} = 1.00 \text{ m}$

$A = 0.984 \text{ m}^2$

$I = 0.604 \text{ m}^4$

N = Number of initial pre-stressing tendon = 6

Now,

$$\begin{aligned} f_{cgp} &= P/A + Pe^2/I - M_{Ge}/I \\ &= 1338.12 \times 6 / 0.984 + 1338.12 \times 6 \times (1)^2 / 0.604 - 4693.79 \times 1 / 0.604 \\ &= 8159.26 + 13292.58 - 7771.18 \\ &= 13680 \text{ kN/m}^2 \\ &= 13.68 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \Delta f_{PES} &= \{(N-1)/2N\} (E_p/E_{ci}) f_{cgp} \\ &= \{(6-1)/(2 \times 6)\} \times (197 \times 10^3 / 24952) \times 13.68 \\ &= 45.66 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{So, Elastic shortening loss} &= 45.66 \times 10^3 \times 100 \times 1184 \times 10^{-6} / 1652 \\ &= 3.27\% \end{aligned}$$

1.3.8.2 Determination of Long Term Losses:

a) Shrinkage loss:

Loss of pre stress due to shrinkage in post tensioned member is calculated by using the following equation:

$$\Delta f_{SH} = 83 \gamma_h \gamma_{st}$$

Here,

$$\gamma_{st} = 35 / (7 + f'_{ci})$$

$$\gamma_h = 1.7 - 0.01H$$

Here,

γ_{st} = Correction factor for specific concrete strength at time of prestress transfer to the concrete member.

γ_h = Correction factor for relative humidity of the ambient air.

H = The average annual ambient relative humidity (%)

= 60% (Assume)

$$f'_{ci} = 0.75 \times 35$$

$$= 26.25$$

So,

$$\gamma_{st} = 35/(7 + 26.25) = 1.0526$$

$$\gamma_h = 1.7 - 0.01 \times 60 = 1.1$$

$$\Delta f_{SH} = 83 \gamma_h \gamma_{st}$$

$$= 83 \times 1.1 \times 1.0526$$

$$= 96.1 \text{ MPa}$$

$$\begin{aligned} \text{Shrinkage loss \%} &= 96.1 \times 10^3 \times 100 \times 1184.4 \times 10^{-6}/1652 \\ &= 6.9\% \end{aligned}$$

b) Creep loss in post tension member:

$$\Delta f_{cr} = 10.0 (f_{pi} A_{ps}/A_g) \gamma_h \gamma_{sT}$$

Here,

f_{pi} = Pre-stressing steel stress immediately prior to transfer (MPa)

$$= 0.75 \times 1860$$

$$= 1395 \text{ MPa}$$

$$A_{ps} = 98.7 \times 12 \times 6$$

$$= 7106.4 \text{ mm}^2$$

$$A_g = 1.30 \times 10^6 \text{ mm}^2$$

So,

$$\Delta f_{cr} = 10.0 (f_{pi} A_{ps}/A_g) \gamma_h \gamma_{sT}$$

$$= 10 \times (1395 \times 7106.4/1.30 \times 10^6) \times 1.1 \times 1.0526$$

$$= 88.30 \text{ MPa}$$

$$\begin{aligned} \text{Creep loss \%} &= 88.30 \times 10^3 \times 100 \times 1184.4 \times 10^{-6}/1652 \\ &= 6.33\% \end{aligned}$$

c) Steel relaxation loss:

Referring from AASHTO designation M204-89,

Relaxation loss of pre-stressing steel after 100 hr = 2.5%

Relaxation loss of pre-stressing steel after 1000 hr = 3.5%

1.3.9 Schedule of Stresses:

- a) Moment due to self wt. of girder,

$$M_G = 4693.79 \text{ kN-m}$$

$$\begin{aligned} \text{Stress at girder bottom, } \sigma_b &= 4693.79 \times 1.167 / (0.604 \times 1000) \\ &= 9.07 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Stress at girder top, } \sigma_t &= 4693.79 \times 1.232 / (0.604 \times 1000) \\ &= 9.57 \text{ MPa} \end{aligned}$$

$$\text{Eccentricity} = 1167.31 - 167 = 1002.31 \text{ mm}$$

- b) Moment due to pre-stress = $1652 \times 6 \times 1.0$
= 9912 kN-m

So,

$$\begin{aligned} \text{Stress at girder bottom, } \sigma_b &= 9212 \times 1.167 / (0.604 \times 1000) \\ &= 19.15 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Stress at girder top, } \sigma_t &= 9912 \times 1.232 / (0.604 \times 1000) \\ &= 20.22 \text{ MPa} \end{aligned}$$

- c) Moment due to cross girder = 599.4 kN-m

So,

$$\begin{aligned} \text{Stress at girder bottom, } \sigma_b &= 599.4 \times 1.167 / (0.604 \times 1000) \\ &= 1.158 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Stress at girder top, } \sigma_t &= 599.4 \times 1.232 / (0.604 \times 1000) \\ &= 1.22 \text{ MPa} \end{aligned}$$

- d) Moment due to deck slab = 1776 kN-m

So,

$$\begin{aligned} \text{Stress at girder bottom, } \sigma_b &= 1776 \times 1.167 / (0.604 \times 1000) \\ &= 3.46 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Stress at girder top, } \sigma_t &= 1776 \times 1.232 / (0.604 \times 1000) \\ &= 3.62 \text{ MPa} \end{aligned}$$

- e) Moment due to wearing course = 425.5 kN-m

So,

$$\begin{aligned} \text{Stress at girder bottom, } \sigma_b &= 425.5 \times 1.488 / (1.03 \times 1000) \\ &= 0.615 \text{ MPa} \end{aligned}$$

$$\begin{aligned} \text{Stress at girder top, } \sigma_t &= 425.5 \times 0.911 / (1.03 \times 1000) \\ &= 0.38 \text{ MPa} \end{aligned}$$

Here,

$$S_{td} = 1.09 \times 10^9 \text{ mm}^3$$

$$\sigma_{td} = 425.5 / (1.09 \times 1000)$$

$$= 0.39 \text{ MPa}$$

f) Total live load moment = 3301.58 kN-m

So,

$$\text{Stress at girder bottom, } \sigma_b = 3301.58 \times 1.488 / (1.03 \times 1000)$$

$$= 4.77 \text{ MPa}$$

$$\text{Stress at girder top, } \sigma_t = 3301.58 \times 0.911 / (1.03 \times 1000)$$

$$= 2.92 \text{ MPa}$$

Here,

$$S_{td} = 1.09 \times 10^9 \text{ mm}^3$$

$$\sigma_{td} = 3301.58 / (1.09 \times 1000)$$

$$= 3.028 \text{ MPa}$$

Loss of pre-stress due to creep modified differential shrinkage:

Let,

Creep modified differential shrinkage, $A_{sh} = 100 \times 10^{-6}$

Force due to creep modified differential shrinkage,

$$P_{diff} = 100 \times 10^{-6} \times 1.56 \times 0.2 \times 28.397 \times 10^6$$

$$= 886 \text{ kN}$$

$$\text{Stress at deck top, } = [886/1.30 + 886 \times 1.007/1.09 - 100 \times 10^{-6} \times 28.397 \times 10^6] \times 1/1000$$

$$= -1.33 \text{ N/mm}^2$$

$$\text{Stress at girder bottom, } \sigma_b = [886/1.30 - (886 \times 1.007 \times 1.488)/1.03] \times 1/1000$$

$$= -0.607 \text{ N/mm}^2$$

$$\text{Stress at girder top, } \sigma_t = [886/1.30 + (886 \times 1.007 \times 0.911)/1.03] \times 1/1000$$

$$= 1.48 \text{ N/mm}^2$$

Table: Schedule of Stresses

Sl no.	Description of item	Axial force kN	Bending moment (kN-m)	Stress at girder bottm (N/mm2)	Stress at girder top (N/mm2)	Stress at deck top (N/mm2)
01	Moment due to self wt of girder		4693.79	-9.07	+9.57	
02	Axial force due to pre stressing(1652x6) Moment due to prestressing (1652 x 6 x 1.00)	9912	9912	+10.07 +19.15	+10.07 -20.22	
03	Loss of pre stress due to friction = 16 %			-4.67	+1.62	

04	Loss of prestress due to elastic shortening (3.27 %)			-0.967	+0.332	
Sub Total 1:				14.51	1.372	
Allowable compression, $0.6f'_{ci} = 15.75 \text{ N/mm}^2$				OK	OK	
Allowable tension $-0.25\sqrt{f'_{ci}} = -1.28 \text{ N/mm}^2$						
05	Loss of prestress due to relaxation loss 0 %			-	-	
06	Loss of prestress due to shrinkage 6.9%			-2.016	+0.700	
Sub total 2				12.5 OK	2.03 OK	
07	Moment due to X girder		599.4	-1.158	+1.22	+0.39
08	Moment due to deck		1776	-3.46	+3.62	
09	Moment due to wc		425.5	-0.615	+0.38	
10	Moment due to LL		3301.58	-4.77	+2.92	+3.028
11	Final relaxation (3.5%)			-1.022	+0.355	
12	Stress due to creep modified diff, shrinkage			-0.607	+1.48	-1.33
13	Creep loss (6.33%)			-1.85	+0.642	
Total stress at service				-0.982	12.65	2.088
Load condition				OK	OK	OK
Allowable compression, $0.45f'_c = 15.75 \text{ N/mm}^2$						
Allowable tension, $-0.5\sqrt{f'_c} = -2.96 \text{ N/mm}^2$						

1.3.10 Calculation of Moment Capacity:

Average stress in pre-stressing steel when $f_{pe} \geq 5 \text{ fpu}$

$$f_{ps} = f_{pu}(1 - K c/d_p) \quad [\text{Ref. AASHTO 07, Eq. 5.7.3.1.1-1}]$$

$$f_{ps} = \text{Average stress in prestressing steel}$$

$$f_{pu} = \text{specified tensile strength of pre-stressing steel} = 1860 \text{ MPa}$$

$$K = 2(1.04 - f_{py}/f_{pu}) \quad [\text{Ref. AASHTO 07, Eq. 5.7.3.1.1-2}]$$

$$= 0.28 \text{ for low relaxation strand} \quad [\text{Ref. AASHTO 07, Table 5.7.3.1.1-1}]$$

$$d_p = \text{distance from extreme compression fiber to centroid of the pre stressing tendon}$$

$$= h - y_{bs} = 2600 - 165 = 2435 \text{ mm}$$

$[y_{bs} = \text{distance between the c.g of the prestressing cables and bottom concrete fiber of the beam} = 165]$

c = distance between the neutral axis and the compression face

Assuming rectangular behavior:

$$\begin{aligned} c &= (A_{ps} f_{pu} + A_s f_y - A_s' f_y') / (0.85 f_c' \beta_1 b + k A_{ps} f_{pu} / d_p) \\ &= (12 \times 98.71 \times 6 \times 1860 + 0 - 0) / \{ (0.85 \times 25 \times 0.85 \times 1850) + (0.28 \times 12 \times 98.71 \times 6 \times 1860 / 2435) \} \\ &= 13217904 / (33415.63 + 1519.92) = 378.35 > h_f \text{ mm} \\ &= 378.35 > 200 \text{ mm} \quad \text{Not ok} \end{aligned}$$

Assuming T-section behavior:

So,

$$\begin{aligned} c &= (A_{ps} f_{pu} + A_s f_s - A_s' f_s' - 0.85 f_c' (b - b_w) h_f) / (0.85 f_c' \beta_1 b_w + k A_{ps} f_{pu} / d_p) \\ &= \frac{(12 \times 98.71 \times 6) \times 1860 + 0 - 0 - 0.85 \times 35 (1564 - 300) \times 200}{0.85 \times 35 \times 0.85 \times 300 + 0.28 (12 \times 6 \times 98.71) \times 1860 / 2435} \\ &= 625.63 \text{ mm} \end{aligned}$$

$$a = \beta_1 \times c = 0.85 \times 625.63 = 531.78 \text{ mm}$$

$$\begin{aligned} f_{ps} &= f_{pu} (1 - k c / d_p) \\ &= 1860 (1 - 0.28 \times 625.63 / 2435) = 1726.19 \text{ MPa} \end{aligned}$$

$M_r = \Phi M_n$ where M_n = Nominal resisting moment

$$\Phi = 1 \quad [\text{Ref. AASHTO 07, Art. 5.5.4.2}]$$

$$\begin{aligned} M_n &= A_{ps} f_{ps} (d_p - a/2) + A_s f_s (d_s - a/2) + A_s' f_s' (d_s' - a/2) + 0.85 f_c' (b - b_w) h_f (a/2 - h_f/2) \\ &= (12 \times 6 \times 98.71) \times 1726.19 (2435 - 531.78/2) + 0 + 0 + 0.85 \times 35 (1564 - 300) \times 200 (531.78/2 - 200/2) \\ &= (2.66 \times 10^{10} + 1.25 \times 10^9) / 10^6 \\ &= 27850 \text{ kN-m} \end{aligned}$$

$$M_r > M_u$$

OK

1.3.11 Calculation of Non-prestressing Reinforcement:

$$\begin{aligned} \text{Surface reinforcement} &= 0.003 b t \quad [\text{Ref. AASHTO 07, Art. 5.6.3.6}] \\ &= 0.003 \times 1000 \times 300/2 = 450 \text{ mm}^2 / \text{m} \end{aligned}$$

Providing T-10

$$\text{Spacing} = 1000 \times 78.5 / 450 = 175 \text{ mm}$$

$$\text{Total no. of surface bar needed} = 2300 / 175 \times 2 = 26$$

1.3.12 Calculation of Shear Reinforcement:

(Ref. AASHTO'07, Art. 5.8.3.3)

The nominal shear resistance V_n shall be determined as lesser of

$$V_n = V_c + V_s + V_p \dots\dots\dots(1)$$

$$V_n = 0.25 f_c' b_v d_v + V_p \dots\dots(2)$$

Where, $V_c = 0.083\beta\sqrt{f_c'}b_vd_v$ b_v = effective web width as the minimum web width within
The depth d_v
= 300 mm

d_v = effective shear depth taken as the distance measured perpendicular to neutral axis between the resultant of the tensile and compressive forces due to flexure it need not be taken to be lesser than the greater of 0.9 d_e or 0.72h(mm)

$$(i) \quad d_v = M_n / A_s f_y = A_s f_y (d - a/2) / A_s f_y = (d - a/2) = (2435 - 531.78/2) = 2169.11 \text{ mm}$$

$$(ii) \quad 0.72h = 0.72 \times 2600 = 1872 \text{ mm}$$

$$(iii) \quad 0.9d_e = 0.9 \times 2435 = 2191.5 \text{ mm}$$

$$0.9d_e > 2169.11, \text{ Hence } d_v = 2191.5 \text{ mm}$$

1.3.12.1 Calculation of β & θ :

Here, β = factor indicating ability of diagonally cracked concrete to transmit tension as specified in

AASHTO '07 Article 5.8.3.4

θ = Angle of inclination of diagonal compressive stresses as determined in AASHTO'07 Article 5.8.3.4

$$\begin{aligned} v_u &= \text{Total factored shear} / \text{Area} \\ &= [1445.74 \times 10^3 / 1.30 \times 10^6] \times 1/1000 \\ &= 1.112 \times 10^{-3} \end{aligned}$$

$$v_u / f_c' = 1.112 \times 10^{-3} / 35 = 3.18 \times 10^{-5} \text{ m}^2$$

Referred from AASHTO 07 Table: 5.8.3.4.2

$$\theta = 36.4, \beta = 2.23$$

$$\begin{aligned} \therefore V_c &= 0.083\beta\sqrt{f_c'}b_vd_v & [\text{Ref. AASHTO 07, Art. 5.8.3.3}] \\ &= 0.083 \times 2.23 \times \sqrt{35} \times 300 \times 2191.5 \\ &= 719912.48 \text{ N} \end{aligned}$$

$$\therefore V_s = A_v f_y d_v \cot \theta / S$$

Here, $S = 125 \text{ mm C/C}$

$$A_v = 113 \times 2 = 226 \text{ mm}^2$$

$$\begin{aligned} V_s &= 226 \times 415 \times 2191.5 \times 1.36 / 125 \\ &= 2236283.74 \text{ N} \end{aligned}$$

1.3.12.2 Calculation of Prestress Force Component:

Effective prestress force of Cable No. 1	$P_1 = 1652 - 2(1652 - 1508.1) = 1362.20 \text{ kN}$
Effective prestress force of Cable No. 2	$P_2 = 1692 - 2(1652 - 1500.3) = 1348.60 \text{ kN}$
Effective prestress force of Cable No. 3	$P_3 = 1652 - 2(1652 - 1496.7) = 1341.38 \text{ kN}$
Effective prestress force of Cable No. 4	$P_4 = 1652 - 2(1652 - 1504.1) = 1356.20 \text{ kN}$
Effective prestress force of Cable No. 5	$P_5 = 1652 - 2(1652 - 1494.6) = 1337.26 \text{ kN}$
Effective prestress force of Cable No. 6	$P_6 = 1652 - 2(1652 - 1492.6) = 1333.16 \text{ kN}$

$V_{P1} = 1362.2 \times 0.0256$	$= 34.87 \text{ kN}$	$\theta_1 = 1.47$
$V_{P2} = 1348.6 \times 0.0941$	$= 126.92 \text{ kN}$	$\theta_2 = 5.40$
$V_{P3} = 1341.4 \times 0.1279$	$= 171.60 \text{ kN}$	$\theta_3 = 7.35$
$V_{P4} = 1356.2 \times 0.060$	$= 81.37 \text{ kN}$	$\theta_4 = 3.44$
$V_{P5} = 1337.26 \times 0.1469$	$= 196.44 \text{ kN}$	$\theta_5 = 8.45$
$V_{P6} = 1333.16 \times 0.1659$	$= 221.17 \text{ kN}$	$\theta_6 = 9.55$

$$\begin{aligned} \text{Total } V_P &= 832.37 \text{ kN} \\ V_n &= (719912.48 + 2236283.74 + 832370) / 1000 \\ &= 3788.56 \text{ kN} \\ \text{Again } V_n &= (0.25 \times 35 \times 2191.5 \times 300 + 832370) / 1000 \\ &= 6585 \text{ kN} \\ \text{Hence } V_n &= 3788.56 \text{ kN} > 1445.74 \text{ kN, Hence OK.} \end{aligned}$$

1.3.12 Calculation of Deflection:

Uniformly distributed load due to prestressing force at transfer,

$$\begin{aligned} \text{c.g of cables at end} &= (1 \times 350 + 1 \times 700 + 1 \times 1050 + 1 \times 1400 + 1 \times 1750 + 1 \times 2100) / 6 \\ &= 1225 \text{ mm} \end{aligned}$$

$$\text{c.g of cables at mid} = 165 \text{ mm}$$

$$w = 8Fh/L^2$$

$$\begin{aligned} &= 8 \times 1652 \times 6 \times 1.060 / 40.65^2; \quad \text{Here, } h = 1225 - 165 = 1060 \text{ mm} \\ &= 51 \text{ kN/m} \end{aligned}$$

Deflection due to prestressing force at transfer,

$$\Delta_P = 5wL^4 / 384EI$$

$$E_{ci} = \text{modulus of elasticity of concrete at transfer} = 24.59 \times 10^6 \text{ kN/m}^2$$

$$I = \text{moment of inertia of non-composite girder} = 0.604 \text{ m}^4$$

$$\Delta_P = (5 \times 51 \times 40.65^4 / 384 \times 24.59 \times 10^6 \times 0.604) \times 1000 = 122 \text{ mm}$$

$$\text{Net deflection due to prestress} = 122 - [(0.058 \times 1652 \times 6) \times 40.65^2 / 8 \times 24.59 \times 10^6 \times 0.604] \times 1000$$

$$= 114 (\uparrow)$$

Deflection due to beam self wt,

$$\Delta_g = 5wL^4 / (384E_{ci}I)$$

w = beam self wt. = 27.86 kN/m

$$\Delta_g = (5 \times 27.86 \times (40.65)^4) / (384 \times 24.59 \times 10^6 \times 0.604) \\ = 0.067 \text{ m} = 67 \text{ mm} (\downarrow)$$

Deflection after transfer = 114-67 = 47mm

Deflection due to X-girder,

$$\Delta_{xg} = (90 \times 40.65^3 / 48 \times 28.39 \times 10^6 \times 0.604) \times 1000 = 7.34 \text{ mm}$$

Deflection due to slab wt,

$$\Delta_s = 5wL^4 / (384E_cI)$$

E_c = modulus of elasticity of concrete at service stage = 28.39×10^6 kN/m²

w = slab wt. = 8.88 kN/m

$$\Delta_s = [(5 \times 8.88 \times (40.65)^4) / (384 \times 28.39 \times 10^6 \times 1.03)] = 10.8 \text{ mm} (\downarrow)$$

Deflection due to wearing course,

$$\Delta_{wc} = 5wL^4 / (384E_cI_c)$$

w = wearing course wt. = 2.13 kN/m

$$\Delta_{wc} = (5 \times 2.13 \times (40.65)^4) / (384 \times 28.39 \times 10^6 \times 1.03) = 2.62 \text{ mm} (\downarrow)$$

Deflection due to lane load,

$$\Delta_{LL} = 5wL^4 / (384E_cI_c)$$

w = lane load = 5.45 kN/m

$$\Delta_{LL} = (5 \times 5.45 \times (40.65)^4) / (384 \times 28.39 \times 10^6 \times 1.03)$$

$$= 6.15 \text{ mm} (\downarrow)$$

Deflection due to truck & impact load,

$$\Delta_{WL} = PL^3 / (48E_cI_c)$$

P = wheel load = $(145 \times 2 + 35) \times \text{DFM} \times \text{Dynamic allowance}$

$$= 325 \times 0.586 \times 1.33$$

$$= 253.3 \text{ kN}$$

$$\Delta_{WL} = (253.3 \times (40)^3 \times 1000) / (48 \times 28.395 \times 10^6 \times 1.03)$$

$$= 11 \text{ mm} (\downarrow)$$

Allowable deflection for live load = $L/800$ (Ref. AASHTO 07 Art. 2.5.2.6.2)

$$= (40.65) \times 103 / 800 = 50.82 \text{ mm}$$

$$\text{Total live load deflection} = 11 + 6.15 = 17.15 \text{ mm} < 50.82 \text{ mm}$$

Hence OK.

1.3.14 Design of End block

Taking bursting force = 30% of jacking force

[Ref. AASHTO 07, Art.5.10.9.6]

$$T_{\text{burst}} = (.30 \times 12 \times 98.7 \times 1860) / 100 \\ = 661 \text{ kN}$$

Yield stress of steel, $f_y = 415$ Mpa

Allowable stress, $f_s = 207.5$ Mpa

$$A_t = 661 \times 10^3 / 207.5 = 3186 \text{ mm}^2$$

[Ref. AASHTO 07, Art.10.9.3.2]

Reinforcement is distributed in $1.5 \times (\text{lateral dimension}) = 1.5(550+650)/2 = 900 \text{ mm}$
Hence 32-T12-125 vertical bar is provided.

1.3.15 Cable Profile Details

12K-13 Cable requires duct size of minimum 55mm (inner). Here, 65 mm of duct size is used for cable profiling.

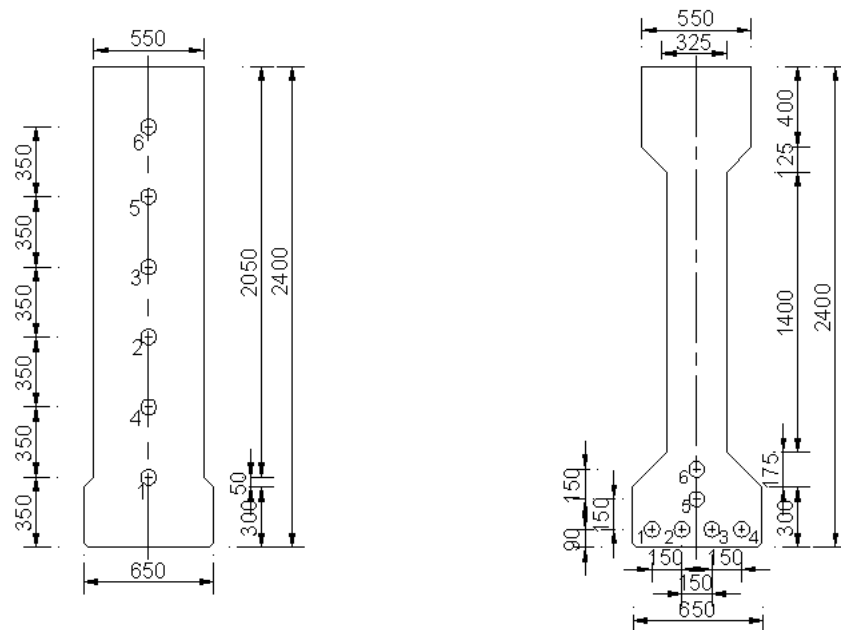


Fig 1.3.14 Cable Profile of End and Mid-section of PC girder

Distance of $(65+50) = 115$ is required as minimum distances between the ducts. In this case, 150mm is provided between the ducts in horizontal direction. Parabola equations are used for profiling the cables. Vertical coordinates of the cables at different length are located using the following equation

$$Y = 4 \times X \times H \times (L-X)/L^2$$

Here,
 X = Distance in the long direction
 H = Vertical distance of the cables in mid and end section
 L = Total Length of Girder

And, Horizontal Co-ordinates are calculated using the following equation

$$Z = Z \text{ coordinate of end section} + 4 \times (L - 2 \times \text{End Block}) \times Z \text{ coordinate of mid section} \times \{(L - 2 \times \text{End Block}) - (X \text{ coordinate at desired section} - \text{end block})\} / (L - 2 \times \text{End Block})^2$$

The table is provided below where the cable profile ordinates of Cable no 1 are calculated.

Table: Cable Profile Ordinates of Cable 1.

Ordinates	X=0	X=L/20	X=L/10	X=3L/20	X=L/5	X is measured from End section.
X	0	2032.5	4065	6097.5	8130	
Y	350	300.60	256.40	217.40	183.60	
Z	0	0	-39.85	-83.25	-120.85	
Ordinates	X=L/4	X=3L/10	X=7L/20	X=2L/5	X=9L/20	X=L/2
X	10162.5	12195	14227.5	16260	18292.5	20325
Y	155.00	131.6	113.40	100.40	92.60	90.00
Z	-152.67	-178.71	-198.96	-213.42	-222.10	-225

CHAPTER-2 ELASTOMERIC BEARING DESIGN (SI UNITS)

METHOD B - STEEL - REINFORCED ELASTOMERIC BEARINGS (AASHTO 2007 ART. NO. 14.7.5)

2.1 Initial Design Data

Span	= 25.0 m
Dead Load, P_D	= 434 kN (due to self wt. of deck, girder, x-girder & wearing course at service condition)
Live Load, P_{LL}	= 340 kN (due to truck load without impact & lane load at service condition)
Horizontal Movement of Bridge Superstructure, Δ_0	= 7 mm [Detailed calculations are provided hereafter]

Detailed Calculation of Horizontal Movement of Bridge Superstructure, Δ_0

$$\begin{aligned}\Delta_T &= 0.5 \times L \times \alpha \times \Delta t \\ &= (25000/2) \times 12 \times 10^{-6} \times 30 \\ &= 4.50 \text{ mm}\end{aligned}$$

$$\begin{aligned}\Delta_{SH} &= \epsilon_{SH} \times L/2 \\ &= 200 \times 10^{-6} \times 25000/2 \\ &= 2.50 \text{ mm}\end{aligned}$$

$$\begin{aligned}\Delta_0 &= 4.5 + 2.5 \\ &= 7.0 \text{ mm}\end{aligned}$$

Axis of Pad Rotation:	Transverse
Calculated Rotation	= 0.005 Radians
Rotation Construction Tolerance	= 0.005 Radians (Ref. AASHTO 2007, Art. 14.4.2.1)
Design Rotation, θ_s	= 0.008 Radians (Obtained from STAAD analysis)
Bearing Shape:	Rectangular

Note:

1. Bearing is Subject to Shear Deformation.
2. Bridge Deck is Not Fixed against Horizontal Translation

2.2 Bearing Geometry

Flange Width = 460 mm
 Bearing Width, $W = 350$ mm
 Flange Width $\geq W$
 $460 \text{ mm} \geq 350 \text{ mm}$

OK

Total Unfactored Compressive Load, $P_T = (434+340) \times 1000$
 $= 774000 \text{ N.}$
 Minimum Required Area of Bearing, $A_{\min} = 774000/11 = 70364 \text{ mm}^2$ (subject
 to shear deformation)
 (Ref. AASHTO 2007, Art.
 14.7.5.3.2)
 Minimum Bearing Length, $L_{\min} = 70634/350 = 201 \text{ mm.}$
 Bearing Length, $L = 250 \text{ mm.}$
 Bearing Length, $L \geq \text{Minimum Bearing Length, } L_{\min}$
 $250 \text{ mm} \geq 201 \text{ mm}$

OK

Bearing Provided, $A = 350 \times 250$
 $= 87500 \text{ mm}^2.$

2.3 Shear Deformation: (REF.AASHTO 2007, ART. 14.7.5.3.4)

Maximum Total Shear Deformation of Elastomer at Service Limit,
 $\Delta s = \Delta_0 = 7.0 \text{ mm.}$
 Factored shear deformation $2\Delta s = 2 \times 7.0 = 14.0 \text{ mm}$
 Elastomeric Layer Thickness, $h_{ri} = 10.0 \text{ mm}$
 Thickness of top and Bottom Cover Layers (each),
 $h_{\text{cover}} = 5.0 \text{ mm}$
 $h_{\text{cover}} \leq 0.7 h_{ri}$
 (Ref. AASHTO 2007, Art. 14.7.5.1)

$$5.0 \leq 0.7 \times 10.0 = 5.0 \leq 7.0$$

OK

Number of Interior Elastomeric Layers, $n_{\text{int}} = 4$
 (Excluding Exterior Layer Allowance)

Total Elastomer Thickness = $h_{rt} = 2h_{\text{cover}} + n_{\text{int}}h_{ri} = 2 \times 5 + 4 \times 10 = 50 \text{ mm.}$
 $h_{rt} \geq 2\Delta s$ (Ref. AASHTO 2007, Art.14.7.5.3.4-1)
 $50 \geq 2 \times 7.0 = 50 \geq 14.0$

OK

2.4 Compressive Stress: (REF. AASHTO 2007, ART. 14.7.5.3.2)

$$\begin{aligned}\text{Service Average Compressive Stress (Total Load), } \sigma_s &= P_T/A \\ &= 774000/87500 \\ &= 8.85 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{Service Average Compressive Stress (Live Load), } \sigma_L &= P_{LL}/A \\ &= 340/87500 \\ &= 0.004 \text{ MPa}\end{aligned}$$

$$\begin{aligned}\text{Rectangular Shape Factor, } S_i &= LW/2h_{ri} (L+W) \\ &\quad (\text{Ref. AASHTO 2007, Art. 14.7.5.1-1}) \\ &= 250 \times 350 / \{2 \times 10 \times (250+350)\} \\ &= 7.29\end{aligned}$$

$$\begin{aligned}\text{Shear Modulus of Elastomer, } G &= 0.9 \text{ MPa} \\ \text{Now, } 0.9 \leq G \leq 1.38 &\quad (\text{Ref. AASHTO 2007, Art. 14.7.5.2}) \\ &= 0.9 \leq 0.9 \leq 1.38\end{aligned}$$

OK

For Bearings Subject to Shear Deformation:

$$\begin{aligned}\sigma_s &\leq 1.66GS && (\text{Ref. AASHTO 2007, Art.14.7.5.3.2-1}) \\ &= 8.85 \leq 1.66 \times 0.9 \times 7.29 \\ &= 8.85 \leq 10.89\end{aligned}$$

OK

$$\begin{aligned}\text{Now, } \sigma_s &\leq 11 && (\text{Ref. AASHTO 2007, Art.14.7.5.3.2-1}) \\ &= 8.85 \leq 11\end{aligned}$$

OK

$$\begin{aligned}\text{Now, } \sigma_L &\leq 0.66GS && (\text{Ref. AASHTO 2007, Art.14.7.5.3.2-2}) \\ &= 0.004 \leq 0.66 \times 0.9 \times 7.29 \\ &= 0.004 \leq 4.33\end{aligned}$$

OK

2.5 Combined Compression and Rotation:

(REF. AASHTO 2007, ART. 14.7.5.3.5)

RECTANGULAR BEARINGS:

B = Length of Pad = 250 mm

Exterior Layer Allowance, $n_{ext} = 0$ (Ref. AASHTO 2007, Art. 14.7.5.2)

Equivalent Number of Interior Elastomeric Layers, $n = n_{\text{int}} + n_{\text{ext}}$
 $= 4.0 + 0 = 4.0$

$$\sigma_s > 1.0GS \left(\frac{\theta_s}{n} \right) \left(\frac{B}{h_{ri}} \right)^2 \quad (\text{Ref. AASHTO 2007, Art. 14.7.5.2})$$

$$= 8.85 > 1.0 \times 0.9 \times 7.29 \times (0.008/4) \times (250/10)^2$$

$$= 8.85 > 8.20$$

OK

Check shear deformation: (Ref. AASHTO 2007, Art. 14.7.5.3.5-2)

$$\sigma_s < 1.875GS \left[1 - 0.200 \left(\frac{\theta_s}{n} \right) \left(\frac{B}{h_{ri}} \right)^2 \right]$$

$$= 8.85 < 1.875 \times 0.9 \times 7.29 [1 - \{0.2 \times (0.008/4) \times (250/10)^2\}]$$

$$= 8.85 < 9.23$$

OK

2.6 Stability: (REF. AASHTO 2007, ART. 14.7.5.3.6)

For free horizontal translation: $2A \leq B$

$$A = \frac{1.92 \frac{h_{rt}}{L}}{\sqrt{1 + \frac{2L}{W}}} = 1.92 \times (50/250) / \sqrt{1 + (2 \times 250/350)} = 0.246$$

(Ref. AASHTO 2007, Art. 14.7.5.3.5-2)

$$2A = 2 \times 0.246 = 0.493$$

$$B = \frac{2.67}{(S + 2.0) \left(1 + \frac{L}{4.0W} \right)} = \frac{2.67}{[(7.29 + 2.0) \times \{1 + 250/(4.0 \times 350)\}]} = 0.244$$

(Ref. AASHTO 2007, Art. 14.7.5.3.5-3)

Now, $2A \leq B$
 $0.493 \leq 0.244$

NOT SATISFIED

As, this condition is not satisfied, the following equation is followed from AASHTO 2007.

Bridge Deck Free to Translate Horizontally:

$$\sigma_s \leq \frac{GS}{2A - B} \quad (\text{Ref. AASHTO 2007, Art. 14.7.5.3.6-4})$$

$$= 8.85 \leq 0.9 \times 7.29 / (0.493 - 0.244)$$

$$= 8.85 \leq 26.36 \text{ MPa}$$

OK**REINFORCEMENT:** (REF. AASHTO 2007, ART. 14.7.5.3.7)

Service Limit State:

Min. Yield Strength of Steel Reinforcement, $f_y = 250 \text{ MPa}$ Thickness of Steel Reinforcement = h_s

$$h_{s \min} = \frac{3.0 h_{\max} \sigma_s}{F_y} = 3.0 \times 10 \times 8.85 / 250 = 1.061 \text{ mm}$$

(Ref. AASHTO 2007, Art. 14.7.5.3.7-1)

Fatigue Limit State:

Constant Amplitude Fatigue Threshold = $\Delta F_{TH} = 165 \text{ MPa}$

$$h_{s \min} = \frac{2.0 h_{\max} \sigma_L}{\Delta F_{TH}} = 2 \times 0.004 \times 10 / 165 = 0.0005 \text{ mm}$$

(Ref. AASHTO 2007, Art. 14.7.5.3.7-2)

Required Minimum Reinforcement Thickness, $h_{s \min} = 1.061 \text{ mm}$ Reinforcement Thickness, $h_s = 3.0 \text{ mm}$ Now, $h_s \geq h_{s \min}$

$$= 3.0 \geq 1.061$$

OK**2.7 Final Design Summary:**

Bearing Width, W	= 350 mm
Bearing Length, L	= 250 mm
Elastomeric Layer Thickness, h_{ri}	= 10 mm
Thickness of top and Bottom cover Layers (each), h_{cover}	= 5.0 mm
Number of Interior Elastomeric Layers, n_{int} (Excluding Exterior Layer Allowance)	= 4
Total Elastomer Thickness, h_{rt}	= 50 mm
Reinforcement Thickness, h_s	= 3 mm
Total Bearing Thickness	= $h_{rt} + h_s(n_{int} + 1)$
	= $50 + (4 + 1) \times 3.0$
	= 65 mm

CHAPTER 3

SUBSTRUCTURE & FOUNDATION

3.0 STRUCTURAL DESIGN OF ABUTMENT-WING WALL AND PILE CAP

3.1 Model Details

3.1.1 General

STAAD.Pro 2006 has been used as a data processing tool for design purpose. Full view of 8.0m height abutment structural model is presented here along with load case details, pile reactions and node displacement summary reports. Detailed partial models of abutment wall and wing wall are described with plate no's, orientation of axis and stress distribution of plates by contour map and tabular forms. Node displacement summary from the STAAD.Pro analysis is attached with the rest of the report. AASHTO 07 codes have been followed for detailing of reinforcement for all the elements of substructure.

Abutment height 8.0m model with 30 piles and counterfort at wing wall with superstructure load of 25.0m (c/c bearing) is chosen for presenting the structural design example of Abutment-Wing wall and Pile Cap.

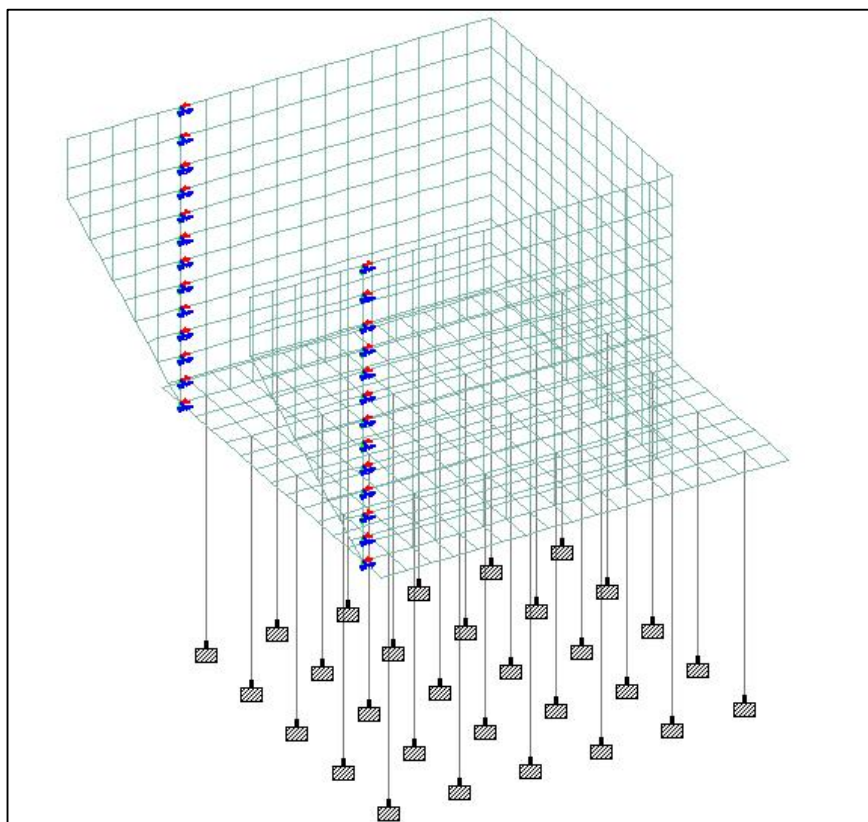


Fig 3.1 Full View of Substructure Model from STAAD.Pro

3.1.2 Load Case Details & Node Displacement Summary

Load case details with basic and combination cases and node displacement summary are provided in Appendix-“A” obtained from STAAD.Pro model.

3.1.3 Pile Reaction

Pile reactions at nodes of 30 piles are given below which are based on inelastic analysis and thus shows flexible distribution of pile reaction.

Table 3.1 Pile Reactions at Nodes for Service Load from STAAD.Pro Model

Node	F_Y , kN	Node	F_Y , kN
76	763.274	73	567.934
79	756.742	72	540.008
69	756.528	82	539.989
75	735.689	77	522.149
85	723.402	78	511.538
66	723.311	68	511.356
80	721.816	63	483.051
70	721.807	83	482.976
65	688.46	86	470.502
57	688.237	67	470.335
74	655.032	60	442.406
71	631.374	59	418.607
81	631.303	61	418.531
64	587.836	58	367.685
84	587.57	62	367.525

Elastic analysis of pile load distribution along with stability analysis is performed using Program DPM-EX. Different components of loading on substructure and foundation are calculated for vertical load calculation.

The following table provides vertical load calculations of the abutment. The following diagram is the reference drawing for the calculations following.

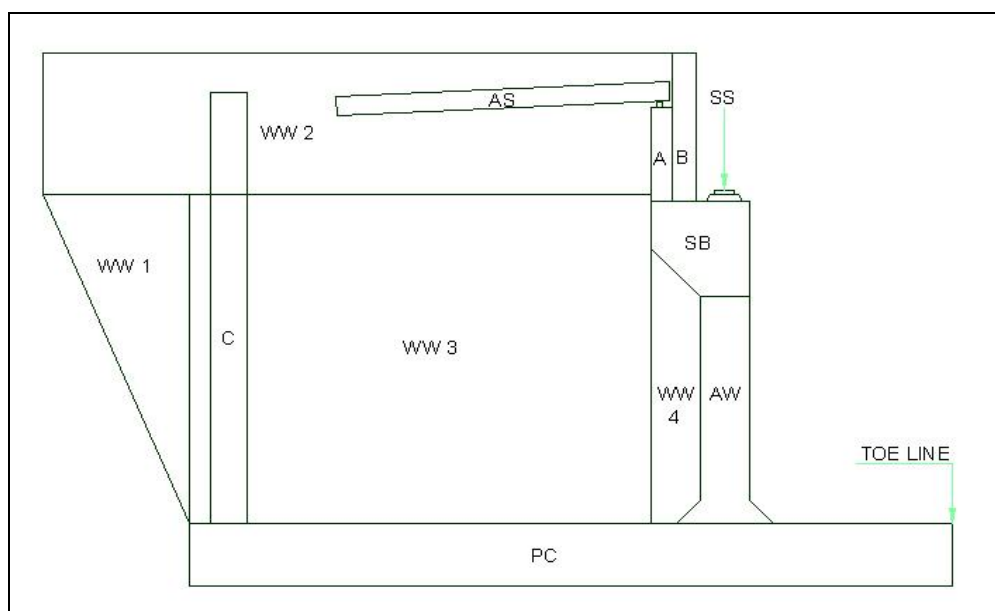


Fig 3.2 Wedges of Substructure for Calculation

Table: Vertical Load Calculation

Restoring Moment about Toe line		Volume (m ³)	Unit weight (KN/m ³)	Service Load (kN)	Lever Arm, m	Moment, kN-m
Wedge No	Name of Wedges					
AW	Abutment Wall	17.10	24.00	410.36	2.80	1149.00
SB	Seat Beam	11.89	24.00	285.47	3.10	884.94
B	Back Wall	5.33	24.00	127.86	3.30	421.95
A	Approach Slab Wall	2.48	24.00	59.47	3.58	212.61
AS	Approach Slab	8.26	24.00	198.24	5.58	1105.19
ASS	Approach Slab Support	0.05	24.00	1.12	3.58	3.99
WW1	Wing Wall, Region 1	5.41	24.00	129.74	11.15	1446.65
WW2	Wing Wall, Region 2	10.98	24.00	263.52	8.28	2180.63
WW3	Wing Wall, Region 3	27.98	24.00	671.62	7.00	4701.31
WW4	Wing Wall, Region 4	1.66	24.00	39.74	3.40	135.13
C	Counterfort	8.84	24.00	212.22	9.25	1963.04
PC	Pile Cap	118.66	24.00	2847.74	5.15	14665.88
S	Soil	430.85	18.00	7755.26	6.70	51960.27
SU	Surcharge	38.65	18.00	695.69	6.70	4661.14
SS	Superstructure			3100.00	2.83	8757.50
TOTAL			ΣV	16798	ΣM_R	85491.73

Calculation of Lateral Forces:

$$\text{Pressure due to Surcharge, } P1 = 0.61 \times 0.33 \times 18 = 3.62 \quad \text{kN/m}^2$$

$$\text{Pressure due to Soil, } P2 = 7.10 \times 0.33 \times 18 = 42.17 \quad \text{kN/m}^2$$

$$\text{Force due to Surcharge, } F1 = 7.10 \times 3.62 = 25.73 \quad \text{kN/m}$$

$$\text{Force due to Soil, } F2 = \frac{1}{2} \times 42.61 \times 7.10 = 149.72 \quad \text{kN/m}$$

$$\text{Total Force} = 25.73 + 149.72 = 175.44 \quad \text{kN/m}$$

$$\Sigma H = 175.44 \times 9.60 = 1684.26 \quad \text{kN}$$

Overturning moment, $\Sigma M_{OT} = M_{OT} \text{ due to soil} + M_{OT} \text{ due to surcharge}$

$$= 149.72 \times 9.60 \times 6.80/3 \times 1.5 + 25.73 \times 9.60 \times 6.80/2$$

$$= 6356.25 \text{ kN-m}$$

Pile Load/Reaction Calculation,

$$\text{C.G of Load, } x' = (\Sigma M_R - \Sigma M_{OT}) / \Sigma V = 4.71 \text{ m}$$

$$\text{C.G of Pile, } y' = (5 \times 0.65 + 5 \times 2.45 + 5 \times 4.25 + 5 \times 6.05 + 5 \times 7.85 + 5 \times 9.65) / 30 = 5.15 \text{ m } [N=30]$$

$$\text{Eccentricity, } e = y' - x' = 0.44 \text{ m}$$

$$\Sigma X^2 = [(X1)^2 \times 5 + (X2)^2 \times 5 + (X3)^2 \times 5] \times 2$$

$$= [(5.15 - 0.65)^2 \times 5 + (5.15 - 0.65 - 1.8)^2 \times 5 + (5.15 - 0.65 - 1.8 - 1.8)^2 \times 5] \times 2 = 283.5$$

m²

$$\text{Pile Load, } P = \Sigma V / \Sigma N \pm (\Sigma V \times e \times X) / \Sigma X^2$$

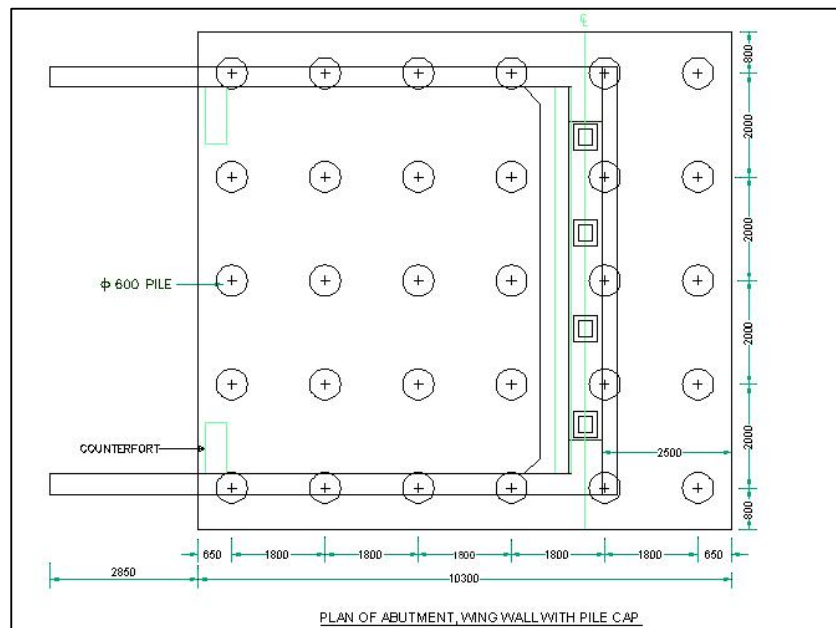


Fig 3.3 Plan of Abutment, Wing Wall with Pile Cap

At X1= 680 kN (row1 pile from toe line)

At X2= 630 kN (row2 pile from toe line)

At X3= 585 kN (row3 pile from toe line)

At X4= 536 kN (row4 pile from toe line)

At X5= 490 kN (row5 pile from toe line)

At X6= 445 kN (row6 pile from toe line)

3.2 Abutment Wall Design

304	868	869	870	871	872	873	874	875	876	877	878	303
460	857	858	859	860	861	862	863	864	865	866	867	897
308	846	847	848	849	850	851	852	853	854	855	856	545
437	835	836	837	838	839	840	841	842	843	844	845	674
425	824	825	826	827	828	829	830	831	832	833	834	662
413	813	814	815	816	817	818	819	820	821	822	823	650
401	802	803	804	805	806	807	808	809	810	811	812	638
389	791	792	793	794	795	796	797	798	799	800	801	626
377	780	781	782	783	784	785	786	787	788	789	790	614
365	769	770	771	772	773	774	775	776	777	778	779	602
353	758	759	760	761	762	763	764	765	766	767	768	590
341	747	748	749	750	751	752	753	754	755	756	757	578
55	298	284	49	260	246	46	222	208	39	184	170	36

Load 7

2079	2080	2081	2082	2083	2084	2085	2086	2087	2088	2089	2090
2067	2068	2069	2070	2071	2072	2073	2074	2075	2076	2077	2078
2055	2056	2057	2058	2059	2060	2061	2062	2063	2064	2065	2066
2043	2044	2045	2046	2047	2048	2049	2050	2051	2052	2053	2054
2031	2032	2033	2034	2035	2036	2037	2038	2039	2040	2041	2042
2019	2020	2021	2022	2023	2024	2025	2026	2027	2028	2029	2030
2007	2008	2009	2010	2011	2012	2013	2014	2015	2016	2017	2018
1995	1996	1997	1998	1999	2000	2001	2002	2003	2004	2005	2006
1983	1984	1985	1986	1987	1988	1989	1990	1991	1992	1993	1994
1971	1972	1973	1974	1975	1976	1977	1978	1979	1980	1981	1982
1959	1960	1961	1962	1963	1964	1965	1966	1967	1968	1969	1970
1947	1948	1949	1950	1951	1952	1953	1954	1955	1956	1957	1958

Load 7

Fig 3.4 Node no's of Abutment Wall

Fig 3.5 Plate no's of Abutment Wall

Abutment wall is designed considering plate properties with thickness 600mm. Plate and node no's of abutment wall are provided with the following figures. Moment contour map of plate according to plate orientations are also attached here. From the contour maps, higher concentration is found at the earth face or compression face.

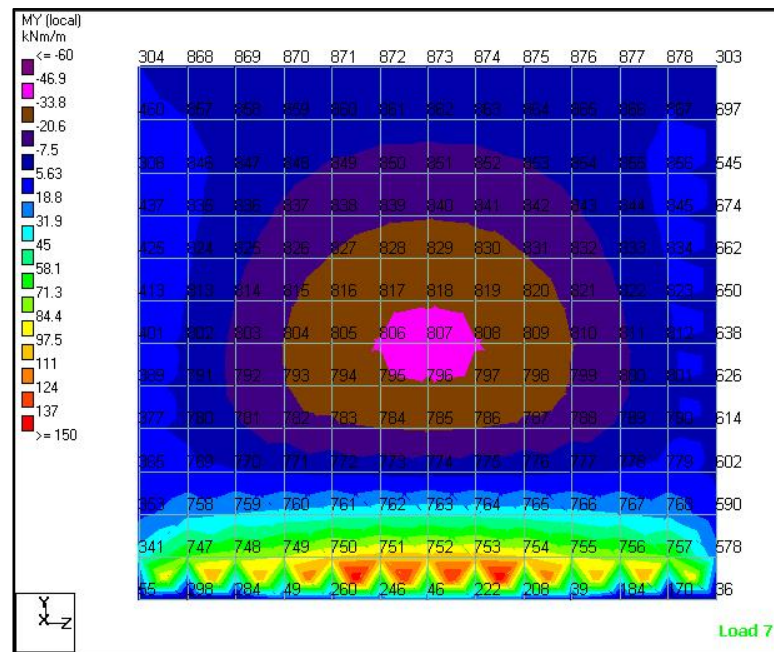


Fig 3.6 Bending Moment Contour of Abutment Wall (with node nos), M_y , kN-m

From the plate stress results, maximum flexural moment, M_y is found at plate no 1951 of value 146 kN-m/m along vertical direction which is found at the bottom section. With progression in height of 0.6m, certain change in moment is observed of value 65 kN-m/m. This value continues to decrease with increasing height of wing wall. For this reason, extra reinforcement is provided at the bottom only for design moment of 146 kN-m/m and for the full height of wing wall minimum reinforcement is provided following AASHTO 07 requirements. For water face or compression face, maximum moment 36 kN-m/m is considered for design reinforcement calculations and checked against minimum reinforcement requirements. The detailed calculations are provided below.

Reinforcement Design Calculation

Vertical Reinforcement For water face (W/F),

$$\text{Design Moment} = 36 \text{ kN-m/m}$$

$$\text{Compressive strength of Concrete, } f_c' = 20 \text{ MPa}$$

$$\text{Thickness of abutment wall} = 0.6 \text{ m}$$

$$\text{Modulus of Rupture} = 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa}$$

$$\text{Moment of Inertia} = b \times h^3 / 12 = 0.018 \text{ m}^4$$

$$\text{Cracking Moment} = 2.32 \times 1000 \times 0.018 / (0.6/2) = 140 \text{ kN-m/m}$$

Checking against AASHTO 07 criteria for minimum reinforcement,

$$\text{Criteria 1, } 1.2 \times \text{Cracking moment} = 167 \text{ kN-m/m}$$

$$\text{Criteria 2, } 1.33 \times \text{Flexural Moment} = 50 \text{ kN-m/m}$$

Minimum reinforcement required is for 50 kN-m/m which is greater than 36 kN-m/m. So, design moment finally considered is 50 kN-m/m.

R16-200 is provided for design moment of 50 kN-m/m. Checking against minimum surface reinforcement and design controlling moment, it is found that R16-250 is required. However, spacing of 200 mm is provided instead of 250 mm as spacing of main/horizontal reinforcement of top bar of pile cap required is 200 mm and thus, spacing of 200 mm is chosen for convenience of working condition.

Vertical Reinforcement For earth face (E/F),

$$\text{Design Moment} = 146 \text{ kN-m/m}$$

$$\text{Compressive strength of Concrete, } f_c' = 20 \text{ MPa}$$

$$\text{Thickness of Wing Wall} = 0.4 \text{ m}$$

$$\text{Modulus of Rupture} = 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa}$$

$$\text{Moment of Inertia} = b \times h^3 / 12 = 0.018 \text{ m}^4$$

$$\text{Cracking Moment} = 2.32 \times 1000 \times 0.018 / (0.6/2) = 140 \text{ kN-m/m}$$

Checking against AASHTO 07 criteria for minimum reinforcement,

$$\text{Criteria 1, } 1.2 \times \text{Cracking moment} = 167 \text{ kN-m/m}$$

$$\text{Criteria 2, } 1.33 \times \text{Flexural Moment} = 195 \text{ kN-m/m}$$

Minimum reinforcement required is for 195kN-m/m which is greater than 146 kN-m/m. So, design moment finally considered is 195 kN-m/m.

Reinforcement area required for 195 kN-m/m is 1450 mm^2 . For this reason, R16-200 and R16-200 are provided. Here, curtailment has been done for one R16-200 at 2500 mm distance from top of pile cap. Maximum moment 105 kN-m/m is found for distance of about 600 mm from top of pile cap (distance of plate). Extra Reinforcement is provided for $(600 + 40 \text{ times bar dia} + \text{Pile cap depth} - 175) \text{ mm} = 2500 \text{ mm}$. The other R16-200 has been continued for full height of wall.

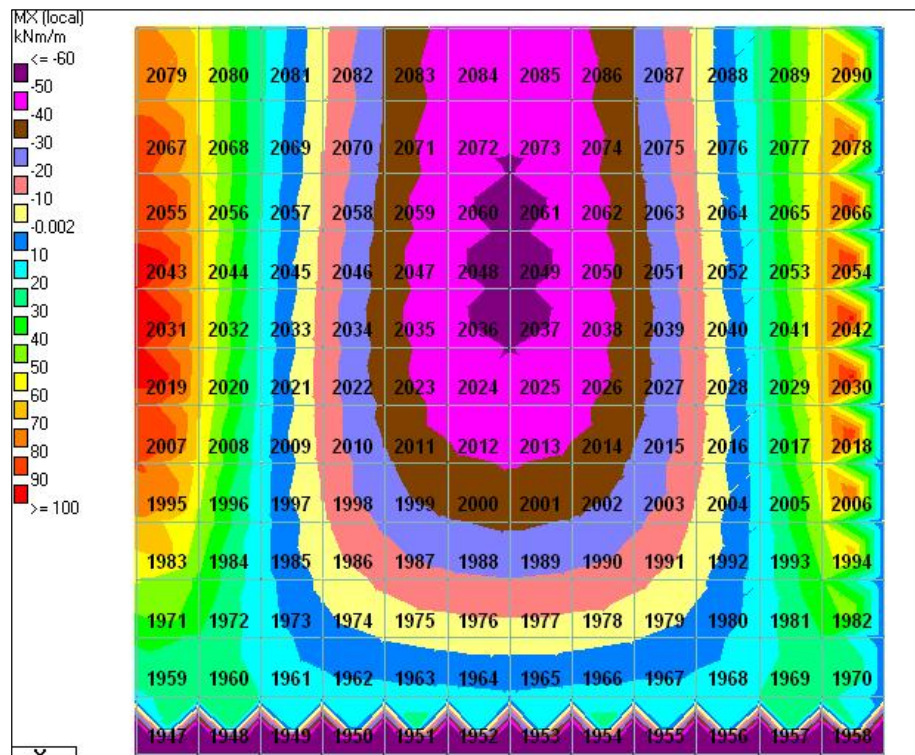


Fig 3.7 Bending Moment Contour of Abutment Wall (with plate nos), M_x , kN-m

It can be observed that maximum tensile stress is observed at plate no 2031 wherever, maximum compressive stress at plate no 2049. It is observed that tension face reinforcements are required near adjoining section between abutment wall and wing wall. Thus, extra reinforcements are provided near these two places and for the whole length minimum reinforcement is provided. Maximum compression face reinforcement is required for 59 kN-m/m.

The detailed calculations are provided below.

Reinforcement Design Calculation

Horizontal Reinforcement For water face (W/F),

Design Moment	= 59 kN-m/m
Compressive strength of Concrete, $f_c' = 20$ MPa	
Thickness of Wall	= 0.6 m
Modulus of Rupture	= $0.52 \times \sqrt{f_c'} = 2.32$ MPa
Moment of Inertia	= $b \times h^3 / 12 = 0.018 \text{ m}^4$
Cracking Moment	= $2.32 \times 1000 \times 0.018 / (0.6/2) = 140$ kN-m/m
Checking against AASHTO 07 criteria for minimum reinforcement,	
Criteria 1, $1.2 \times$ Cracking moment	= 168 kN-m/m
Criteria 2, $1.33 \times$ Flexural Moment	= 78.47 kN-m/m

Minimum reinforcement required is for 78.47 kN-m/m which is greater than 59 kN-m/m So, design moment finally considered is 78 kN-m/m. R16-200 is provided for design moment of 78 kN-m/m.

Horizontal Reinforcement For earth face (E/F),

Design Moment	= 100 kN-m/m
Compressive strength of Concrete, $f_c' = 20$ MPa	
Thickness of Wall	= 0.6 m
Modulus of Rupture	= $0.62 \times \sqrt{f_c'} = 2.32$ MPa
Moment of Inertia	= $b \times h^3 / 12 = 0.018 \text{ m}^4$
Cracking Moment	= $2.77 \times 1000 \times 0.018 / (0.6/2) = 140$ kN-m/m
Checking against AASHTO 07 criteria for minimum reinforcement,	
Criteria 1, $1.2 \times$ Cracking moment	= 168 kN-m/m
Criteria 2, $1.33 \times$ Flexural Moment	= 133 kN-m/m

Minimum reinforcement required is for 133 kN-m/m which is greater than 100 kN-m/m. So, design moment finally considered is 133 kN-m/m.

Reinforcement area required for 133 kN-m/m is 1000 mm^2 . For this calculation, R16-200 and R12-200 are provided. Here, 40 times bar diameter of length is considered in addition to the required length as curtailment length obtained from STAAD.PRO model. At the adjoining part of abutment wall and wing wall extra reinforcement of R12-200 is provided with the continuing reinforcement of R16-200 as, center stress results from STAAD.PRO shows lesser value of M_x for other plates in horizontal direction. So, T16-200 is continued for the total length of wall in horizontal direction.

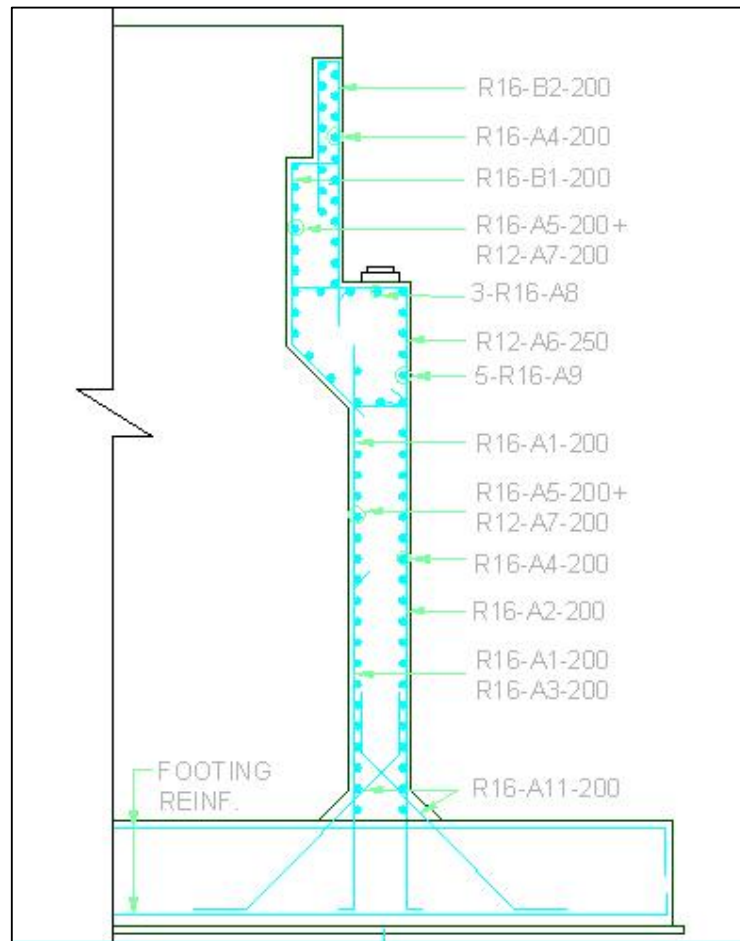


Fig 3.8 Reinforcement Details of Abutment Wall

3.3 Wing Wall Design

Wing wall is designed considering 400mm thickness. Plate and node no's of wing wall are provided with the following figures. Moment contour map of plate according to plate orientations are also attached here.

From the contour maps, higher concentration is found at the earth face or tension face. Detailed Moment according to plate no of a particular section for both x and y axis are attached here with reinforcement calculations and curtailment.

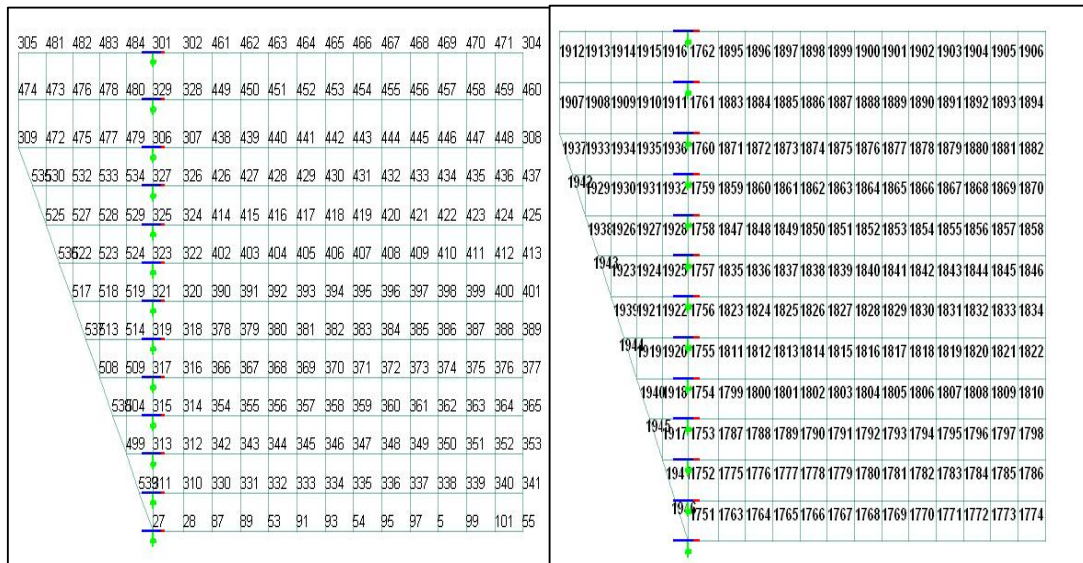
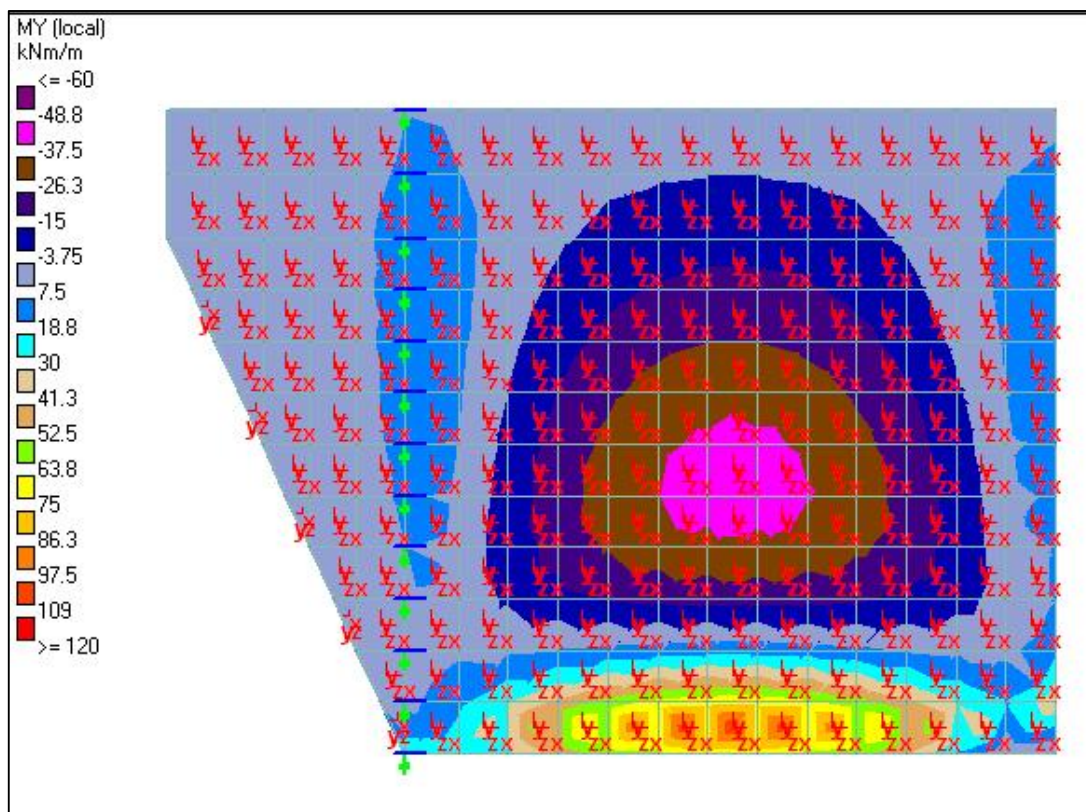


Fig 3.9 Node numbers and Plate numbers



of Wing Wall

Fig 3.10 Bending Moment Contour of Wing Wall, M_y , kN-m

Table: Bending Moment, M_y along section mid-section for Vertical Reinforcement Calculation

SL NO	PLATE NO(from downward to upward)	M_y (kN-m/m)
1	1781	-105
2	1780	-35
3	1792	-8
4	1804	+31
5	1816	+41
6	1828	+42
7	1840	+38
8	1852	+31
9	1864	+23
10	1876	+15
11	1888	+7
12	1900	+1

Here, +ve moment is for water face and –ve moment is for earth face.

It can be observed that maximum tensile stress is observed at plate no 1781 and maximum compressive stress at plate no 1828. Then again, the maximum value of tensile stress 105 kN-m/m is only found at the bottom section which continues to decrease with increasing height of wing wall. For this reason, extra reinforcement is provided at the bottom with design moment of 105 kN-m/m and for the full height of wing wall minimum reinforcement is provided following AASTO 07 requirements. For water face, maximum moment 42 kN-m/m is considered for design reinforcement calculations and checked against minimum reinforcement requirements. The detailed calculations are provided below.

Reinforcement Design Calculation

Vertical Reinforcement For water face (W/F),

Design Moment = 42 kN-m/m

Compressive strength of Concrete, $f_c' = 20$ MPa

Thickness of Wing Wall = 0.4 m

$$\begin{aligned}\text{Modulus of Rupture} &= 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa} \\ \text{Moment of Inertia} = b \times h^3/12 &= 0.00533 \text{ m}^4\end{aligned}$$

$$\text{Cracking Moment} = 2.32 \times 1000 \times 0.00533 / (0.4/2) = 62 \text{ kN-m/m}$$

Checking against AASHTO 07 criteria for minimum reinforcement,

$$\text{Criteria 1, } 1.2 \times \text{Cracking moment} = 75 \text{ kN-m/m}$$

$$\text{Criteria 2, } 1.33 \times \text{Flexural Moment} = 55.86 \text{ kN-m/m}$$

Minimum reinforcement required is for 55.86 kN-m/m which is greater than 42 kN-m/m So, design moment finally considered is 55.86 kN-m/m.

R16-250 is provided for design moment of 55.86 kN-m/m. Checking against minimum surface reinforcement and design controlling moment, it is found that R16-307 is required. However, spacing of 250 mm is provided instead of 307 mm as spacing of main/horizontal reinforcement of top bar of pile cap required is 250 mm and thus spacing of 250mm is chosen for convenience of working condition.

Vertical Reinforcement For earth face (E/F),

$$\text{Design Moment} = 105 \text{ kN-m/m}$$

$$\text{Compressive strength of Concrete, } f_c' = 20 \text{ MPa}$$

$$\text{Thickness of Wing Wall} = 0.4 \text{ m}$$

$$\begin{aligned}\text{Modulus of Rupture} &= 0.62 \times \sqrt{f_c'} = 2.32 \text{ MPa} \\ \text{Moment of Inertia} &= b \times h^3/12 = 0.00533 \text{ m}^4\end{aligned}$$

$$\text{Cracking Moment} = 2.32 \times 1000 \times 0.00533 / (0.4/2) = 62 \text{ kN-m/m}$$

Checking against AASHTO 07 criteria for minimum reinforcement,

$$\text{Criteria 1, } 1.2 \times \text{Cracking moment} = 75 \text{ kN-m/m}$$

$$\text{Criteria 2, } 1.33 \times \text{Flexural Moment} = 139.65 \text{ kN-m/m}$$

Minimum reinforcement required is for 75 kN-m/m which is less than 105 kN-m/m. So, design moment finally considered is 105 kN-m/m.

Reinforcement area required for 105 kN-m/m is 1250 mm². For this reason, R16-250 and R16-250 are provided. Here, curtailment has been done for one R16-150 at 2500mm distance. Extra Reinforcement is provided for 40 times bar diameter in addition to required length for moment concentration as obtained from STAAD.Pro analysis. R16-250 has been continued for the full height as requirement of minimum reinforcement from AASHTO 07.

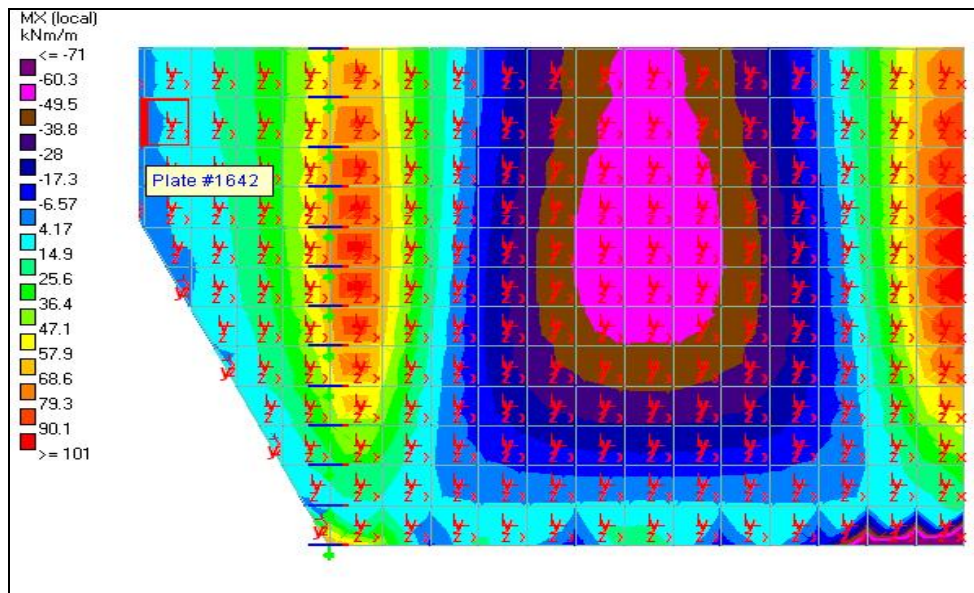


Fig 3.11 Bending Moment Contour of Wing Wall, M_x , kN-m

Table: Bending Moment, M_x along mid horizontal section for Horizontal Reinforcement Calculation

SL NO	PLATE NO	M_y (kN-m/m)	SL NO	PLATE NO	M_y (kN-m/m)
1	1926	-9.5	9	1851	+56
2	1927	-22	10	1852	+59
3	1928	-46	11	1853	+56
4	1758	-96	12	1854	+45
5	1847	-40	13	1855	+27
6	1848	-2	14	1856	-1.2
7	1849	+27	15	1857	-40
8	1850	+45	16	1858	-94

It can be observed that maximum tensile stress is observed at plate no 1754 and 1858 wherever, maximum compressive stress at plate no 1852. It is observed that tension face reinforcements are required near counterfort and support near abutment wall. Thus, extra reinforcements are provided near these two places and for the whole length minimum reinforcement is provided. Maximum compression face reinforcement is required for 59 kN-m/m.

R12-200 is provided as extra reinforcement near counterfort and abutment wall support. The detailed calculations are provided below.

Reinforcement Design Calculation

Horizontal Reinforcement For water face (W/F),

$$\begin{aligned}
 \text{Design Moment} &= 59 \text{ kN-m/m} \\
 \text{Compressive strength of Concrete, } f_c' &= 20 \text{ MPa} \\
 \text{Thickness of Wing Wall} &= 0.4 \text{ m} \\
 \text{Modulus of Rupture} &= 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa} \\
 \text{Moment of Inertia} &= b \times h^3 / 12 = 0.00533 \text{ m}^4 \\
 \\
 \text{Cracking Moment} &= 2.32 \times 1000 \times 0.00533 / (0.4/2) = 68 \text{ kN-m/m} \\
 \text{Checking against AASHTO 07 criteria for minimum reinforcement,} \\
 \text{Criteria 1, } 1.2 \times \text{Cracking moment} &= 75 \text{ kN-m/m} \\
 \text{Criteria 2, } 1.33 \times \text{Flexural Moment} &= 78.47 \text{ kN-m/m}
 \end{aligned}$$

Minimum reinforcement required is for 75 kN-m/m which is greater than 59kN-m/m. So, design moment finally considered is 75 kN-m/m. R16-200 is provided for design moment of 78 kN-m/m.

Horizontal Reinforcement For earth face (E/F),

$$\begin{aligned}
 \text{Design Moment} &= 105 \text{ kN-m/m} \\
 \text{Compressive strength of Concrete, } f_c' &= 20 \text{ MPa} \\
 \text{Thickness of Wing Wall} &= 0.4 \text{ m} \\
 \text{Modulus of Rupture} &= 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa} \\
 \text{Moment of Inertia} &= b \times h^3 / 12 = 0.00533 \text{ m}^4 \\
 \\
 \text{Cracking Moment} &= 2.32 \times 1000 \times 0.00533 / (0.4/2) = 68 \text{ kN-m/m} \\
 \text{Checking against AASHTO 07 criteria for minimum reinforcement,} \\
 \text{Criteria 1, } 1.2 \times \text{Cracking moment} &= 75 \text{ kN-m/m} \\
 \text{Criteria 2, } 1.33 \times \text{Flexural Moment} &= 139.65 \text{ kN-m/m}
 \end{aligned}$$

Minimum reinforcement required is for 75 kN-m/m which is less than 105 kN-m/m. So, design moment finally considered is 105 kN-m/m.

Reinforcement area required for 105 kN-m/m is 1250mm^2 . For this reason, R16-200 and R12-200 are provided near counterfort for length of 2500 mm. Here, 40 times bar diameter of length is considered in addition to the required length obtained from STAAD.PRO model. At the adjoining part of abutment wall and wing wall extra reinforcement of R12-200 is provided with the continuing reinforcement of T16-200 as, center stress results from STAAD.PRO shows lesser value of M_x for other plates in horizontal direction. 40 times bar diameter equivalent to 500 mm is considered in calculating curtailment length in addition to required length obtained from STAAD.Pro analysis. So, R16-200 is continued for the total length of wing wall in horizontal direction.

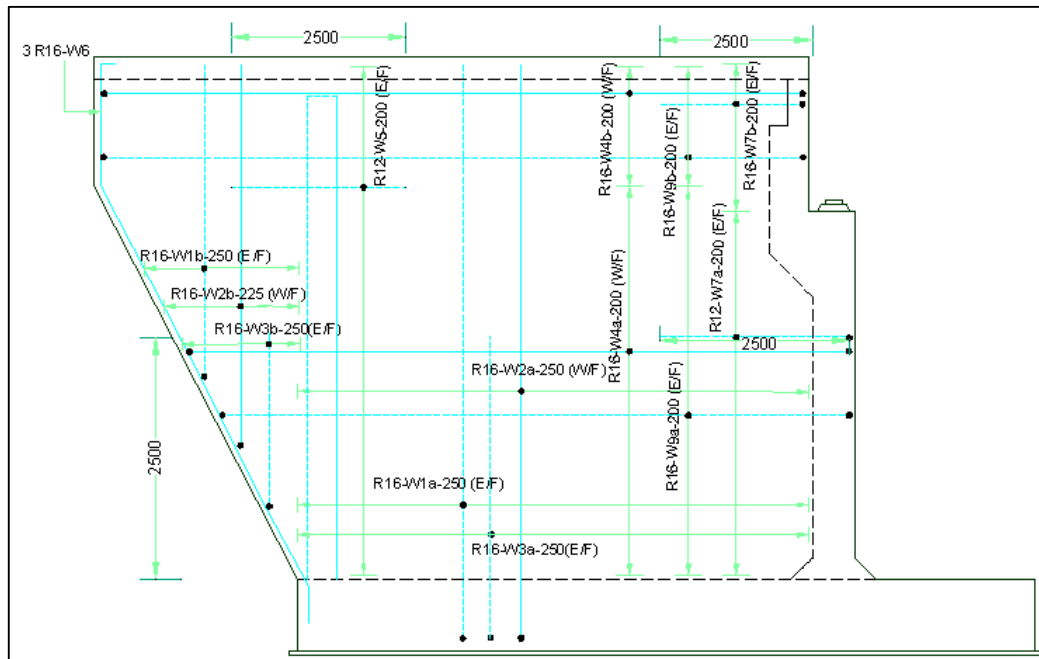


Fig 3.12 Reinforcement Details of Wing Wall

3.4 Pile Cap Design

Pile cap is designed considering plate properties with thickness varying from 700mm to 1000mm Plate and node no's of pile cap are provided with the following figures. Moment contour map of plate according to plate orientations are also attached here.

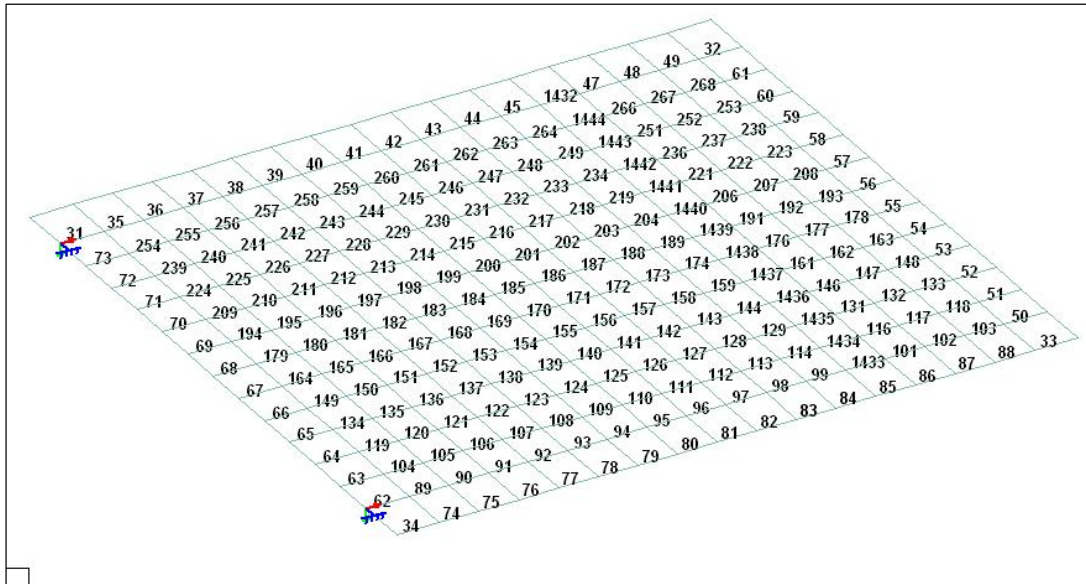


Fig 3.13 Plate Numbers of Pile Cap from STAAD.Pro Model

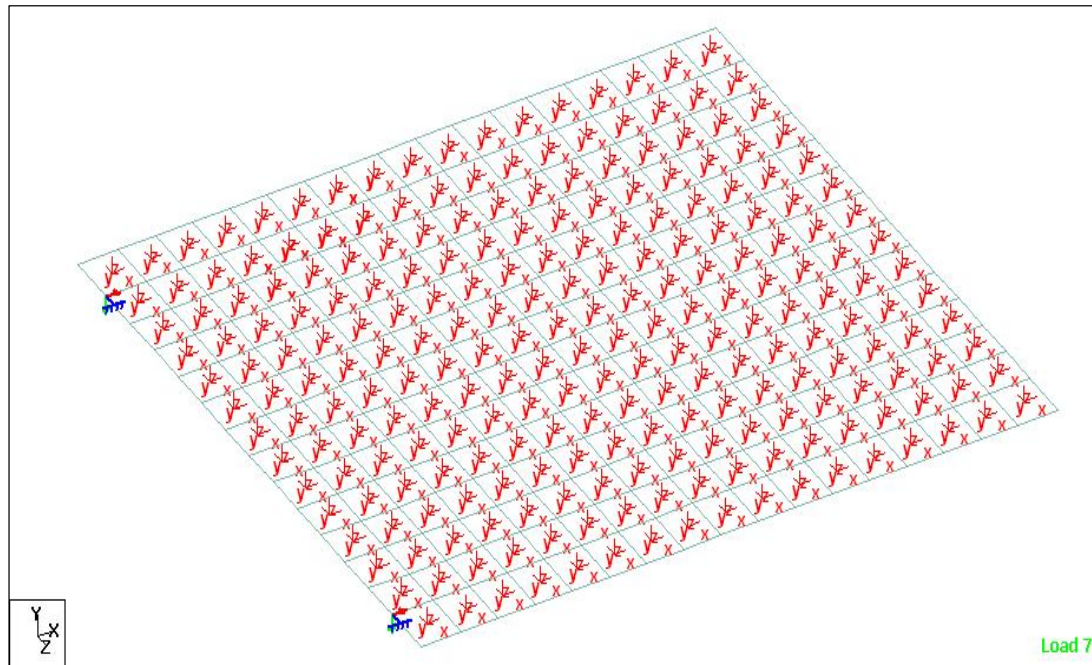


Fig 3.14 Axis Orientation of Pile Cap from STAAD.Pro Model

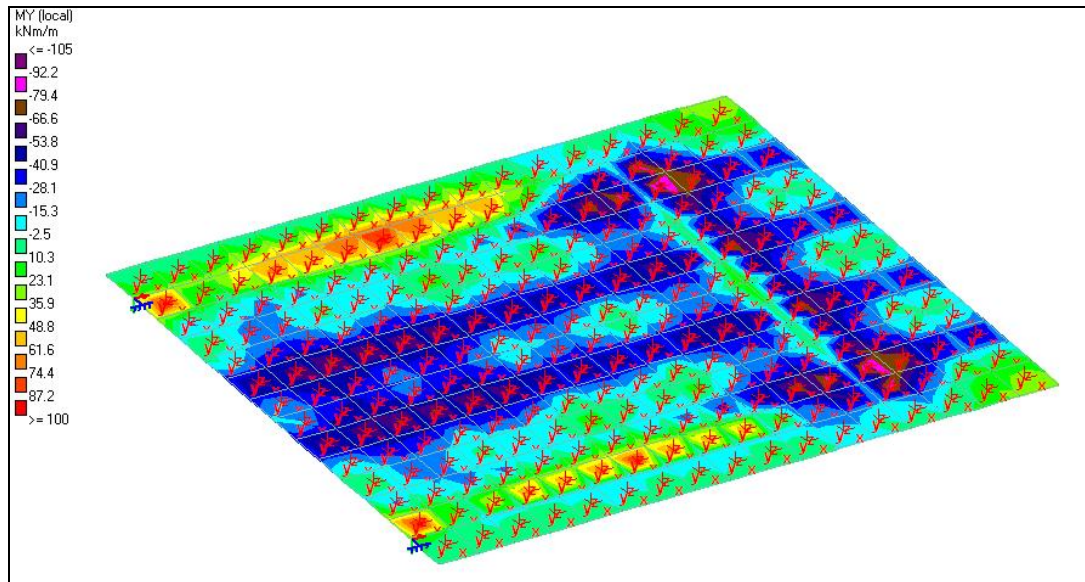


Fig 3.15 Bending Moment Contour along Y axis, M_y of Pile Cap

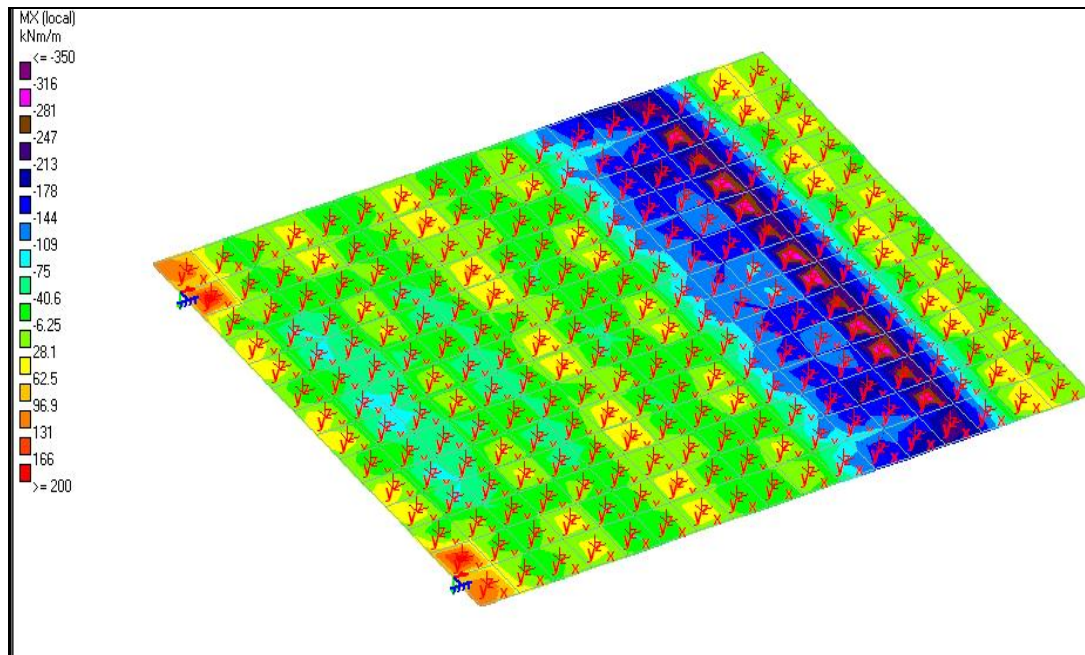


Fig 3.16 Bending Moment Contour along X axis, M_x of Pile Cap

Reinforcement Design along Traffic Direction

Bottom Face

Bending Moment Calculation considering abutment wall as fixed support for abutment height of 8.0m is done to check moment along x axis obtained from STAAD.Pro. Toe side moment for direction along traffic is calculated as follows:

$$M_{LL} = (1.5 \times 680) \times 1.85 / 1.55 + (1.5 \times 630) \times 0.05 / 1.55$$

$$= 1250 \text{ kN-m/m}$$

$$M_{DL} = 0.9 \times 24 \times 1.2 \times 2.5^2 / 2$$

$$= 81 \text{ kN-m/m}$$

$$\text{Design Moment} = 1250 - 81 = 1170 \text{ kN-m/m}$$

Maximum bending moment M_x from STAAD.PRO is 315 kN-m/m as observed from Moment contour, which is less than moment obtained from manual calculation. As, tension face reinforcement is critical, thus, this pile cap is designed for toe side bottom face reinforcement along traffic direction with design moment of 1170 kN-m/m.

Reinforcement Design

$$\text{Design Moment} = 1170 \text{ kN-m/m}$$

$$\text{Compressive strength of Concrete, } f_c' = 20 \text{ MPa}$$

$$\text{Thickness of Pile Cap} = 1.2 \text{ m}$$

$$\text{Modulus of Rupture} = 0.52 \times \sqrt{f_c'} = 2.32 \text{ MPa}$$

$$\text{Moment of Inertia} = b \times h^3 / 12 = 1000 \times 1.2^3 / 12 = 0.144 \text{ m}^4$$

$$\text{Cracking Moment} = 2.32 \times 1000 \times 0.144 / (1.2/2) = 558 \text{ kN-m/m}$$

Checking against AASHTO 07 criteria for minimum reinforcement,

$$\text{Criteria 1, } 1.2 \times \text{Cracking moment} = 670 \text{ kN-m/m}$$

$$\text{Criteria 2, } 1.33 \times \text{Flexural Moment} = 1556 \text{ kN-m/m}$$

So, minimum reinforcement required is for 798.55 kN-m/m which is less than design moment 1170 kN-m/m. So, design moment finally considered is 1170 kN-m/m.

R16-150 and R25-150 is provided for design moment of 1170 kN-m/m as bottom reinforcement for the cantilever section which has been curtailed at the distance of 4025 mm from toe side. $25 \times 40 + 300$ (distance from c/l of abutment wall) = 1300 mm. Distance of pile cap edge and abutment wall c/l is 2800 mm. So, $(2800 - 75) = 2725$ mm of reinforcement is provided at the right side. So, extra reinforcement of R25-150 is curtailed at the distance of $(1300 + 2725) = 4025$ mm from the toe side.

Top Face

Maximum moment at the compression face is 200 kN-m/m which requires R16 bar at 250 mm spacing. Again, vertical reinforcement of wing wall is R16-250 and thus R16-250 is provided as main reinforcement at top face of pile cap.

Reinforcement Design perpendicular to Traffic Direction

Bottom face

Flexural moment of 105kN-m/m is found at the bottom face observed from STAAD.PRO moment contour. Thus, according to previous calculation R16-250 is provided as bottom face y direction reinforcement.

Top face

Flexural moment of 100 kN-m/m is found at the top face observed from STAAD.PRO moment contour. Checking against vertical reinforcement of abutment wall thus, R16-250 is provided as top face y direction reinforcement.

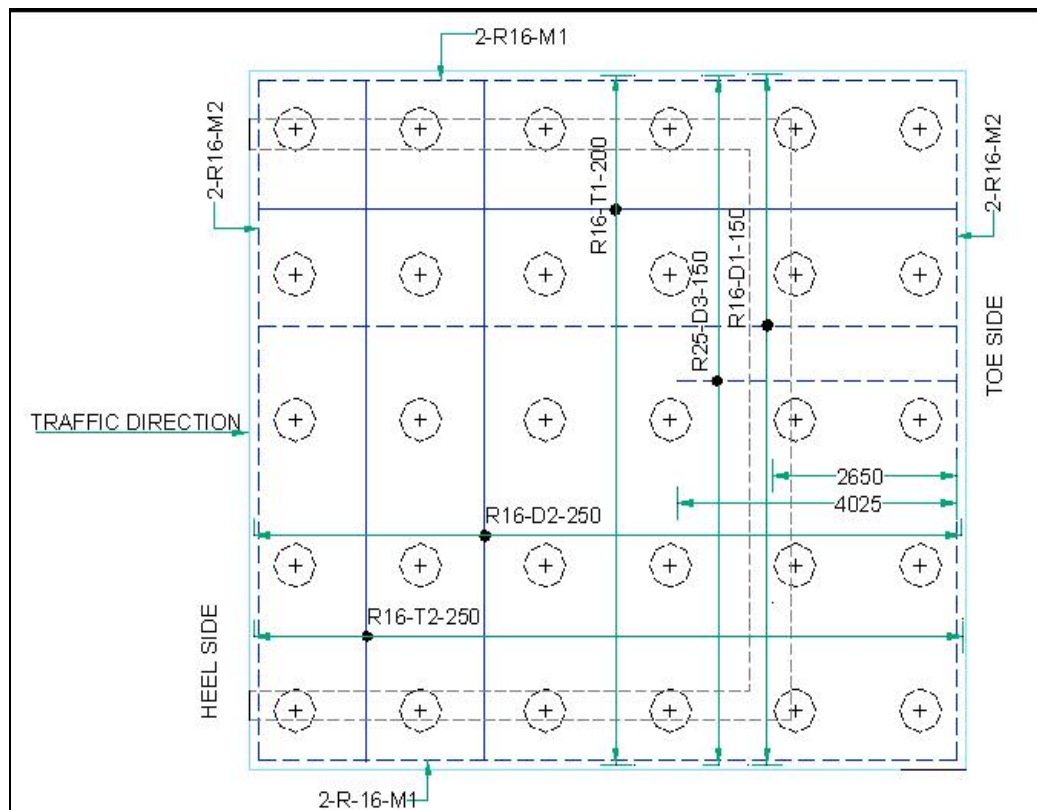


Fig 3.17 Pile Cap Reinforcement Details

3.5 Structural Design of Pile

Material Properties

Concrete Cylinder Strength at 28 Days, $f_c = 25 \text{ MPa}$
 Yield Strength of reinforcing steel, $f_y = 400 \text{ MPa}$

General Data

Unit Weight of Soil, $\gamma = 18 \text{ kN/m}^3$
 Maximum Horizontal Load in Pile (factored), $P_x = 70.1 \text{ kN}$
 Maximum Axial Load in Pile (factored), $P_y = 713 \text{ kN}$

Moment Applied at the Pile Head (factored), $M_T = 0 \text{ kN-m}$
 Coefficient. of Subgrade Modulus, $n_h = 700 \text{ kN/m}^3$
 Pile Diameter $D = 0.6 \text{ m}$
 Modulus of Elasticity, $E = 24000000 \text{ kN-m}^2$

Soil Data

Soil	$n_h \text{ (kN/m}^3\text{)}$
Medium Dense Soil	2500
Stiff Clay	1500
Soft Clay	700
Very Soft Clay	350
Organic Silt	150

NB: For loose submerged cohesion less soil $n_h = 1400 \text{ kN/m}^3$
 Allowable Compressive Stress in pile $= 6.25 \text{ N/mm}^2$ (W. C. Teng, 1962)
 (Considering Structural Strength of Pile only)

Proposed Reinforcement:

No. of Bar	20
Bar Diameter	25mm
Clear Cover	75mm

Analysis:

Axial Stress on Pile, $\sigma_x = 2.53 \text{ N/mm}^2$
 Allowable stress of Pile, $\sigma_{\text{allowable}} = 6.25 \text{ N/mm}^2$

Here, the allowable compressive stress is greater than applied stress. So the lateral restraint required to prevent pile buckling will be very small. There is no need to check the buckling capacity.

No of Longitudinal bar, $n = 16$
 Total Steel Provided, $A_s = n \times \text{Area of Rebar} = 5024 \text{ mm}^2$
 Gross Area of Concrete, $A_g = 3.14 \times (D^2)/4 = 282600 \text{ mm}^2$
 % Steel provided $= A_s/A_g = 1.77$
 For the Circular pile:
 Moment of Inertia, $I = 3.14 \times (D^4)/64 = 3.14 \times (0.6^4)/64 = 0.006 \text{ m}^4$
 Stiffness Factor, $T = (EI/\eta_h)^{0.2} = 2.936 \text{ m}$
 Minimum Length of pile, $L = 4 \times T = 12 \text{ m}$
 Level of Fixity, $L' = 1.8 \times T = 5.29 \text{ m}$

From Reese and Matlock ^(6.13) Graph:
 Bending Moment Coefficient. $A_m = 0.8$
 Bending Moment Coefficient. $B_m = 1.0$
 Bending moment, $M = A_m \times P_x \times T + B_m \times M_T = 164.6 \text{ kN-m}$

Input for PCA COL:

Level of fixity, $L' = 5.29\text{m}$

Axial Load, $P = 713\text{ kN}$ (Factored Load)

Moment, $M = 164.63\text{ kN-m}$ (Factored Moment)


Notes: - *Supporting strength of soil is not considered in evaluating the Capacity of Single Pile*

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3.6 Geotechnical Design of Pile

AASHTO 4.6.5.1 Geotechnical Design				Project : RSM JICA				Date : 18/11/2008			
Bore Hole No.	1	Bore Hole Level	1.500 m	Unit Weight of Soil	18.00 kN/m ³	No. of Piles in X direction	3 nos.				
Pile Size	0.60 m	Ground Water Level	4.000 m	Unit Weight of Concrete	24.00 kN/m ³	No. of Piles in Y direction	5 nos.				
Pile Spacing	1.8 m	Scour Level/Liquefaction zone	1.000 m			Total no. of Piles	15 nos.				
		Pilecap Bottom Level	1.000 m			Overall Width, X (m)	4.2 m				
Factor of Safety against :		Interval of SPT	1.50 m			Overall Length, Y (m)	7.8 m				
Side Resistance	2.5					Perimeter of pile group	24 m				
End Bearing	2.5					Area of pile group	32.76 m ²				
						Reduction factor for group action	0.67				

Depth below Liquefac. Level	SPT N	Soil Code #	Soil Density / Consistency	Cor. SPT (N ₇₀)	Lab S _u (MPa)	S _u for Analysis (MPa)	Adhesion Factor α	Effective Vertical Stress σ' _v = γ' z _i	Bearing Capacity Factor No(ind.)	Load Transfer Fractor β _i	Ultimate unit side (MPa)	Ultimate Friction at Depth (kN)	Ultimate End Bearing (kN)	Allowable Pile Capacity (kN)	Bearing Capacity Factor Nc(Gr.)	Ult. Group Side Friction (kN)	Ult. Group End Bearing (kN)	Ultimate Group Capacity (kN)	Allowable Group Capacity (kN)	Depth below Pile cap (m)
								0.00												
1.5	1	0	Very Soft Silty/Clay	1	0.01	0.40	8.000	9.00			0.003	7	17	6	5.80	75.06	169	243.9	86	1.0
3.0	1	0	Very Soft Silty/Clay	1	0.01	0.40	20.000	9.00			0.003	15	17	3	6.20	150.12	169	319.0	116	2.5
4.5	3	0	Very Soft Silty/Clay	3	0.02	0.40	32.000	9.00			0.008	37	50	19	6.59	375.30	507	882.0	319	4.0
6.0	12	1	Medium Dense Sand	12	0.00	0.00	44.000		0.94		0.041	154	193	117	NA	1488.81	1944	3432.4	1243	5.5
7.5	12	1	Medium Dense Sand	12	0.00	0.00	56.000		0.86		0.048	291	193	166	NA	1743.67	1944	3687.3	1345	7.0
9.0	20	1	Medium Dense Sand	18	0.00	0.00	68.000		0.80		0.054	445	322	273	NA	1953.23	3239	5192.6	1861	8.5
10.5	21	1	Medium Dense Sand	18	0.00	0.00	80.000		0.74		0.059	611	338	340	NA	2121.76	3401	5523.1	1982	10.0
12.0	27	1	Medium Dense Sand	21	0.00	0.00	92.000		0.68		0.063	788	435	444	NA	2252.52	4373	6625.7	2359	11.5
13.5	50	1	Dense Sand	33	0.00	0.00	104.000		0.63		0.065	973	806	660	NA	2348.09	8098	10446.6	3639	13.0
15.0	50	1	Dense Sand	33	0.00	0.00	116.000		0.58		0.067	1162	806	730	NA	2410.57	8098	10509.0	3664	14.5
16.5	50	1	Dense Sand	33	0.00	0.00	128.000		0.53		0.068	1354	806	800	NA	2441.75	8098	10540.2	3676	16.0
18.0	50	1	Dense Sand	33	0.00	0.00	140.000		0.48		0.068	1546	806	871	NA	2443.13	8098	10541.6	3677	17.5
19.5	50	1	Dense Sand	33	0.00	0.00	152.000		0.44		0.067	1735	806	941	NA	2416.03	8098	10514.5	3666	19.0
21.0	50	1	Dense Sand	33	0.00	0.00	164.000		0.40		0.066	1921	806	1010	NA	2361.61	8098	10460.1	3644	20.5
22.5	50	1	Dense Sand	33	0.00	0.00	176.000		0.36		0.063	2100	806	1075	NA	2280.89	8098	10379.4	3612	22.0
24.0	50	1	Dense Sand	33	0.00	0.00	188.000		0.32		0.060	2271	806	1138	NA	2174.78	8098	10273.3	3569	23.5
25.5	50	1	Dense Sand	33	0.00	0.00	200.000		0.28		0.057	2431	806	1196	NA	2044.12	8098	10142.6	3517	25.0
27.0	50	1	Dense Sand	33	0.00	0.00	212.000		0.25		0.053	2581	806	1250	NA	1908.00	8098	10006.5	3463	26.5
28.5	50	1	Dense Sand	33	0.00	0.00	224.000		0.25		0.056	2740	806	1307	NA	2016.00	8098	10114.5	3506	28.0
30.0	50	1	Dense Sand	33	0.00	0.00	236.000		0.25		0.059	2906	806	1368	NA	2124.00	8098	10222.5	3549	29.5

	Job No	Sheet No	Rev
	APPENDIX-"A"		1
Software licensed to DPM Consultants Ltd.		Part	
Job Title Double Lane Bridge Manual		Ref	
Client LGED-JICA		By	Date 16-11-08 Cnd
		File ABUT 8.0 m COUNTER.s	Date/Time 16-Nov-2008 12:59

Job Information

	Engineer	Checked	Approved
Name:			
Date:	16-11-08		

Structure Type	SPACE FRAME
----------------	-------------

Number of Nodes	848	Highest Node	878
Number of Elements	30	Highest Beam	30
Number of Plates	774	Highest Plate	2090

Number of Basic Load Cases	7
Number of Combination Load Cases	2

Included in this printout are data for:


All	The Whole Structure
-----	---------------------

Included in this printout are results for load cases:

Type	L/C	Name
Primary	1	DEAD LOAD
Primary	2	SUPERSTRUCTURE DL
Primary	5	V E P ON PILE CAP
Primary	3	H E P ON WINGWALL 1
Primary	4	H E P ON WINGWALL 2
Primary	8	H E P ON ABUTMENTWALL
Primary	9	SUPERSTRUCTURE LL
Combination	6	COMBINATION SERVICE
Combination	7	COMBINATION FACTORED

Basic Load Cases

Number	Name
1	DEAD LOAD
2	SUPERSTRUCTURE DL
5	V E P ON PILE CAP
3	H E P ON WINGWALL 1
4	H E P ON WINGWALL 2
8	H E P ON ABUTMENTWALL
9	SUPERSTRUCTURE LL

	Job No APPENDIX-"A"	Sheet No 2	Rev
	Part		
Job Title Double Lane Bridge Manual		Ref	
By		Date 16-11-08	Cnd
Client LGED-JICA	File ABUT 8.0 m COUNTER.s	Date/Time 16-Nov-2008 12:59	

Combination Load Cases

Comb.	Combination L/C Name	Primary	Primary L/C Name	Factor
6	COMBINATION SERVICE	1	DEAD LOAD	1.00
		2	SUPERSTRUCTURE DL	1.00
		5	V E P ON PILE CAP	1.00
		3	H E P ON WINGWALL 1	1.00
		4	H E P ON WINGWALL 2	1.00
		8	H E P ON ABUTMENTWALL	1.00
7	COMBINATION FACTORED	9	SUPERSTRUCTURE LL	1.00
		1	DEAD LOAD	1.25
		2	SUPERSTRUCTURE DL	1.25
		5	V E P ON PILE CAP	1.35
		3	H E P ON WINGWALL 1	1.50
		4	H E P ON WINGWALL 2	1.50
		8	H E P ON ABUTMENTWALL	1.50
		9	SUPERSTRUCTURE LL	1.75

Node Displacement Summary

	Node	L/C	X (mm)	Y (mm)	Z (mm)	Resultant (mm)	rX (rad)	rY (rad)	rZ (rad)
Max X	873	7:COMBINATI	12.404	-1.342	0.002	12.477	-0.000	0.000	-0.000
Min X	1	3:H E P ON WI	-2.191	-0.012	0.032	2.191	-0.000	0.000	-0.000
Max Y	309	8:H E P ON AE	7.715	0.330	-0.000	7.722	-0.000	-0.000	0.000
Min Y	841	7:COMBINATI	12.171	-1.375	0.007	12.248	0.000	-0.000	-0.000
Max Z	11	4:H E P ON WI	0.898	0.018	4.656	4.742	0.000	-0.000	-0.000
Min Z	13	3:H E P ON WI	0.898	0.018	-4.656	4.742	-0.000	0.000	-0.000
Max rX	584	7:COMBINATI	11.165	-0.785	0.617	11.210	0.001	0.000	-0.000
Min rX	347	7:COMBINATI	11.165	-0.785	-0.617	11.210	-0.001	-0.000	-0.000
Max rY	416	3:H E P ON WI	-1.740	-0.037	-1.762	2.477	0.000	0.001	-0.000
Min rY	653	4:H E P ON WI	-1.740	-0.037	1.762	2.477	-0.000	-0.001	-0.000
Max rZ	16	7:COMBINATI	11.051	-0.636	0.006	11.070	-0.000	-0.000	0.000
Min rZ	774	8:H E P ON AE	7.942	-0.068	-0.000	7.943	-0.000	0.000	-0.000
Max Rst	873	7:COMBINATI	12.404	-1.342	0.002	12.477	-0.000	0.000	-0.000

RSM'08


	Job No APPENDIX-"A"	Sheet No 3	Rev
	Part		
Job Title Double Lane Bridge Manual		Ref	
By		Date 16-11-08	Chd
Client LGED-JICA	File ABUT 8.0 m COUNTER	Date/Time 16-Nov-2008 12:59	

Plate Centre Stress Summary

	Plate	L/C	Shear		Membrane			Bending		
			Qx (N/mm ²)	Qy (N/mm ²)	Sx (N/mm ²)	Sy (N/mm ²)	Sxy (N/mm ²)	Mx (kNm/m)	My (kNm/m)	Mxy (kNm/m)
Max Qx	1751	4:H E P ON WI	0.945	-0.338	0.012	0.076	0.031	-74.125	-6.056	-5.728
Min Qx	1456	3:H E P ON WI	-0.945	0.338	0.012	0.076	0.031	74.125	6.056	5.728
Max Qy	1768	7:COMBINATI	-0.002	0.376	0.011	-0.384	0.301	-14.955	-105.029	-0.430
Min Qy	1491	7:COMBINATI	0.002	-0.376	0.011	-0.383	0.302	14.958	105.033	0.428
Max Sx	1946	7:COMBINATI	-0.000	0.023	0.386	0.004	0.011	-0.136	-0.800	-0.198
Min Sx	1498	7:COMBINATI	-0.052	-0.051	-0.387	-1.591	0.596	8.088	21.994	-5.944
Max Sy	2065	7:COMBINATI	0.110	0.004	0.228	0.220	0.448	38.507	4.026	1.991
Min Sy	1947	7:COMBINATI	0.060	-0.214	-0.295	-1.810	-0.362	20.430	92.219	-7.258
Max Sxy	1774	7:COMBINATI	0.052	0.051	-0.387	-1.591	0.599	-8.082	-21.954	5.946
Min Sxy	2047	7:COMBINATI	-0.036	0.019	0.040	-1.332	-0.528	-43.570	-21.291	1.102
Max Mx	62	7:COMBINATI	-0.025	-0.240	-0.044	-0.070	-0.041	186.815	91.471	64.312
Min Mx	191	7:COMBINATI	0.245	-0.140	-0.050	0.097	0.023	-336.994	-54.191	-32.271
Max My	1951	7:COMBINATI	0.022	-0.286	-0.008	-0.708	-0.066	24.307	146.042	4.504
Min My	1768	7:COMBINATI	-0.002	0.376	0.011	-0.384	0.301	-14.955	-105.029	-0.430
Max Mxy	62	7:COMBINATI	-0.025	-0.240	-0.044	-0.070	-0.041	186.815	91.471	64.312
Min Mxy	73	7:COMBINATI	-0.024	0.239	-0.044	-0.070	0.041	186.637	91.352	-64.242

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STAAD.Pro for Windows Release 2006

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CHAPTER 4

BOX CULVERT

4.0 Structural Design of Box culvert

4.1 Model Details

4.1.1 General

STAAD.Pro 2006 has been used as a data processing tool for design purpose. Sectional view of 1 vent box culvert of box size 4.0m x 4.0m structural model is presented here along with load case details and node displacement summary reports. Node displacement summary from the STAAD.Pro analysis is attached with the rest of the report. AASHTO 07 codes have been followed for detailing of reinforcement for all the elements of box culvert.

Specific type of foundation is not required for box culvert type structure. It is placed over one layer of plain concrete under lying one layer of sand cushion. 1.0 m width of strip is analyzed which is supported by vertical spring with value of 400 kN/m. Spring support is used to represent properties of soil where allowable bearing capacity is 80kN/m² considering normally consolidated clay/lower bound medium dense sand. Springs are provided at every 0.36 m.

4.1.2 Calculations for Equivalent Strip Width and Loading

Equivalent strip width has been calculated using the following formula from AASHTO 07 Table 4.6.2.1.3-1

$$660 + 0.55 \times S = 2860 \text{ mm} = 2.86 \text{ m}$$

Where, S = Spacing of supporting components = 4000 mm

Considering HL-97 live loading, only rear axle load of truck of 145kN is placed as truck load.

$$\text{Truck load} = 145/2.86 = 50.7 \text{ kN}$$

$$\text{Lane Load} = 9.3/3 = 3.1 \text{ kN/m} \quad [\text{Lane load} = 9.3 \text{ kN/m}]$$

Ref: AASHTO 07 Art
No3.6.1.2.4]

$$\text{Earth Pressure on vertical walls} = 0.4 \times 18 \times 4 = 28.8 \text{ kN/m}^2$$

[Co-efficient is chosen for cases in between active and at rest earth pressure]

$$\text{Surcharge Pressure on vertical walls} = 0.4 \times 18 \times 0.61 = 4.39 \text{ kN/m}^2$$

[Co-efficient is chosen for cases in between active and at rest earth pressure]

Load for Wearing course $= 50/1000 \times 23 = 1.15 \text{ kN/m}^2$ [Unit of weight of Wearing Course $= 23 \text{ kN/m}^3$]

Self weight and wearing course are applied as different load cases for this analysis.

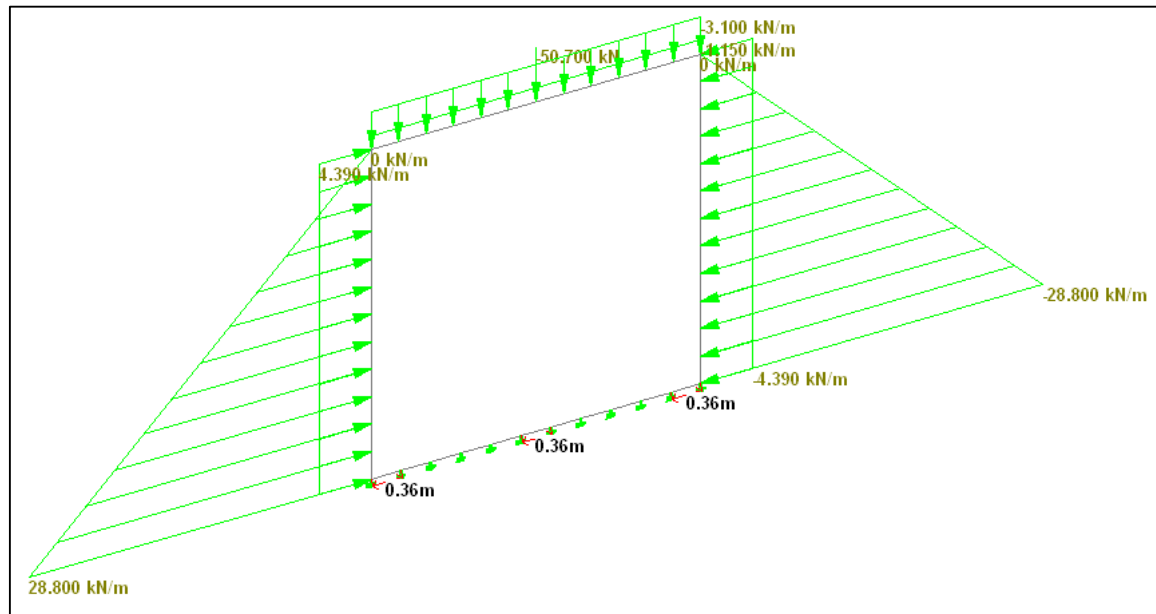


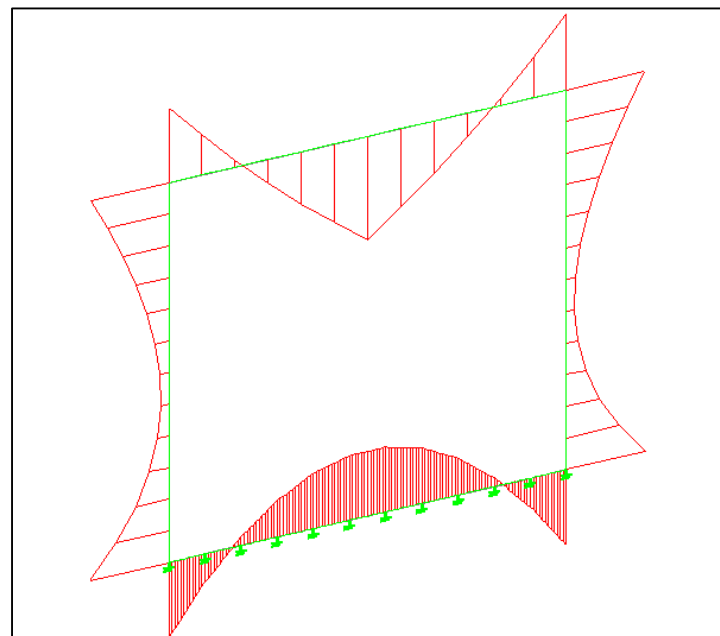
FIG 4.1 Unfactored combination of loading with Spring Support at 0.36m distance

4.1.3 Section Properties

Thickness of Vertical Wall	=	0.35 m
Thickness of Bottom Slab	=	0.30 m
Thickness of Top Slab	=	0.30 m

4.2 Flexural Moment

FIG 4.2 Flexural Moment Diagram of 1 vent Box Culvert



4.3 Calculation of Reinforcement

a) Top Slab

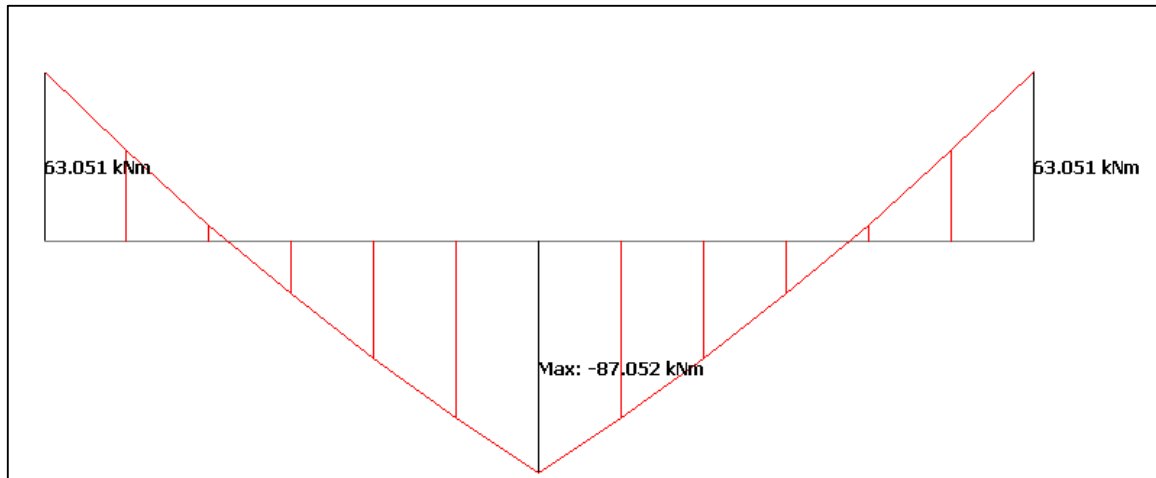


FIG 4.3 Flexural Moment(factored) Diagram of Top Slab

Reinforcement Design

Considering 1 m strip in

Design Moment = 87 kN-m/m (In top slab & in Y- direction)

Compressive strength of Concrete, $f_c' = 20$ MPa

Thickness top slab = 0.3 m

Modulus of Rupture = $0.52 \times \sqrt{f_c'} = 2.32$ MPa

Moment of Inertia = $b \times h^3 / 12 = 1 \times 0.3^3 / 12 = 0.00225$ m⁴

Cracking Moment = $2.32 \times 1000 \times 0.00225 / (0.3/2) = 35$ kN-m/m

Checking against AASHTO 07 criteria for minimum reinforcement,

Criteria 1, $1.2 \times$ Cracking moment = 42 kN-m/m

Criteria 2, $1.33 \times$ Flexural Moment = 116 kN-m/m

So, minimum reinforcement required is for 42 kN-m/m which is less than design moment 87 kN-m/m. So, design moment finally considered is 87 kN-m/m.

R16-125 is provided at the bottom of top slab for design moment of 87 kN-m/m. For top face of top slab maximum flexural moment is found for both corners. Minimum reinforcement of R16-250 is continued whereas extra reinforcement of R12-150 is provided for protecting the corners. Extra reinforcement is provided for one fourth of length in vertical and horizontal direction from outer edge of fillet.

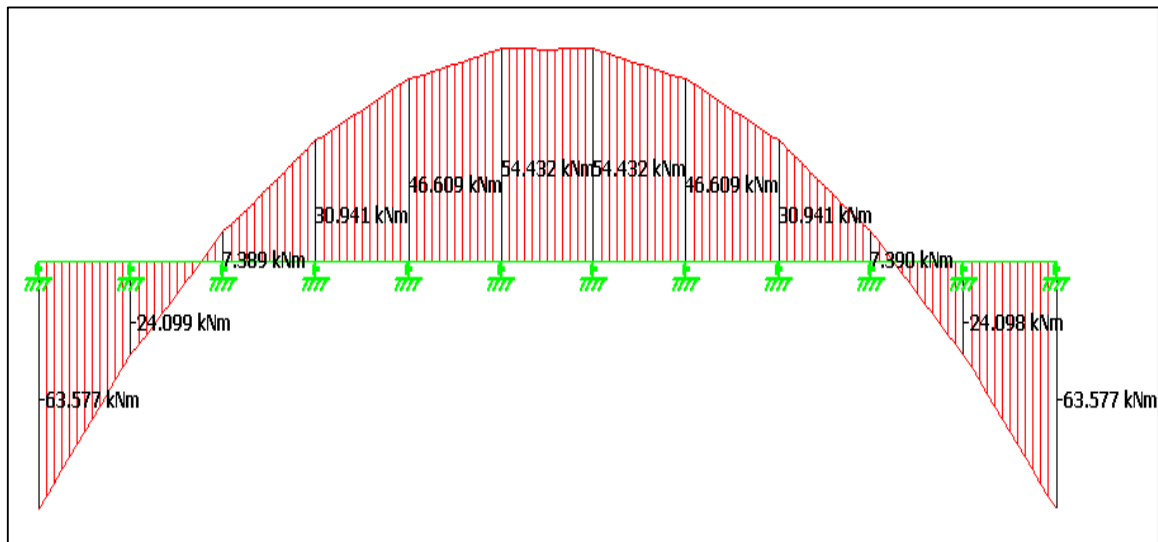
b) Bottom Slab

FIG 4.3 Flexural Moment (factored) Diagram of Bottom Slab

Reinforcement Design

Considering 1 m strip in

Design Moment = 55 kN-m/m (Top face of Bottom Slab)

Compressive strength of Concrete, $f_c' = 20$ MPa

Thickness top slab = 0.3 m

Modulus of Rupture = $0.52 \times \sqrt{f_c'} = 2.32$ MPa

Moment of Inertia = $b \times h^3 / 12 = 1 \times 0.3^3 / 12 = 0.00225 \text{ m}^4$

Cracking Moment = $2.77 \times 1000 \times 0.00225 / (0.3/2) = 35 \text{ kN-m/m}$

Checking against AASHTO 07 criteria for minimum reinforcement,

Criteria 1, $1.2 \times \text{Cracking moment} = 42 \text{ kN-m/m}$

Criteria 2, $1.33 \times \text{Flexural Moment} = 73 \text{ kN-m/m}$

So, minimum reinforcement required is for 42 kN-m/m which is less than design moment 55 kN-m/m. So, design moment finally considered is 55 kN-m/m.

R16-250 and R10-250 are provided at the top of bottom slab for design moment of 70 kN-m/m. As observed from moment diagram above, at 560mm distance from left support only minimum reinforcement is required and thus, R10-250 is continued for required length as observed from diagram in addition to another 40 times bar diameter.

c) **Vertical Wall**

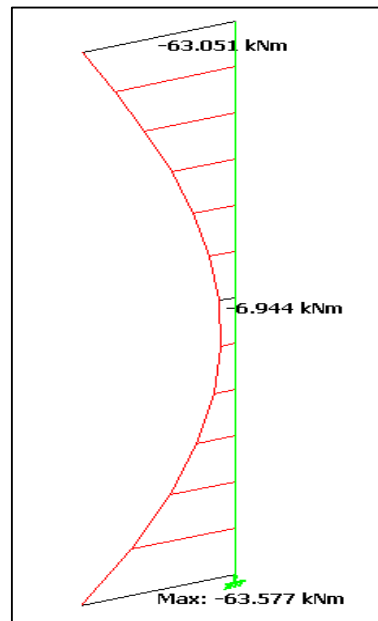


FIG 4.4 Flexural Moment Diagram (factored) of Vertical Wall

Reinforcement Design

Considering 1 m strip in

Design Moment = 64 kN-m/m (Vertical Wall)

Compressive strength of Concrete, $f_c' = 20$ MPa

Thickness top slab = 0.3 m

Modulus of Rupture = $0.52 \times \sqrt{f_c'} = 2.32$ MPa

Moment of Inertia = $b \times h^3 / 12 = 1 \times 0.3^3 / 12 = 0.0036$ m⁴

Cracking Moment = $2.32 \times 1000 \times 0.0036 / (0.35/2) = 48$ kN-m/m

Checking against AASHTO 07 criteria for minimum reinforcement,

Criteria 1, $1.2 \times$ Cracking moment = 57 kN-m/m

Criteria 2, $1.33 \times$ Flexural Moment = 85 kN-m/m

So, minimum reinforcement required is for 57 kN-m/m which is less than design moment 64 kN-m/m. So, design moment finally considered is 64 kN-m/m.

R16-250 is provided at inner and outer faces of vertical wall for design moment as minimum reinforcement. In the corner R12-250 is provided as extra reinforcement along with R16-250. R12-150 is provided for protecting the corners. Extra reinforcement is provided for one fourth of length in vertical and horizontal direction from outer edge of fillet.

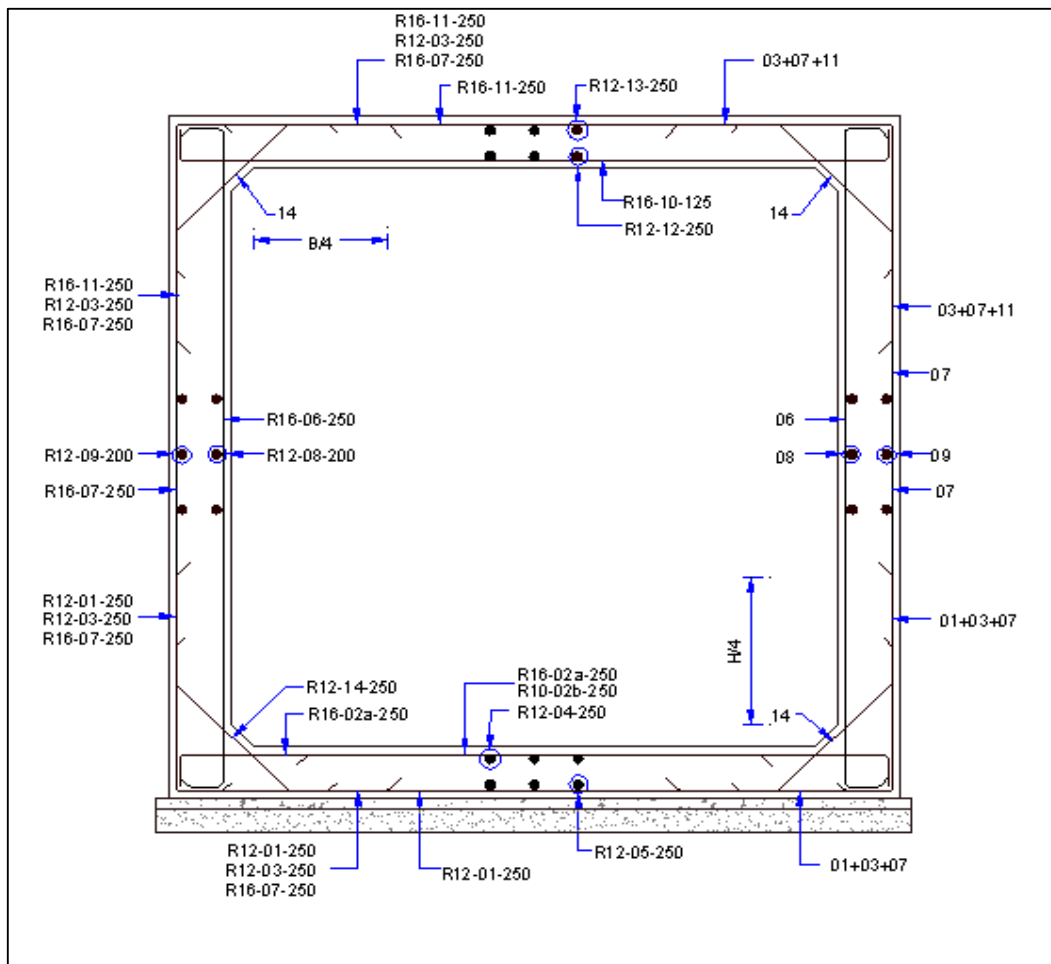


FIG 4.5 Reinforcement Details of One Vent Box Culvert

CHAPTER 5

SLOPE PROTECTION WORK

5.0 DESIGN OF PROTECTIVE WORKS BY LAUNCHING APRON

5.1 General

The calculation of slope protection work of Dharala River at Kurigram is provided here as the typical design example of protective work. The protection work is done on the right bank of the river and extended from 3.04 Km to 3.64 Km.

5.2 Design Calculation

Design Data:

Discharge	:	6093	m ³ /sec	=>	Supplied by field
High Water Level	:	31.88	m(PWD)	=>	Supplied by field
Average Low Water Level	:	27.49	m(PWD)	=>	Supplied by field
Average Flow Velocity, V	:	2	m/sec	=>	Supplied by field (Assumed)
Revetment Material					
1) For pitching			CC Blocks		
2) For dumping	:		CC Blocks		
Wind Velocity	:	70	km./h	=19.44m/sec =>	Assumed
Wind Duration	:	1	hour	=>	Assumed
Fetch Length	:	0.35	km.	=>	Supplied by field
Slope of Bank, θ	:	26.56 ⁰			
Specific Gravity, S_s	:	2.3			
Angale of Repose of Revetment Material, θ	:	40 ⁰			
Ratio of water depth and Revetment size, h/D	:	5			
Existing River Bed Level	:	24.30	m(PWD)	=>	Supplied by field
River Bend Condition	:	Moderate bend		=>	Supplied by field
Multiplying factor for Scour depth F	:	1.5			
Gravitational acceleration, g	:	9.81	m/sec ²		
Strength Co-eff. for CC Block	:	3			
revet. material. β					
Significant wave height, H_s	:	0.7	m		
Wave period, T	:	2.8	sec		
Silt factor f	:	0.8			
Slope of Protection					
Horizontal	:	2			
Vertical	:	1			

Design for Size of Revetment Material

i) Against Velocity

a) Using Neill's Method

$$\begin{aligned} D &= 0.034 \times V^2 \\ &= 0.136 \quad \text{m} \\ &= 136 \quad \text{mm} \end{aligned}$$

b) Using JMBA Equation

$$D_n = \frac{0.7 V^2}{2(S_s-1) g} \times \frac{2}{\text{Log}(6h/D)^2} \times \frac{1}{[1-(\text{Sin}q/\text{sin}f)^2]^{0.5}}$$

0.110	x	0.917	x	1.39201
0.140	m			
140	mm			

ii) Against Wave

From Table 4.1 of Design Manual for wind speed 19.44 m/sec with 1 hour duration and 0.25km Fetch

$$\begin{aligned} \text{Wave breaking parameter, } E &= 1.25 T/H_s^{0.5} \tan\theta \\ &= 2.09 \end{aligned}$$

Using Pilarczyk equation,

$$D = H_s \times 1 \times E^{1/2} / (S_s-1) \times b \times \cos\theta$$

$$= 290\text{mm}$$

Accepted size of revetment material = 290 mm

$$= 58.70 \text{ Kg}$$

Provide CC Blocks with Geotextile filter of size, L = 400 mm

$$B = 400 \text{ mm}$$

$$T = 200 \text{ mm}$$

Equivalent weight = 74 kg O.K

Thickness of Rip-Rap

a) Using English Formula

$$T = 0.06 Q^{1/3}$$

$$= 1.096 \text{ m}$$

$$= 1096 \text{ mm}$$

b) Based on stone size according to ESCAP

$$T = 1.5 D$$

$$= 435 \text{ mm}$$

Average thickness of riprap = 544 mm

Provide thickness of riprap = 750 mm

According to T.S.N Rao & Spring average thickness of sloping apron is 1.25T

Computation of scour depth

The apron is assumed to launch at 1V:2H slope

$$\text{Scour depth, } R = 0.47(Q/f)^{1/3}$$

$$= 9.25 \text{ m}$$

$$\text{Design Scour Depth} = F \times R$$

$$= 13.87 \text{ m}$$

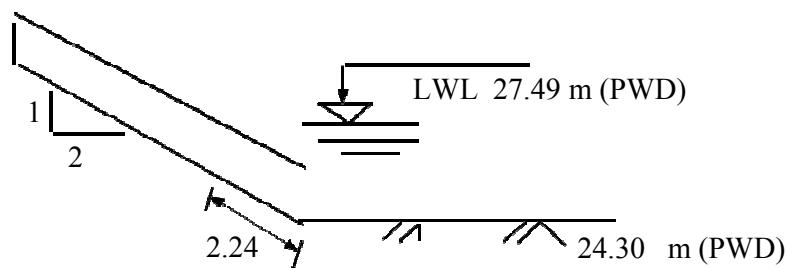
$$\text{Scour Level} = (\text{Design Water Level}) - (\text{Design Scour Depth})$$

$$= 18.01 \text{ m.PWD}$$

$$\text{Existing bed level} = 24.30 \text{ m.PWD}$$

Since existing bed level is higher than the scour level, scour level will be used for computation which is = 18.07 m (PWD)

$$\text{Depth of scour from Existing bed level} = 6.29 \text{ m}$$



$$\text{Length of Protection with 1:2 slope} = 21.20 \text{ m}$$

Use average thickness of riprap 750.00 mm

Volum of dumping blocks = Length of slopping Apron x Average thickness of Apron

= 16.00 m³/m required

Launching Apron

Since existing bed level is above the scour level, Launching apron is to be provided

Length of Launching Apron L as recommended by Inglis (1949) is 1.5 D, where d is the depth of Scour below the existing bed level

$$D = 6.29 \text{ m}$$

$$L = 9.44 \text{ m}$$

For adjustment of thickness with the specified blocks the dimensions are readjusted as follows :

Provide the launching apron as follows :

Thickness of launching apron at start : 1100.00 mm

Thickness of launching apron at end : 1500.00 mm

Length of launching apron : 8.19 m

